

# Probing pairing correlations in nuclei with $(t,p)$ reactions

Gregory Potel Aguilar

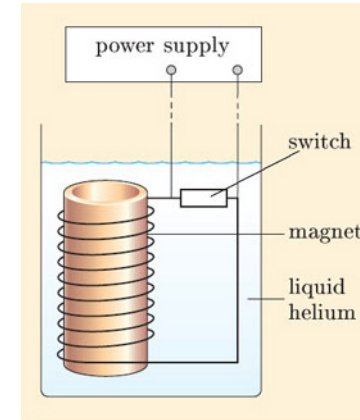
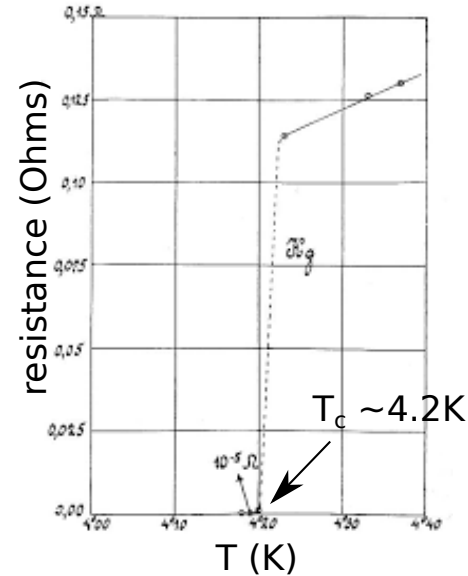
Tallahassee, March 15 2024



# Introduction: superconductivity in metals



H. Kamerlingh Onnes



- In 1911, H. K. Onnes liquefies Helium and discovers superconductivity in mercury.
- When cooled below a critical temperature (e.g.  $T_c = 7.26\text{ K}$  for lead,  $T_c = 3.69\text{ K}$  for tin), many metals become superconductors.
- Persistent supercurrents can be induced in superconducting coils.

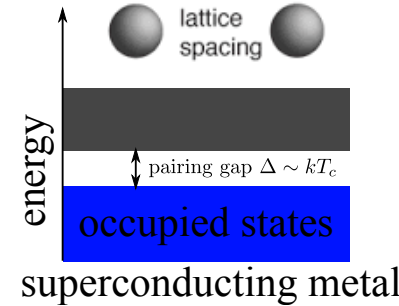
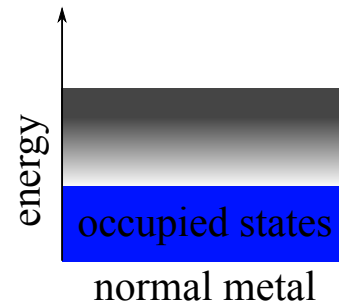
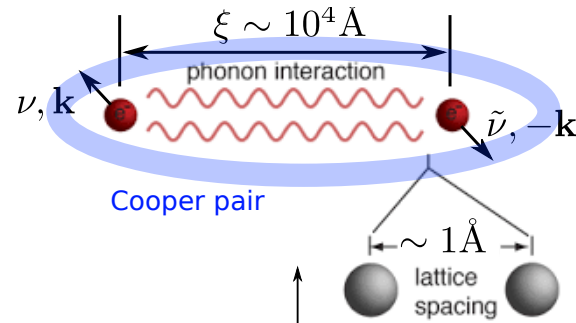
# BCS theory and Cooper pairs

Bardeen Cooper Schrieffer



BCS theory (1957)

More than 40 years later  
arrives the theoretical  
breakthrough!



- Below  $T_c$ , electrons form enormous (correlation length  $\xi \sim 10^4 \text{ \AA}$ ) quasi-bosons (Cooper pairs).
- The binding interaction results from the screening of the Coulomb force and the exchange of lattice phonons.
- An energy gap develops in the low-lying spectrum.
- The Cooper pairs form a condensate

$$|BCS\rangle = \prod_{\nu} \left( U_{\nu} + V_{\nu} e^{i\phi} a_{\nu}^{\dagger} a_{\tilde{\nu}}^{\dagger} \right) |0\rangle$$

# Some experimental evidence of nuclear superfluidity

- Gap in the spectrum of even–even nuclei associated with the breaking of a Cooper pair.
- Odd–even mass staggering: enhanced binding for even number of nucleons.
- Enhanced two–nucleon transfer reactions due to the coherence of the Cooper pair wave function.

Bohr, Mottelson and Pines (1958)

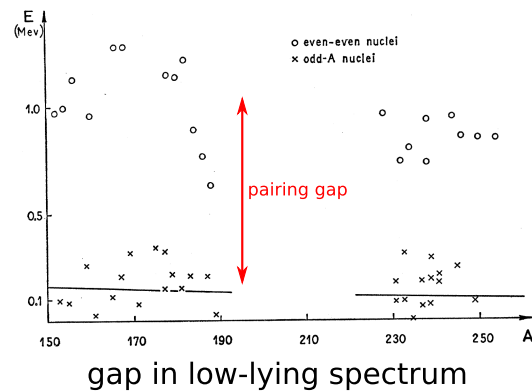
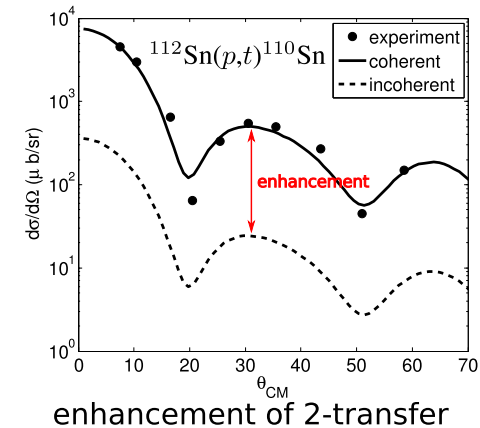
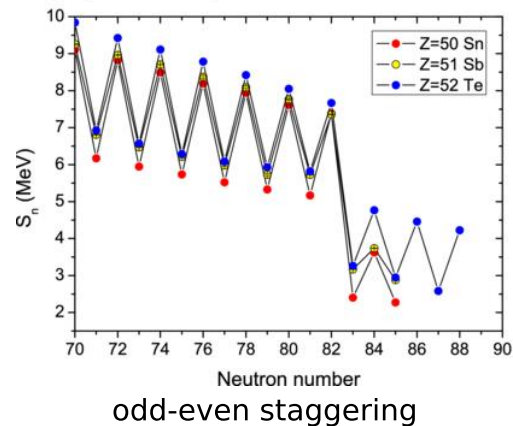
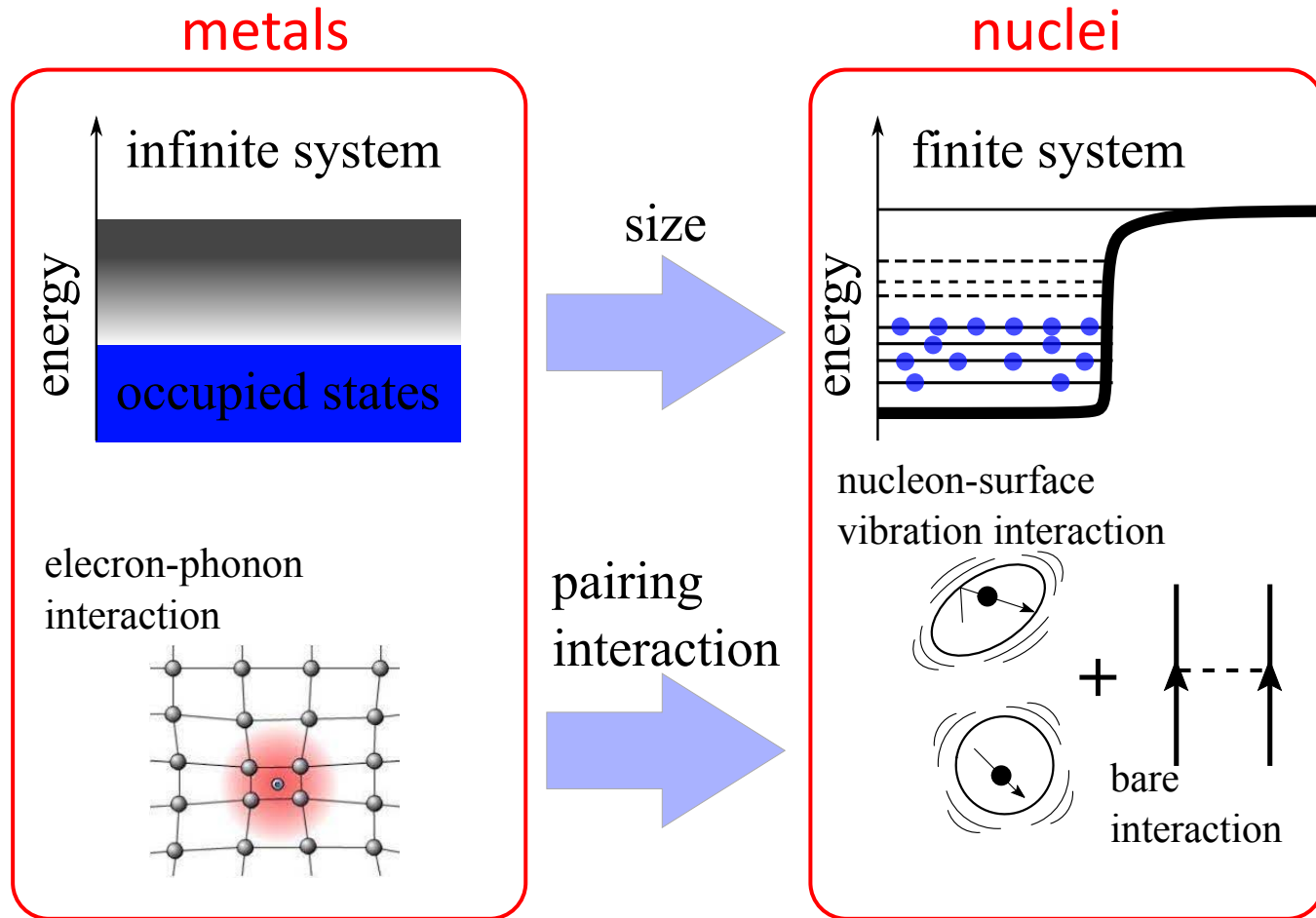


Figure 27 from A Kankainen et al  
2012 J. Phys. G: Nucl. Part. Phys. 39 093101



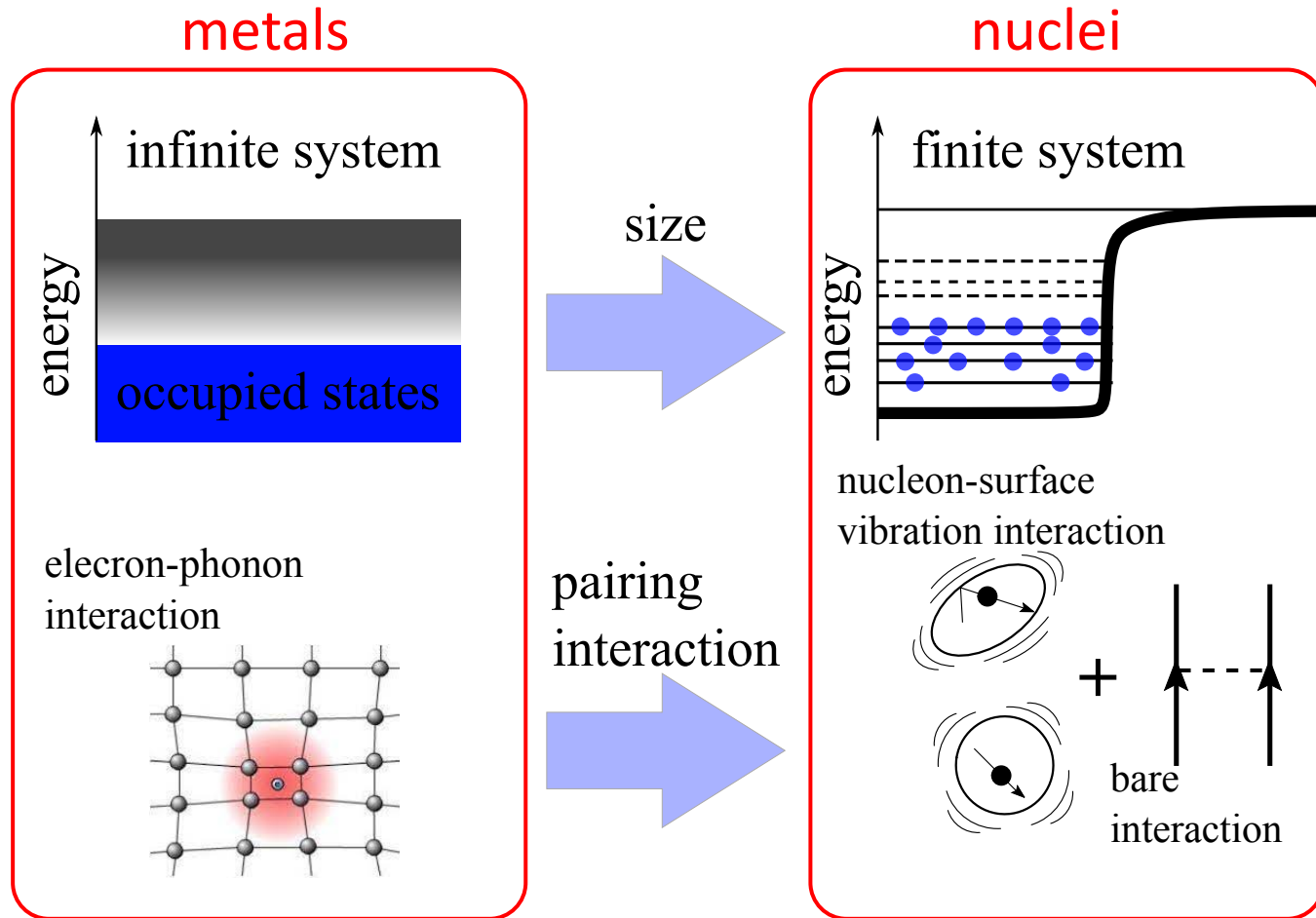
# But, metals and nuclei are quite different, aren't they?



## questions still arise

- Can we observe Cooper pairs in nuclei?
- How do we make a quantitative assessment of pair correlations in nuclei?
- How do we export our knowledge of nuclear superfluidity to nuclear matter?

# But, metals and nuclei are quite different, aren't they?

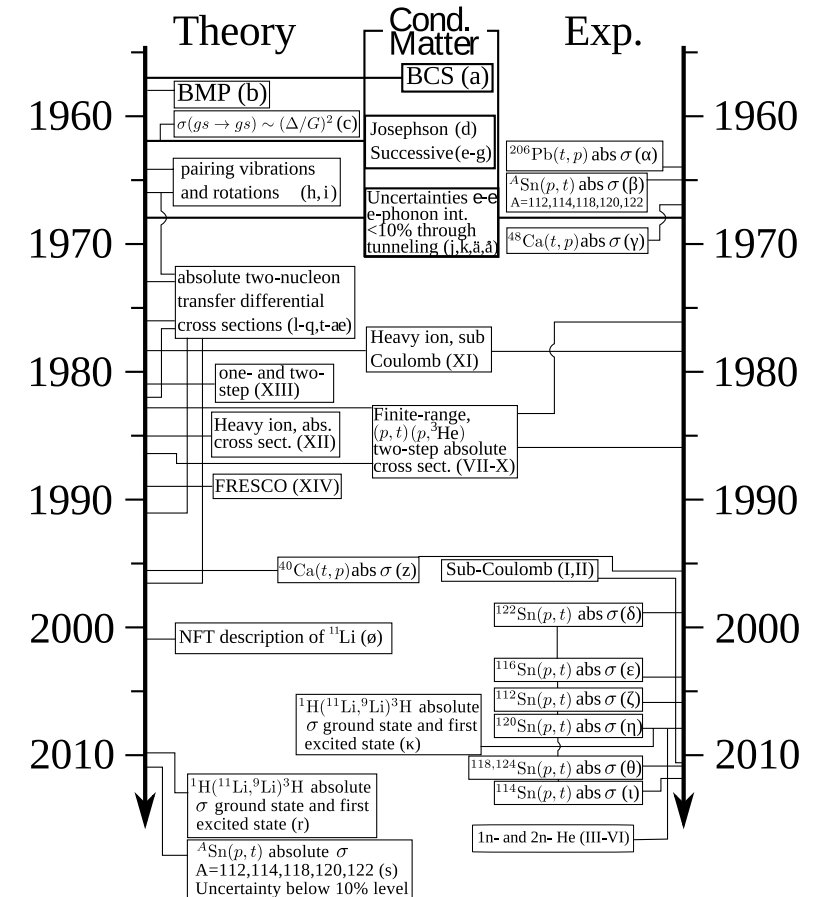
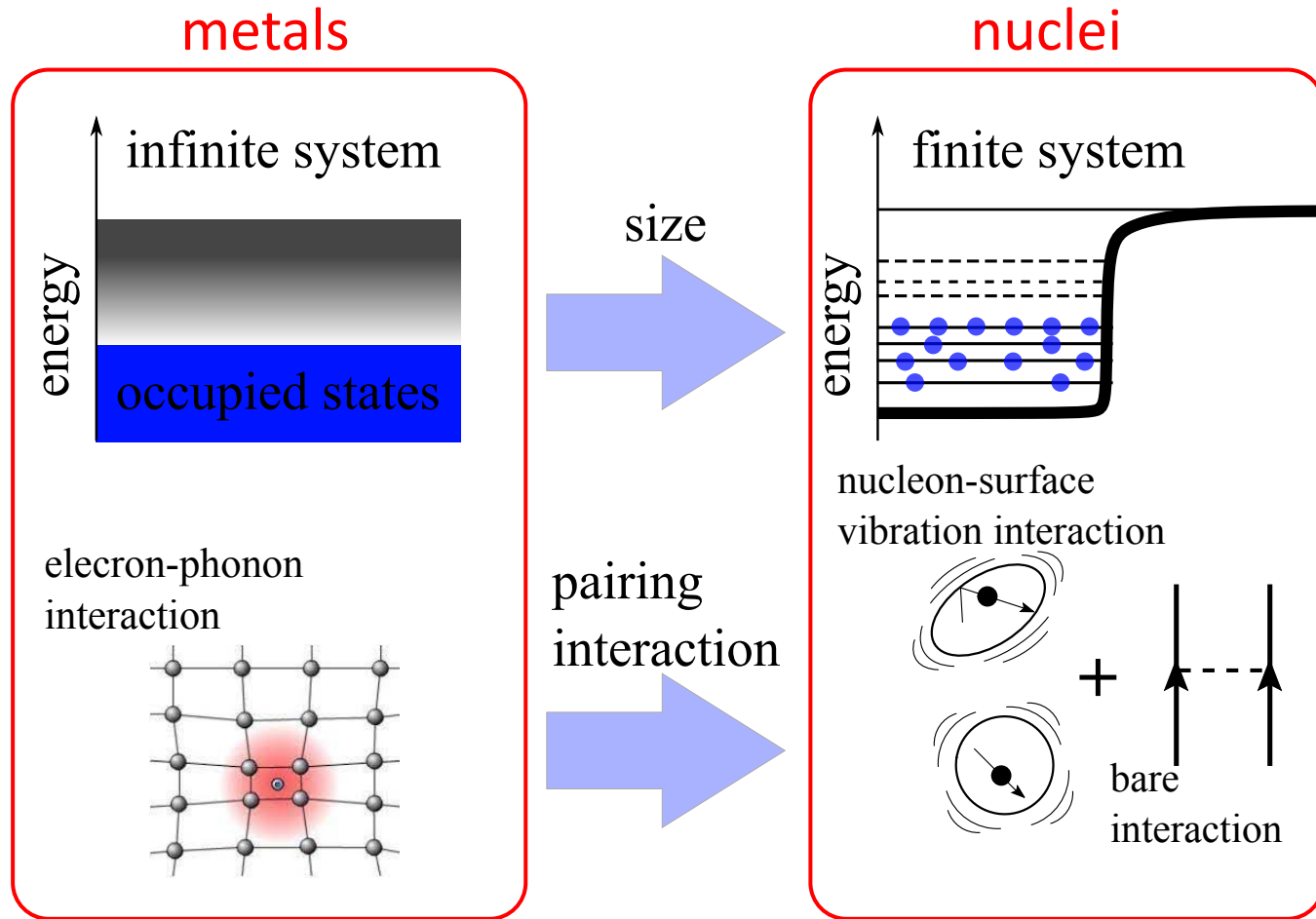


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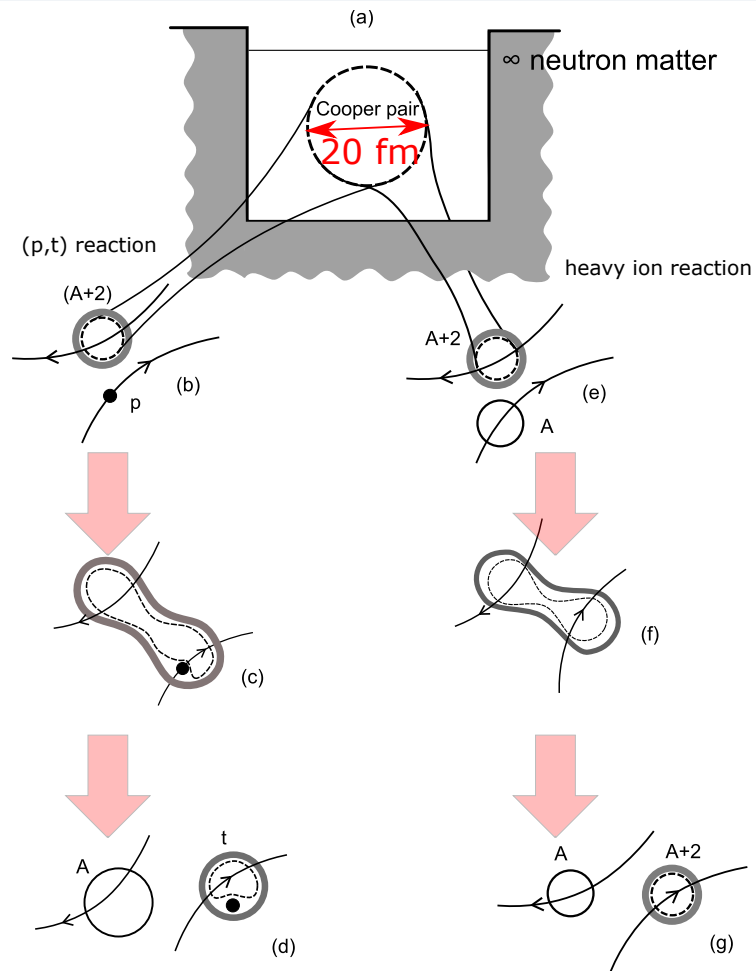
(t,p) reactions are a specific probe of nuclear pairing correlations

# But, metals and nuclei are quite different, aren't they?



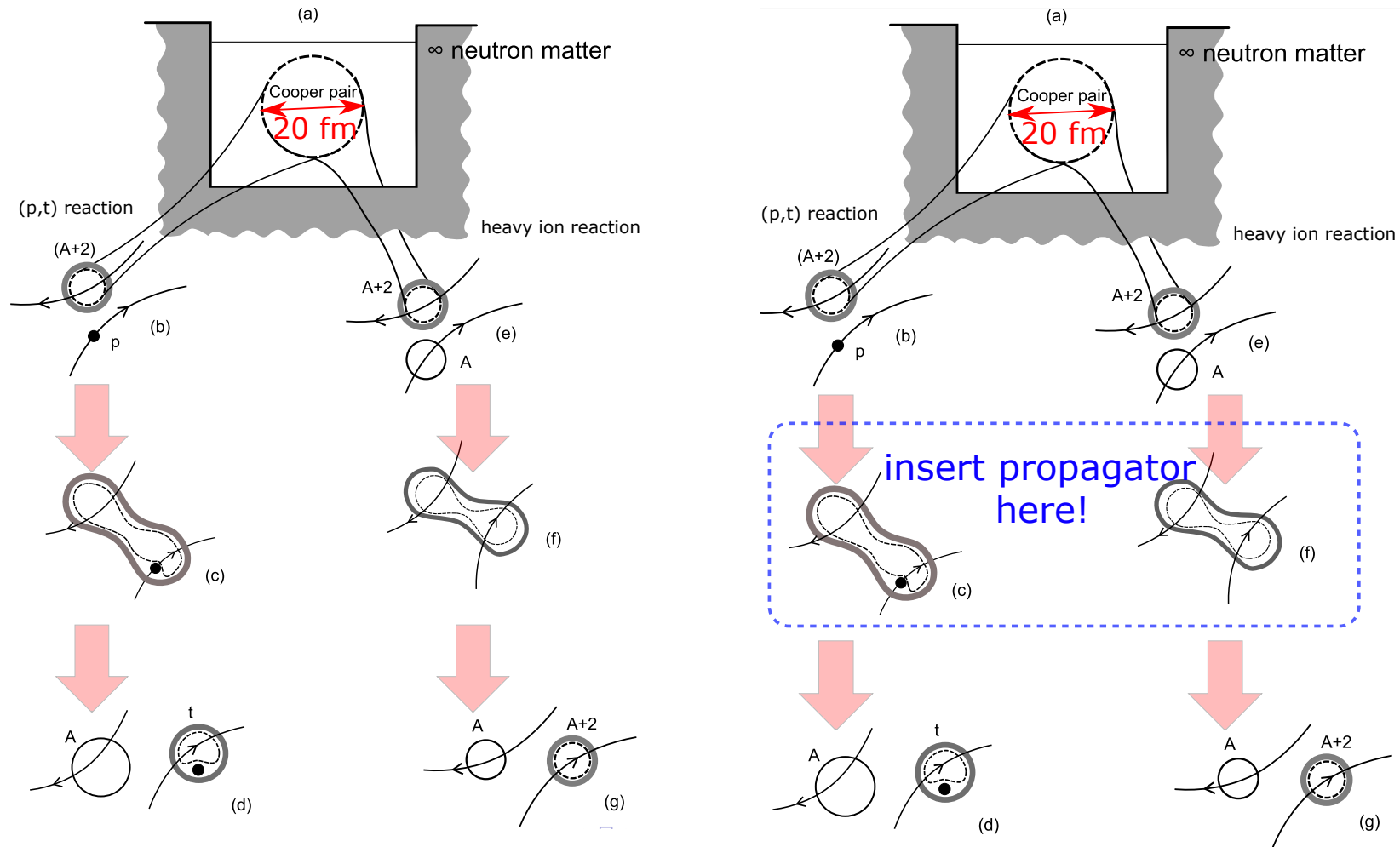
Rep. Prog. Phys. **76** (2013) 106301  
GP, Idini, Barranco, Vigezzi, Broglia

# The 2 neutron transfer process is very delocalized

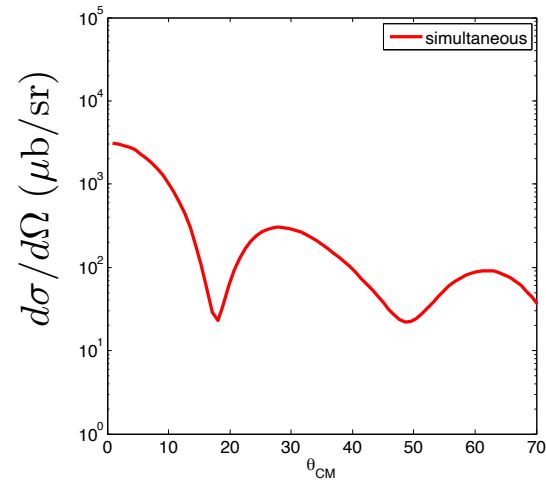




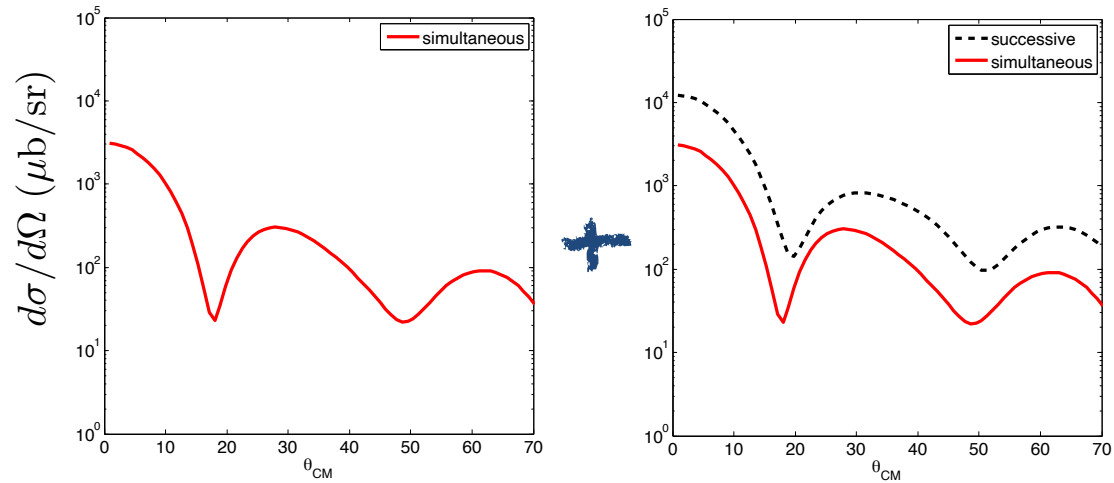
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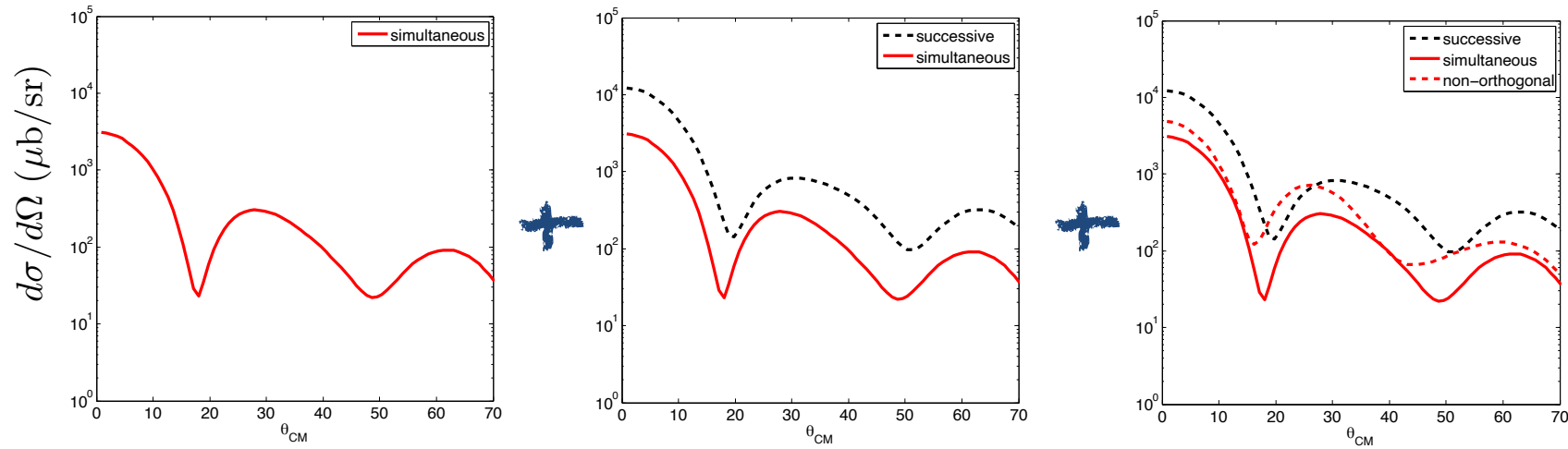
# Computing $^{112}\text{Sn}(p,t)^{110}\text{Sn}$ in second order DWBA



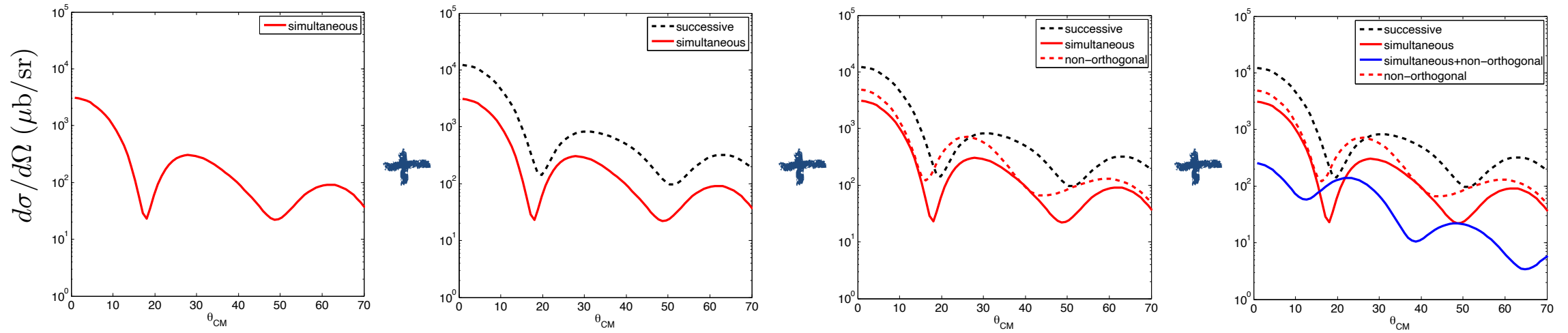
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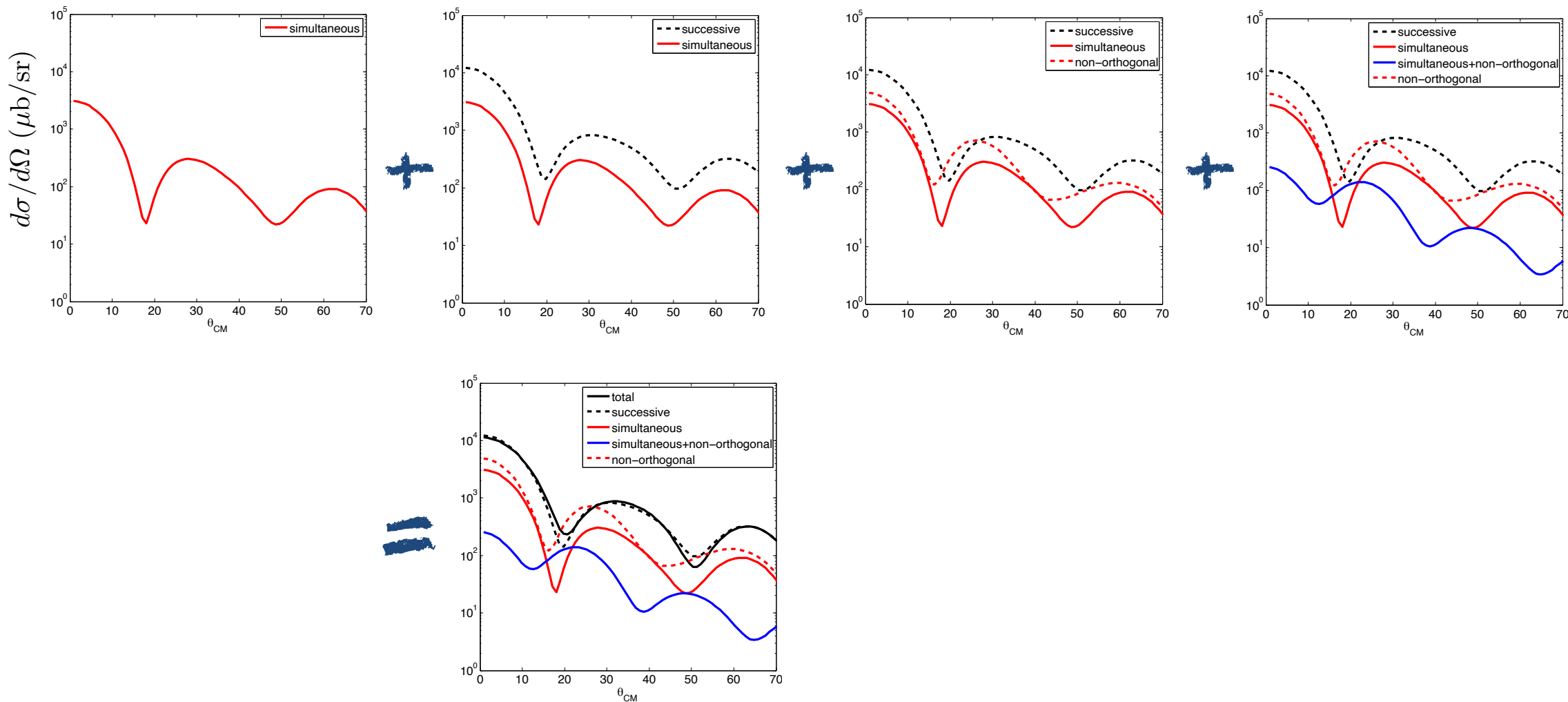
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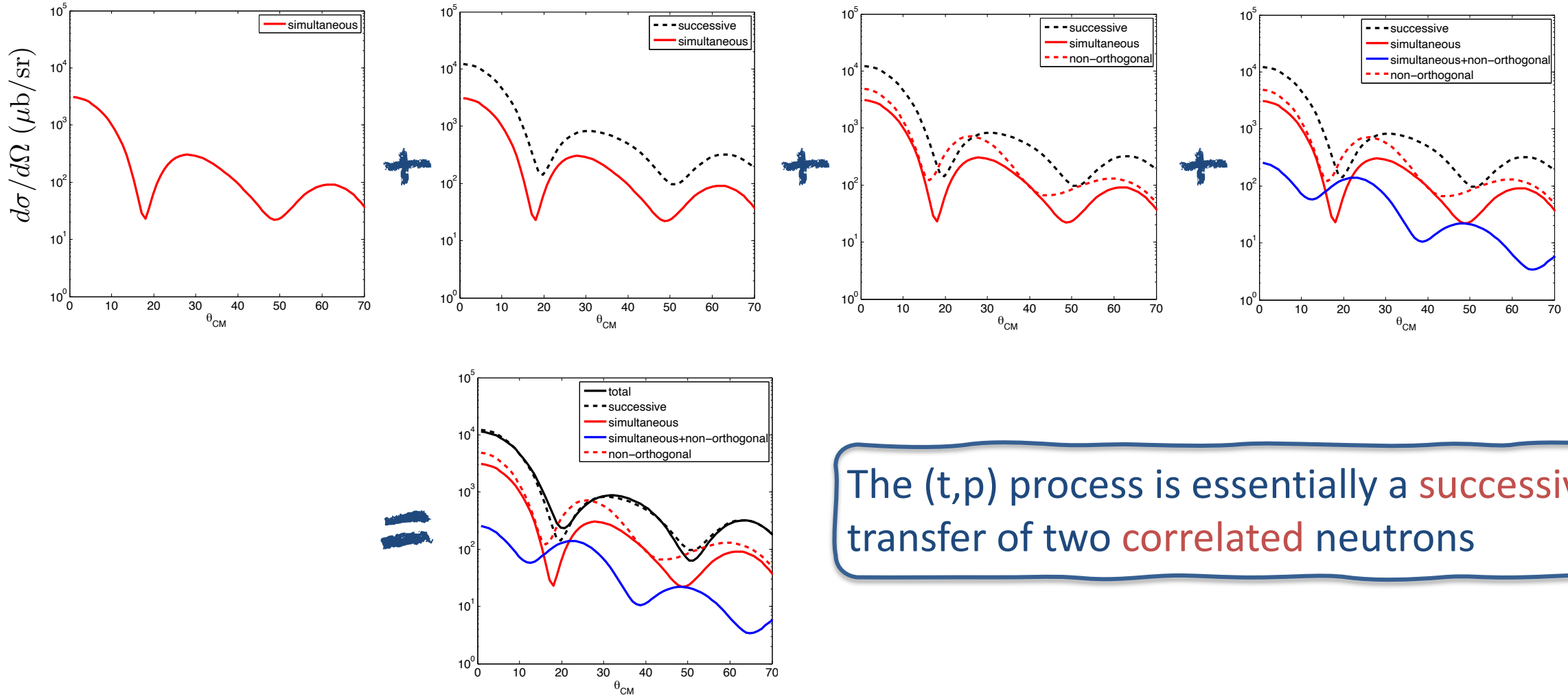
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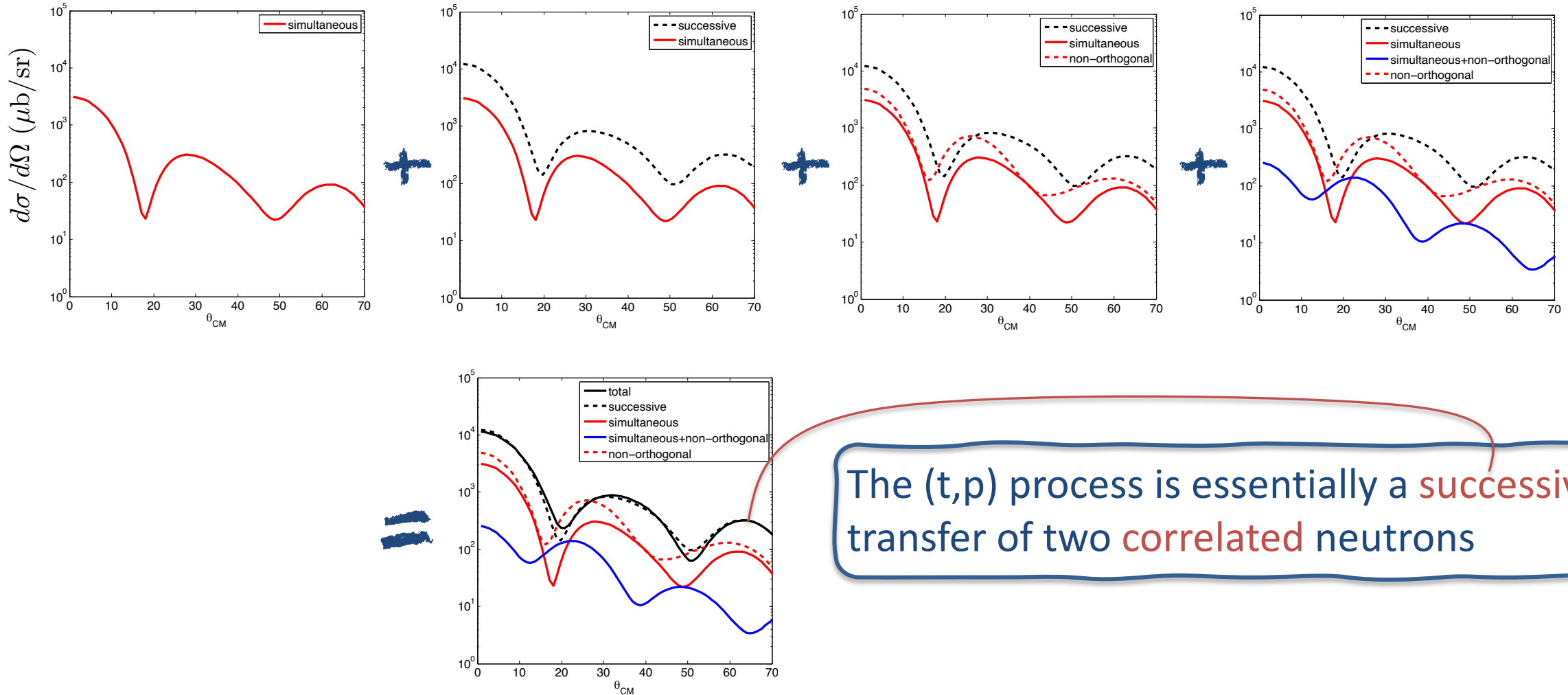


# Computing $^{112}\text{Sn}(p,t)^{110}\text{Sn}$ in second order DWBA



The (t,p) process is essentially a **successive** transfer of two **correlated** neutrons

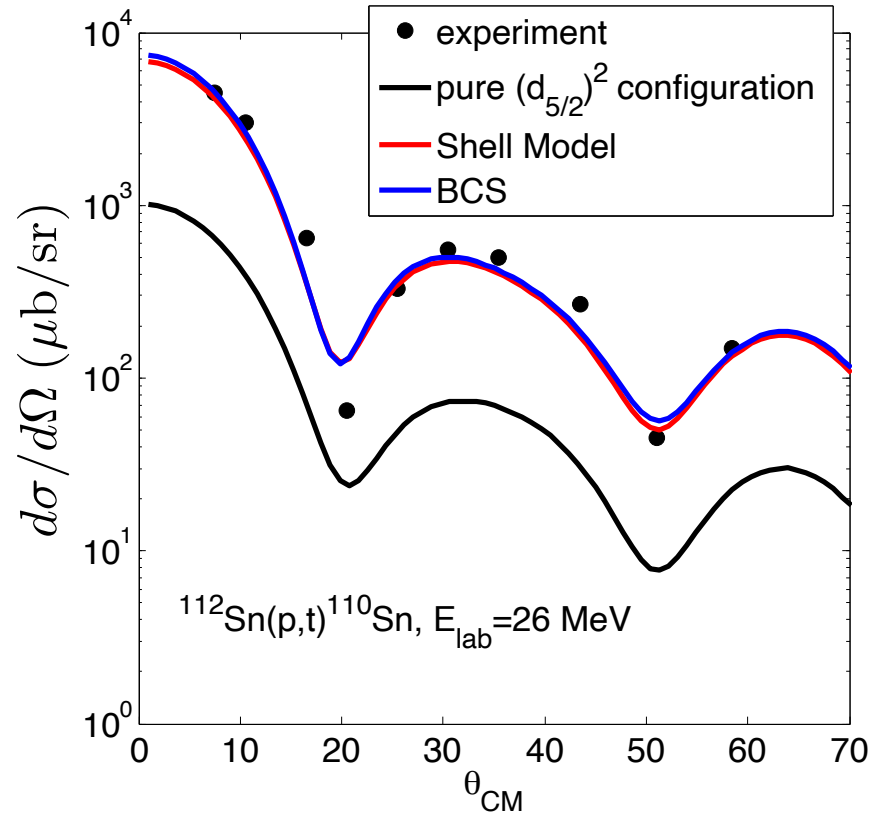
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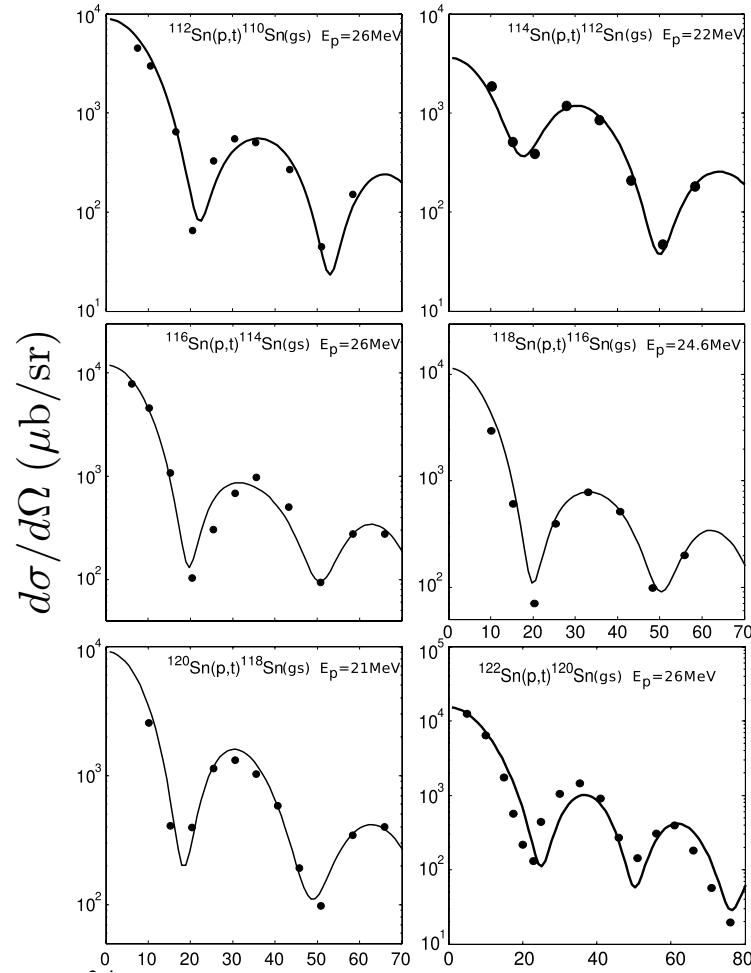
# Theory should account for the *absolute value* of the cross section



enhancement factor with respect to the transfer of uncorrelated neutrons:  
 $\epsilon = 20.6$

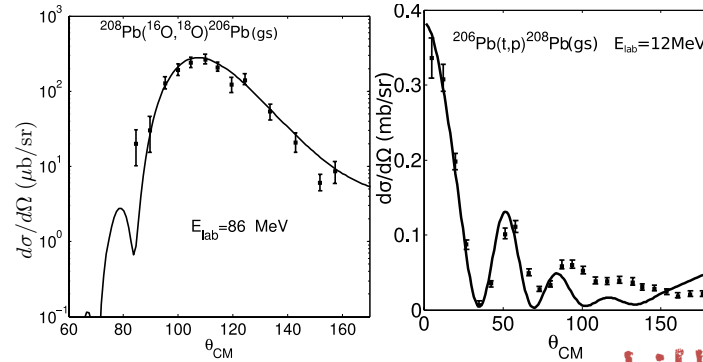
Experimental data and shell model wavefunction from Guazzoni *et al.*  
PRC **74** 054605 (2006)

# Reaction+Structure theory works well across the nuclear chart



Sn isotopes (BCS)

Pb ground state and excited states (QRPA)

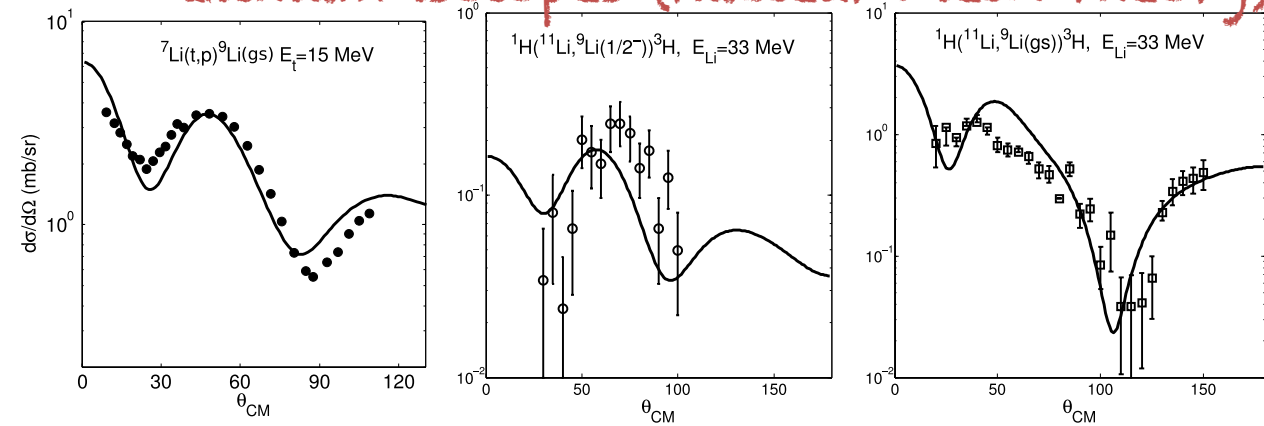


Rep. Prog. Phys. **76** (2013) 106301 (21pp)

## Cooper pair transfer in nuclei

G Potel<sup>1</sup>, A Idini<sup>2,3,4</sup>, F Barranco<sup>5</sup>, E Vigezzi<sup>4</sup> and R A Broglia<sup>3,4,6,7</sup>

Lithium isotopes (Nuclear Field Theory)



# Looking for something new in the nuclear spectrum: The Giant Pairing Vibration (GPV)

Volume 69B, number 2

PHYSICS LETTERS

1 August 1977

## HIGH-LYING PAIRING RESONANCES★

R.A. BROGLIA

*The Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen Ø, Denmark<sup>1</sup>  
State University of New York, Department of Physics, Stony Brook, New York 11794, USA*

and

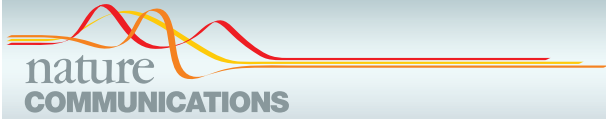
D.R. BES<sup>2</sup>

*NORDITA, DK-2100 Copenhagen Ø, Denmark*

Pairing vibrations based on the excitation of pairs of particles and holes across major shells are predicted at an excitation energy of about  $70/A^{1/3}$  MeV and carrying a cross section which is 20%–100% the ground state cross section.

Collective pairing mode predicted almost 50 years ago, awaiting experimental confirmation?

# (t,p) is an ideal process to populate the elusive Giant Pairing Vibration



ARTICLE

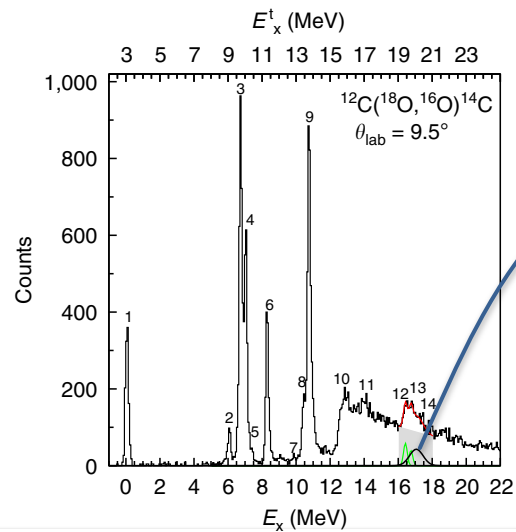
Received 28 Dec 2014 | Accepted 24 Feb 2015 | Published 27 Mar 2015

DOI: 10.1038/ncomms7743

OPEN

## Signatures of the Giant Pairing Vibration in the $^{14}\text{C}$ and $^{15}\text{C}$ atomic nuclei

F. Cappuzzello<sup>1,2</sup>, D. Carbone<sup>2</sup>, M. Cavallaro<sup>2</sup>, M. Bondi<sup>1,2</sup>, C. Agodi<sup>2</sup>, F. Azaiez<sup>3</sup>, A. Bonaccorso<sup>4</sup>, A. Cunsolo<sup>2</sup>, L. Fortunato<sup>5,6</sup>, A. Foti<sup>1,7</sup>, S. Franchoo<sup>3</sup>, E. Khan<sup>3</sup>, R. Linares<sup>8</sup>, J. Lubian<sup>8</sup>, J.A. Scarpaci<sup>9</sup> & A. Vitturi<sup>5,6</sup>



bump in the continuum populated by the reaction  $^{12}\text{C}(^{18}\text{O}, ^{16}\text{O})^{14}\text{C}$

# (t,p) is an ideal process to populate the elusive Giant Pairing Vibration



## ARTICLE

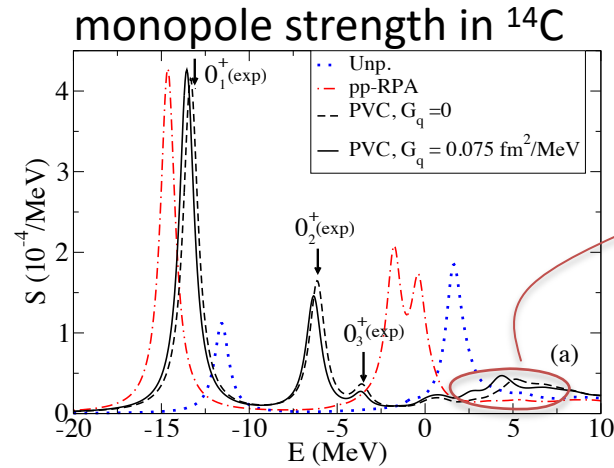
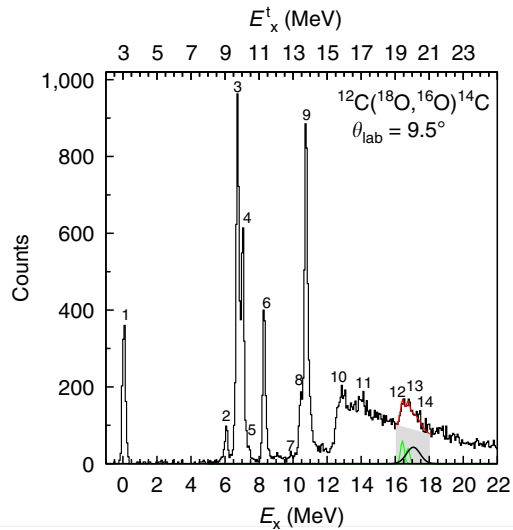
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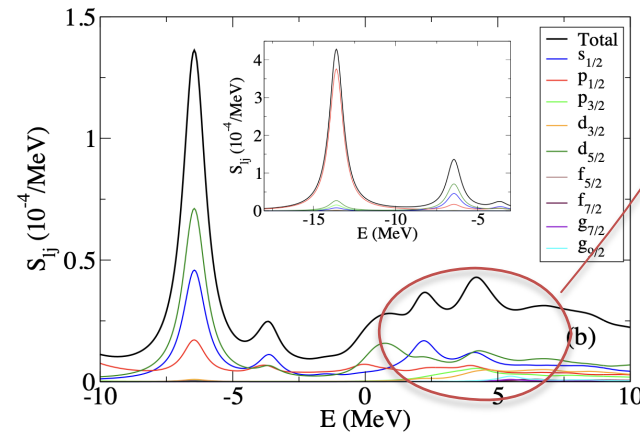
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we predict a rather broad structure in the continuum



Fragmentation of the Giant Pairing Vibration in  $^{14}\text{C}$  induced by many-body processes

F. Barranco,<sup>1</sup> G. Potel,<sup>2</sup> and E. Vigezzi<sup>3</sup>

# (t,p) is an ideal process to populate the elusive Giant Pairing Vibration



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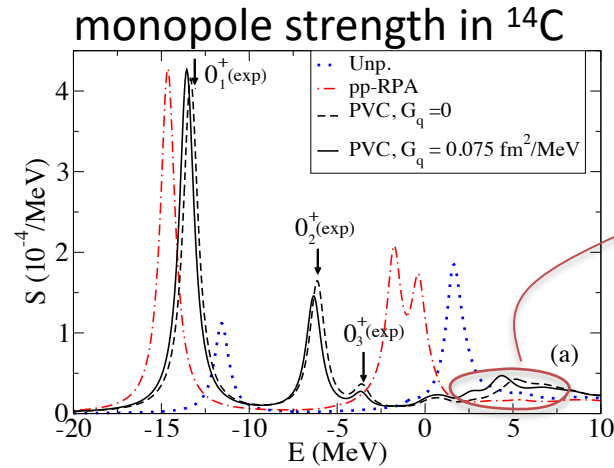
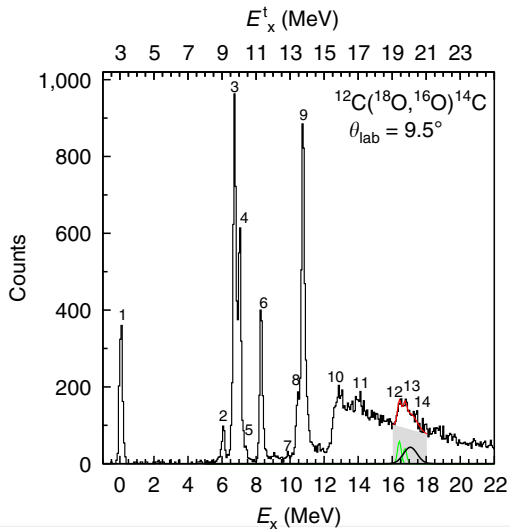
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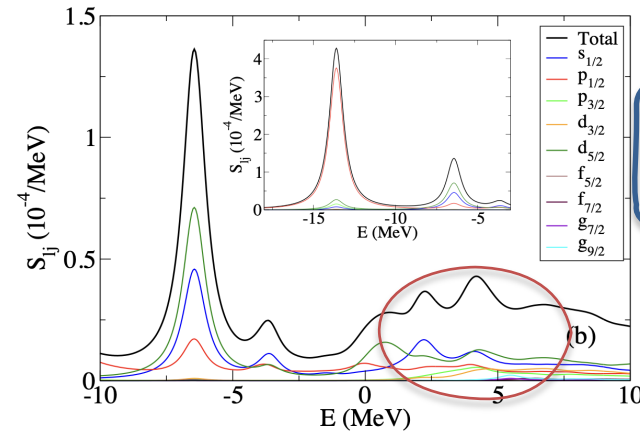
OPEN

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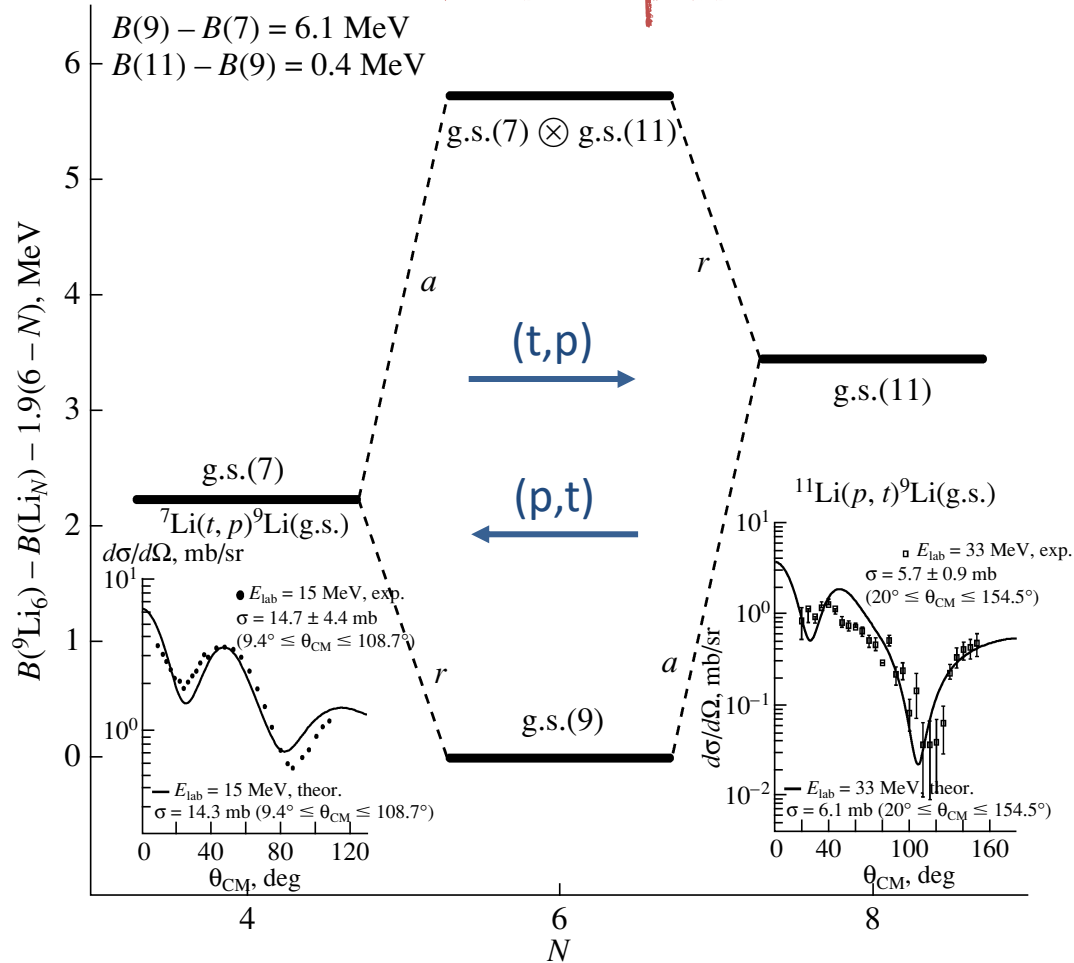
working on a theoretical estimate of  $^{12}\text{C}(t,p)^{14}\text{C}(\text{GPV})$

Fragmentation of the Giant Pairing Vibration in  $^{14}\text{C}$  induced by many-body processes

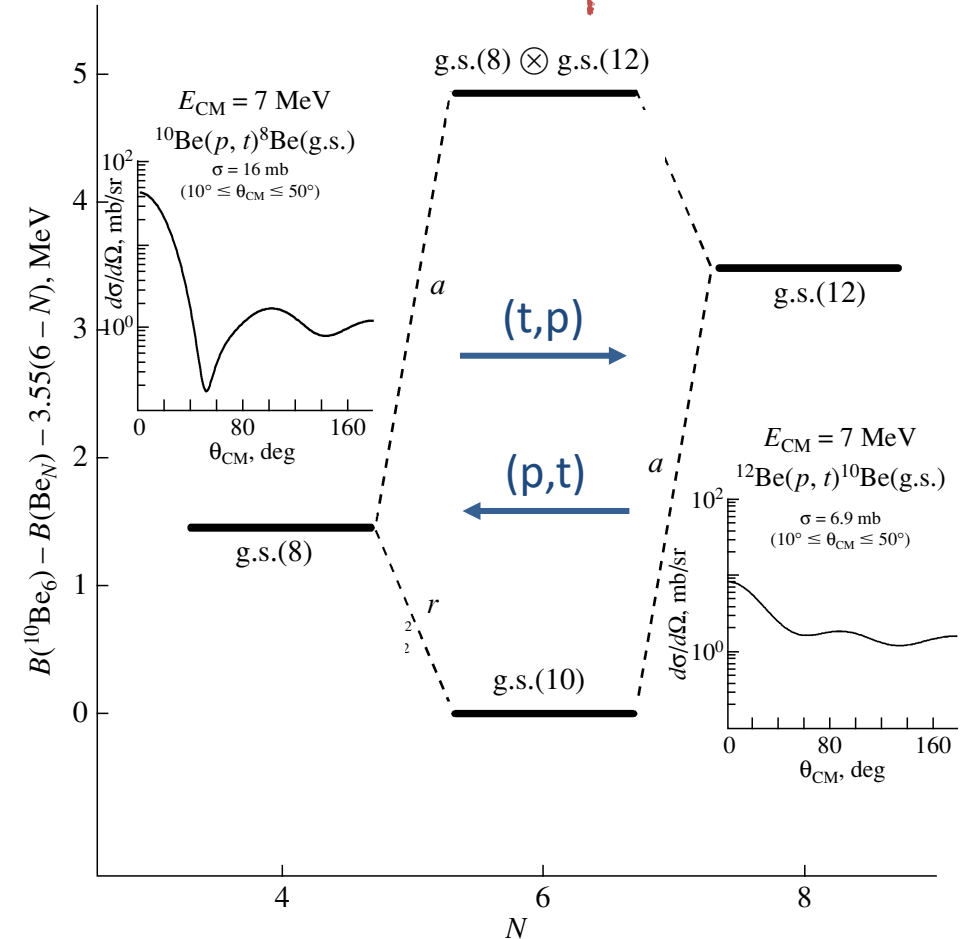
F. Barranco,<sup>1</sup> G. Potel,<sup>2</sup> and E. Vigezzi<sup>3</sup>

# Excited halo state in $^{12}\text{Be}$ ( $0^+_2$ )

## Li isotopes

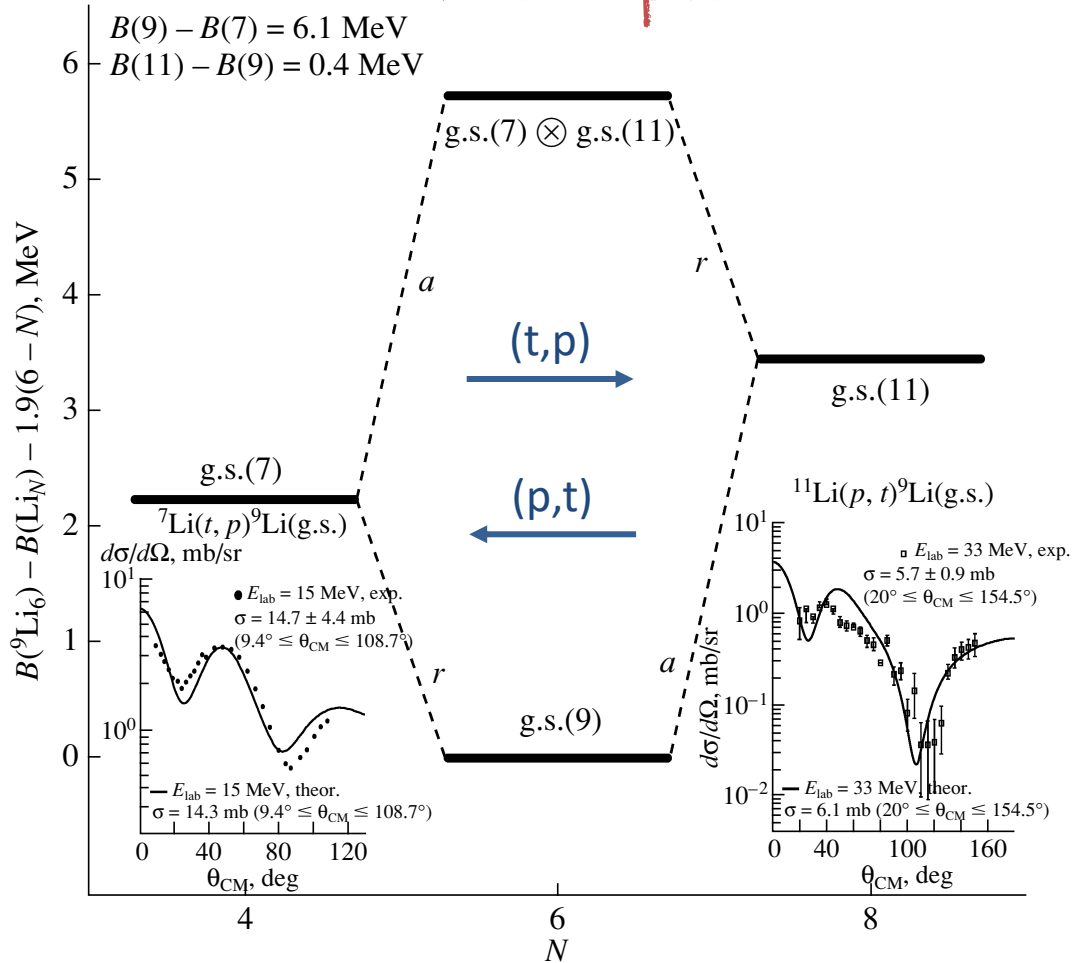


## Be isotopes

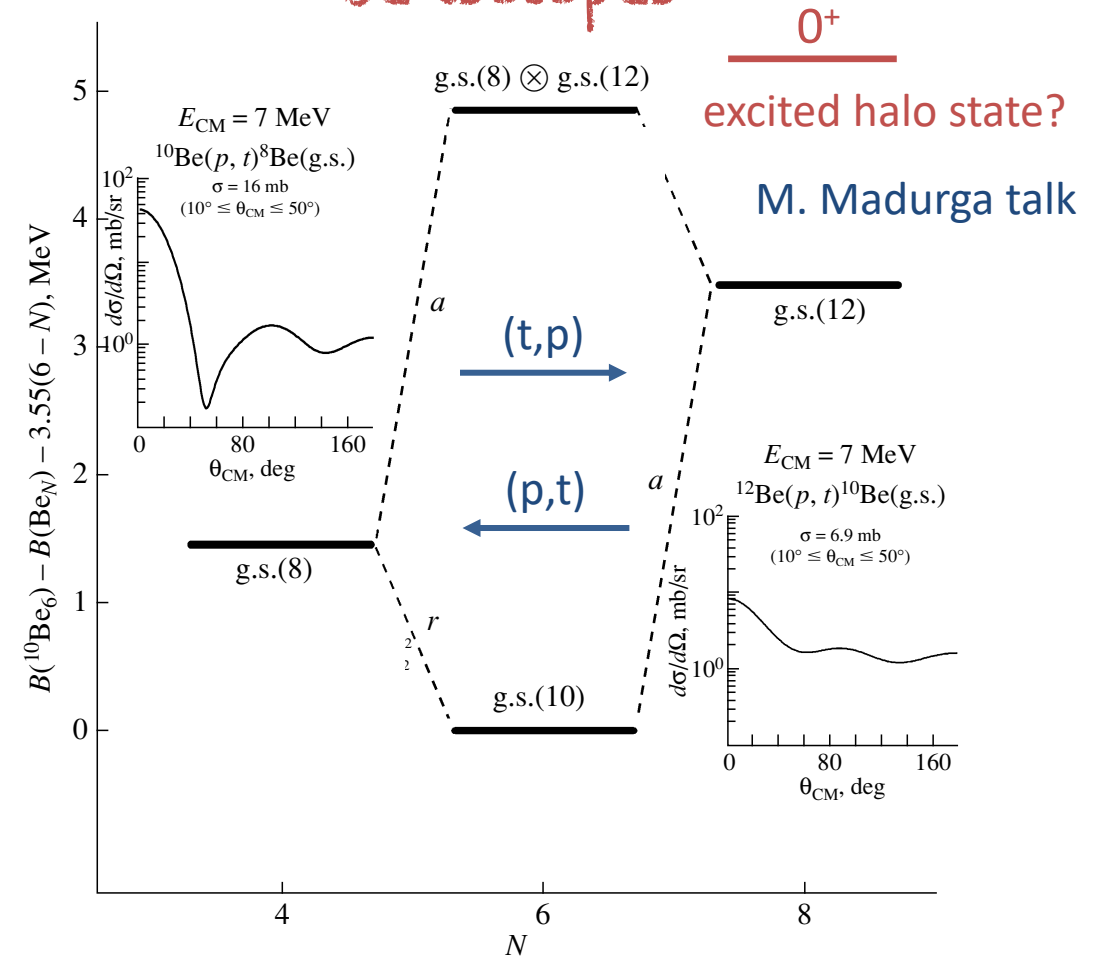


# Excited halo state in $^{12}\text{Be}$ ( $0^+_2$ )

## Li isotopes



## Be isotopes





# The Pygmy Dipole Resonance (**PDR**) as a two-quasiparticle mode

- The **PDR** is rather well described in the harmonic approximation (RPA, QRPA) as a **two-quasiparticle mode**.
- Therefore, PDR in a nucleus  $A_0$  can be better **probed** with two-quasiparticle fields, i.e., particle-hole (**ph**), particle-particle (**pp**), and hole-hole (**hh**) fields.

**ph**

Coulomb, inelastic, and  $\gamma$ -induced excitation on  $A_0$ :

- $A_0(d,d')A_0(\text{PDR})$
- $A_0(p,p')A_0(\text{PDR})$
- $A_0(\alpha,\alpha')A_0(\text{PDR})$
- $A_0(\gamma,\gamma')A_0(\text{PDR})$
- $A_0(n,n')A_0(\text{PDR})$
- $A_0(X,X')A_0(\text{PDR})$

one-nucleon transfer on  $A_0-1$ :

- $A_0-1(d,p)A_0(\text{PDR})$   
Spieker et al., PRL (2020)
- Weinert et al., PRL (2021)

**pp**

two-nucleon transfer on  $A_0-2$ :

- $A_0-2(t,p)A_0(\text{PDR})$

**proposed  
in this talk**

# The Pygmy Dipole Resonance (**PDR**) as a two-quasiparticle mode

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complementary classification of dipole modes

isovector



isoscalar

ph

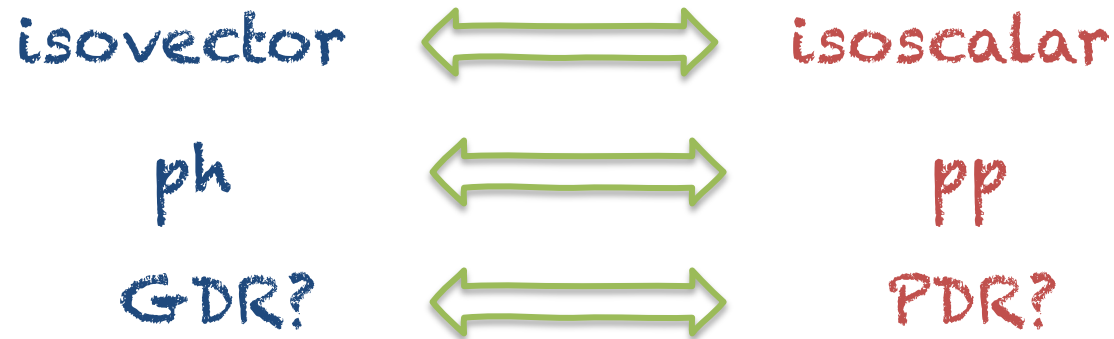


pp

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complementary classification of dipole modes



# Probing the $^{11}\text{Li}$ PDR with 2-neutron transfer

Eur. Phys. J. A (2019) 55: 243  
DOI 10.1140/epja/i2019-12789-y

THE EUROPEAN  
PHYSICAL JOURNAL A

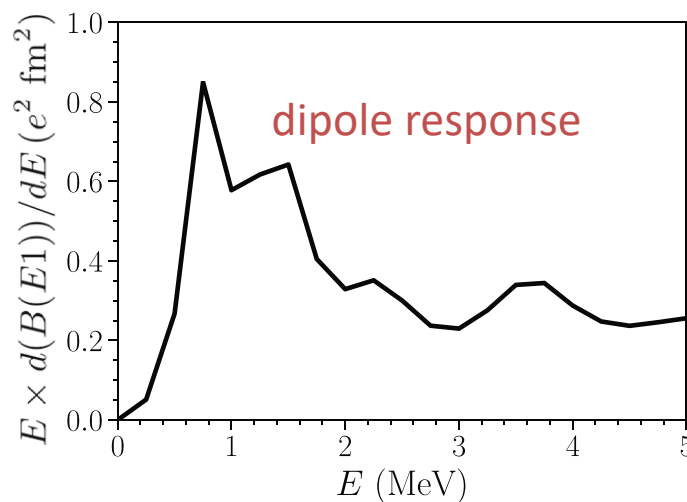
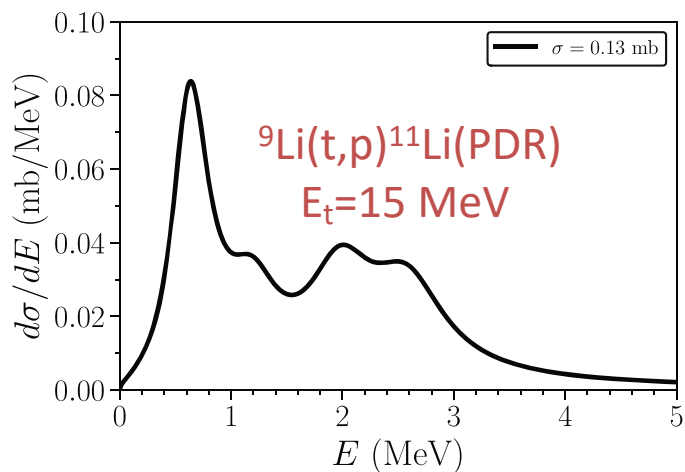
Regular Article – Theoretical Physics

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

## Characterization of vorticity in pygmy resonances and soft-dipole modes with two-nucleon transfer reactions\*

R.A. Broglia<sup>1,2</sup>, F. Barranco<sup>3</sup>, G. Potel<sup>4,a</sup>, and E. Vigezzi<sup>5</sup>

Probing the  $^{11}\text{Li}$  low-lying dipole strength via  $^9\text{Li}(t,p)$  with the ISS

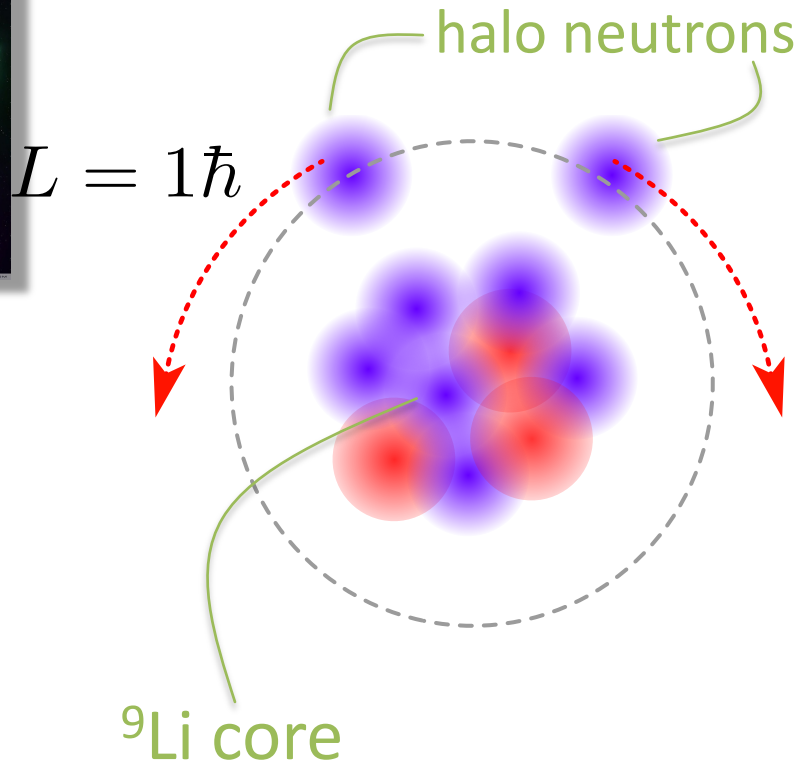


Y. Ayyad<sup>1</sup>, E. Vigezzi<sup>2</sup>, G. Potel<sup>3</sup>, R. Broglia<sup>4,5</sup>, B.P. Kay<sup>6</sup>,  
A.O. Macchiavelli<sup>7</sup>, H. Alvarez-Pol<sup>8</sup>, F. Barranco<sup>9</sup>, D. Bazin<sup>1,10</sup>, M. Caamaño<sup>8</sup>,  
A. Ceulemans<sup>11</sup>, J. Chen<sup>1</sup>, H.L. Crawford<sup>7</sup>, B. Fernández-Domínguez<sup>8</sup>, S.J. Freeman<sup>12</sup>,  
L.P. Gaffney<sup>13</sup>, C.R. Hoffman<sup>6</sup>, R. Kanungo<sup>14</sup>, C. Morse<sup>7</sup>, O. Poleshchuk<sup>11</sup>, R. Raabe<sup>11</sup>,  
C.A. Santamaria<sup>7</sup>, D.K. Sharp<sup>12</sup>, T. L. Tang<sup>6</sup>, K. Wimmer<sup>15</sup>, A.H. Wuosmaa<sup>16</sup>

experiment approved at ISOLDE facility  
(CERN). Spokepersons: Ayyad, Vigezzi

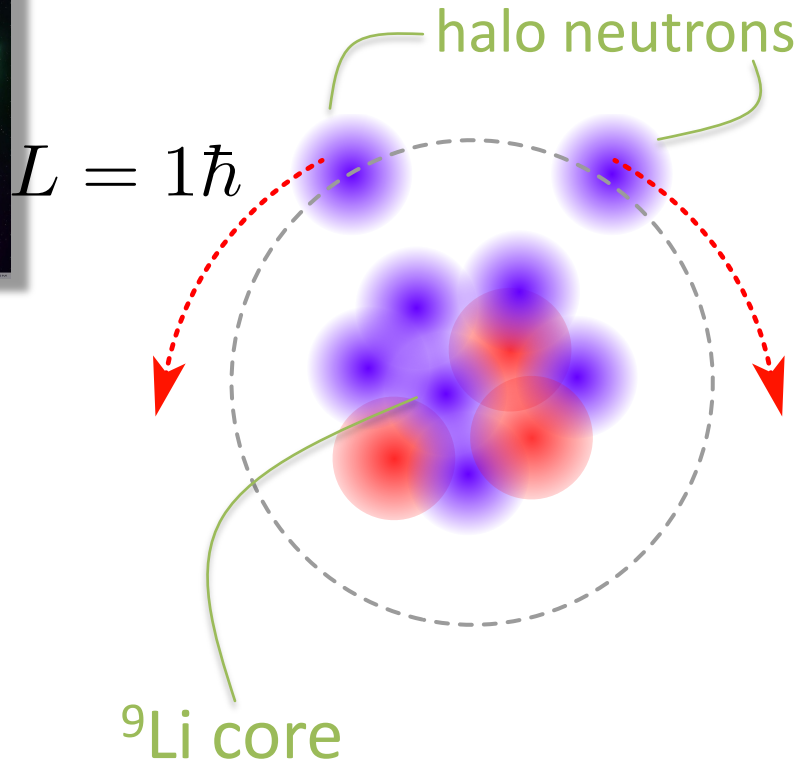
# the $^{11}\text{Li}$ PDR has the structure of an elementary quantum vortex

structure of a multipolar ( $1^-$ ) Cooper pair:  
elementary quantum vortex



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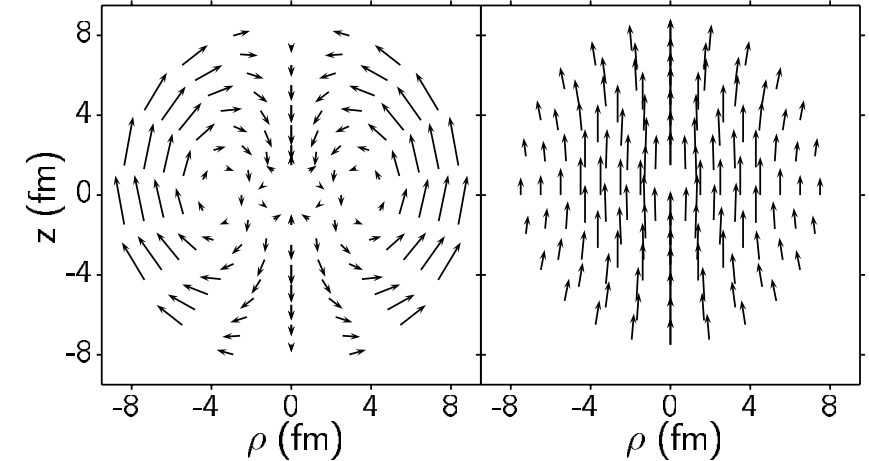
structure of a multipolar ( $1^-$ ) Cooper pair:  
elementary quantum vortex



velocity field of  $^{208}\text{Pb}$  dipole states

$E_x = 6.5 - 10.5$  MeV

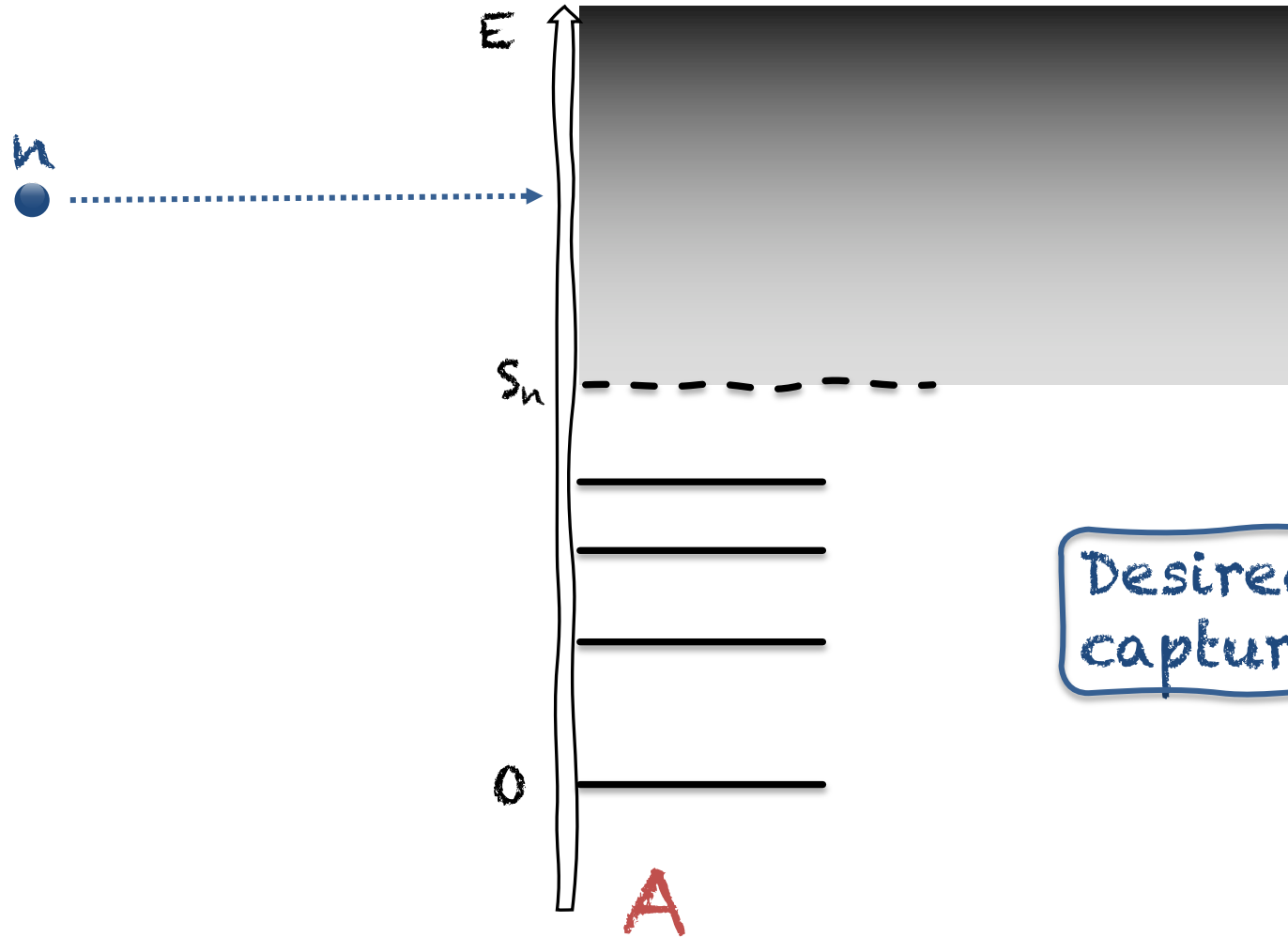
$E_x > 10.5$  MeV



Ryezayeva *et al.* PRL **89** (2002) 272502

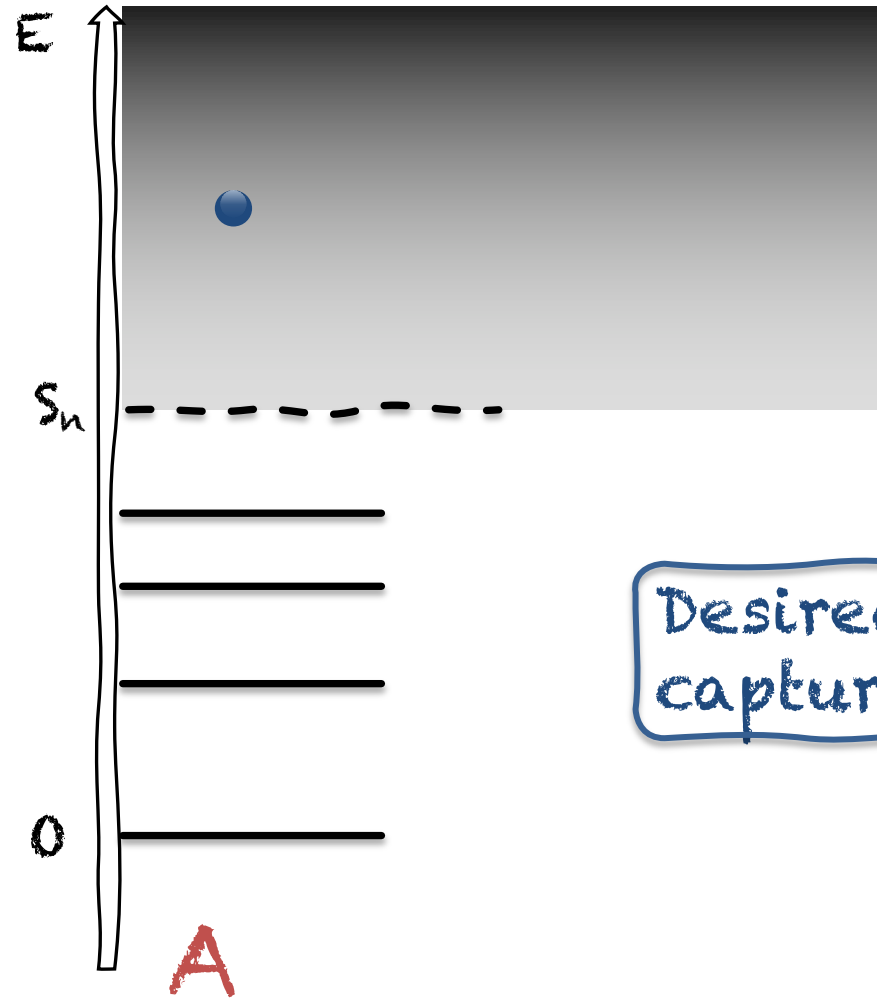
- Is vorticity a signature of PDR?
- Is there an experimental signature for it?

# Using the Surrogate Reaction Method (SRM) to infer ${}^A\text{X}(n,\gamma){}^{A+1}\text{X}$ from ${}^A\text{X}(d,p\gamma){}^{A+1}\text{X}$



Desired reaction: neutron capture on target  $A$

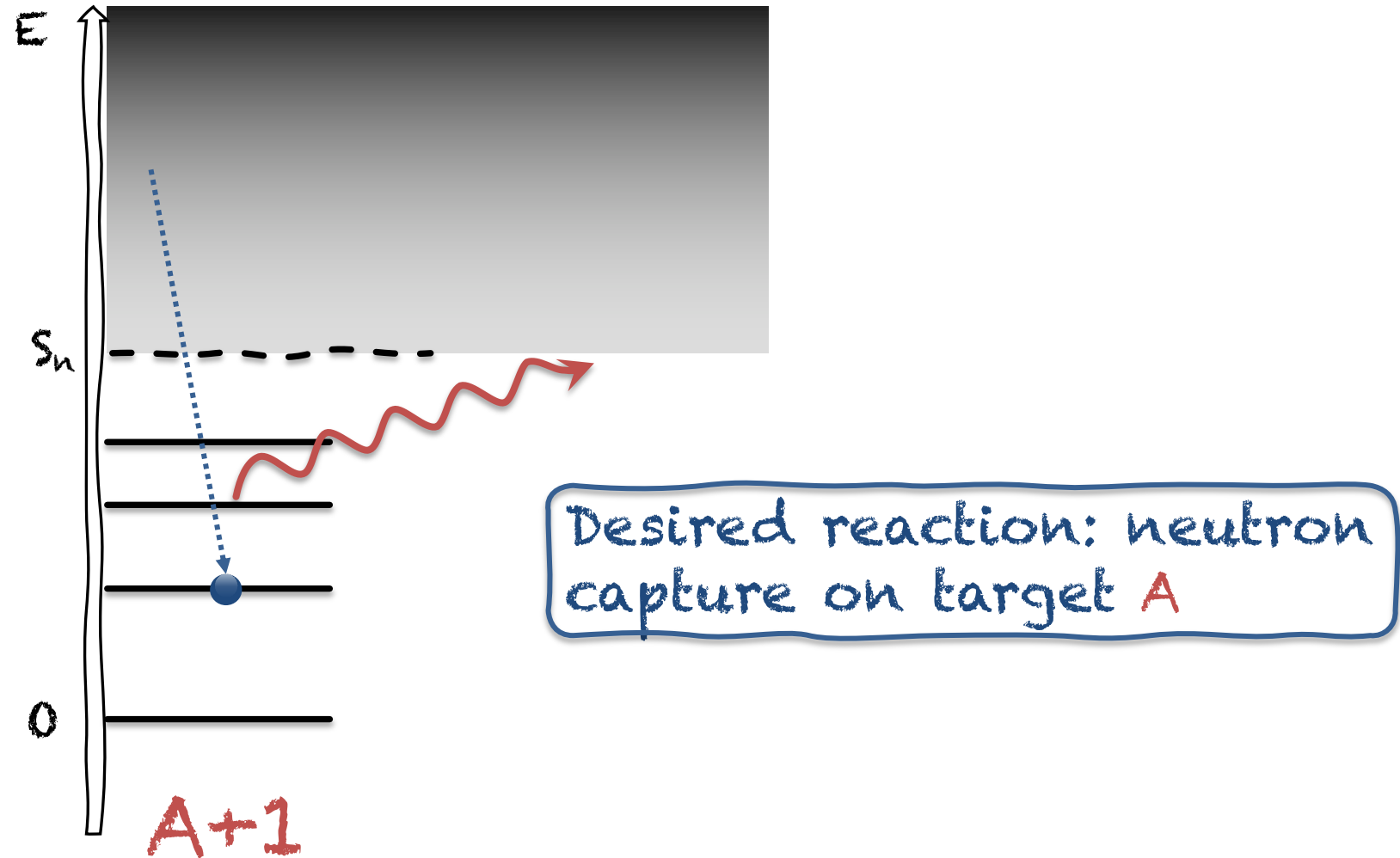
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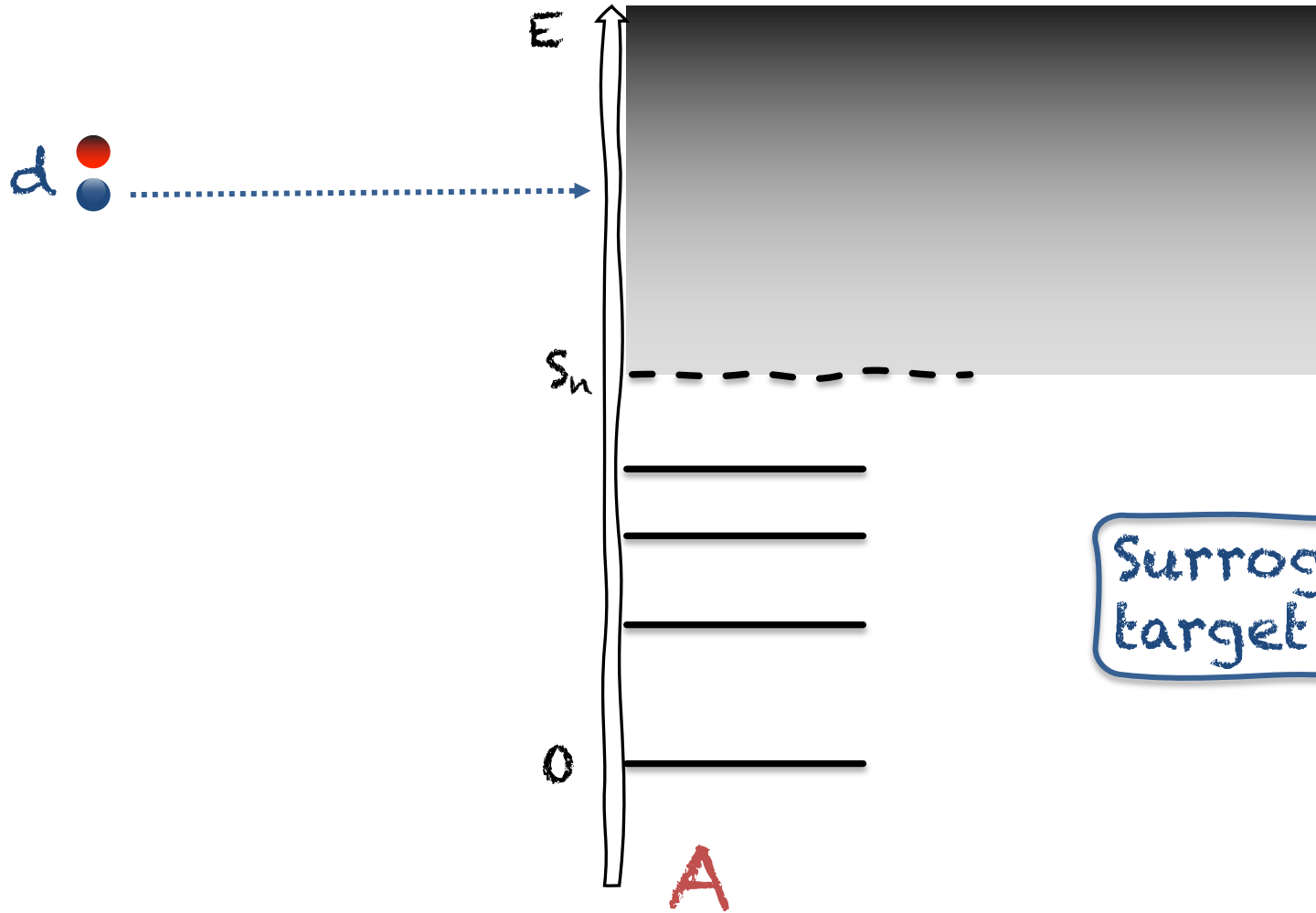
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# Using the Surrogate Reaction Method (SRM) to infer ${}^A\text{X}(n,\gamma){}^{A+1}\text{X}$ from ${}^A\text{X}(d,p\gamma){}^{A+1}\text{X}$

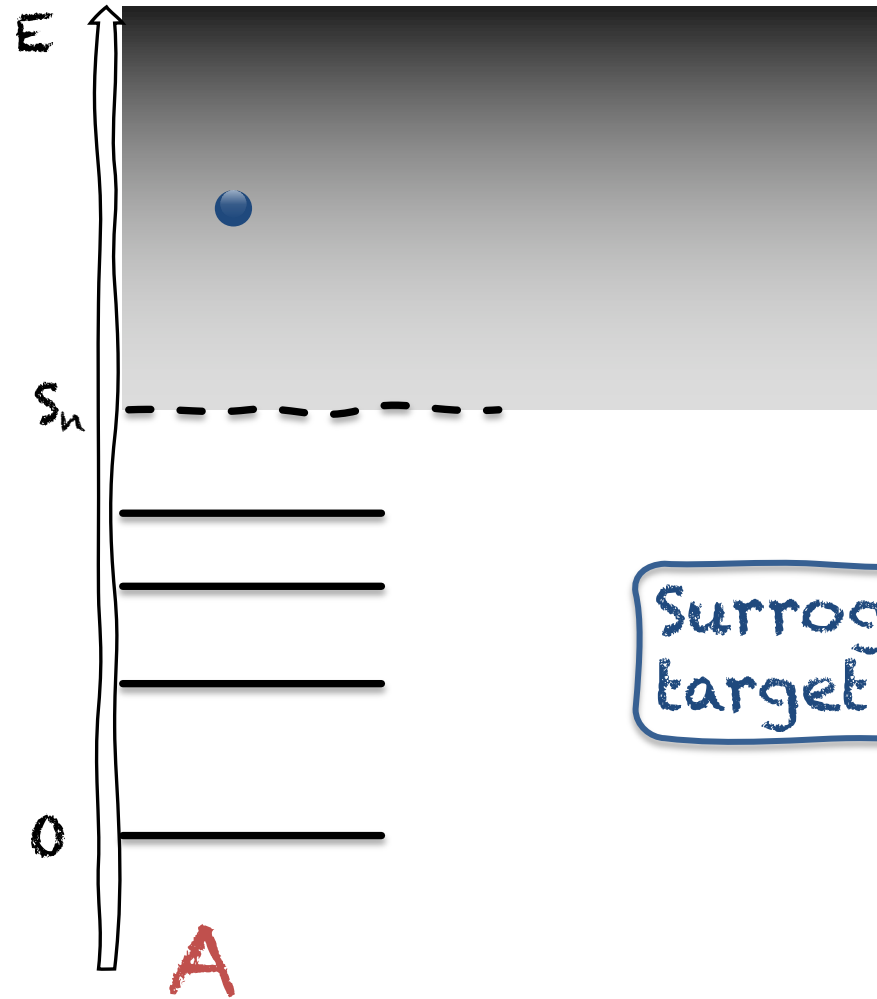
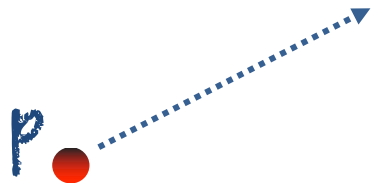


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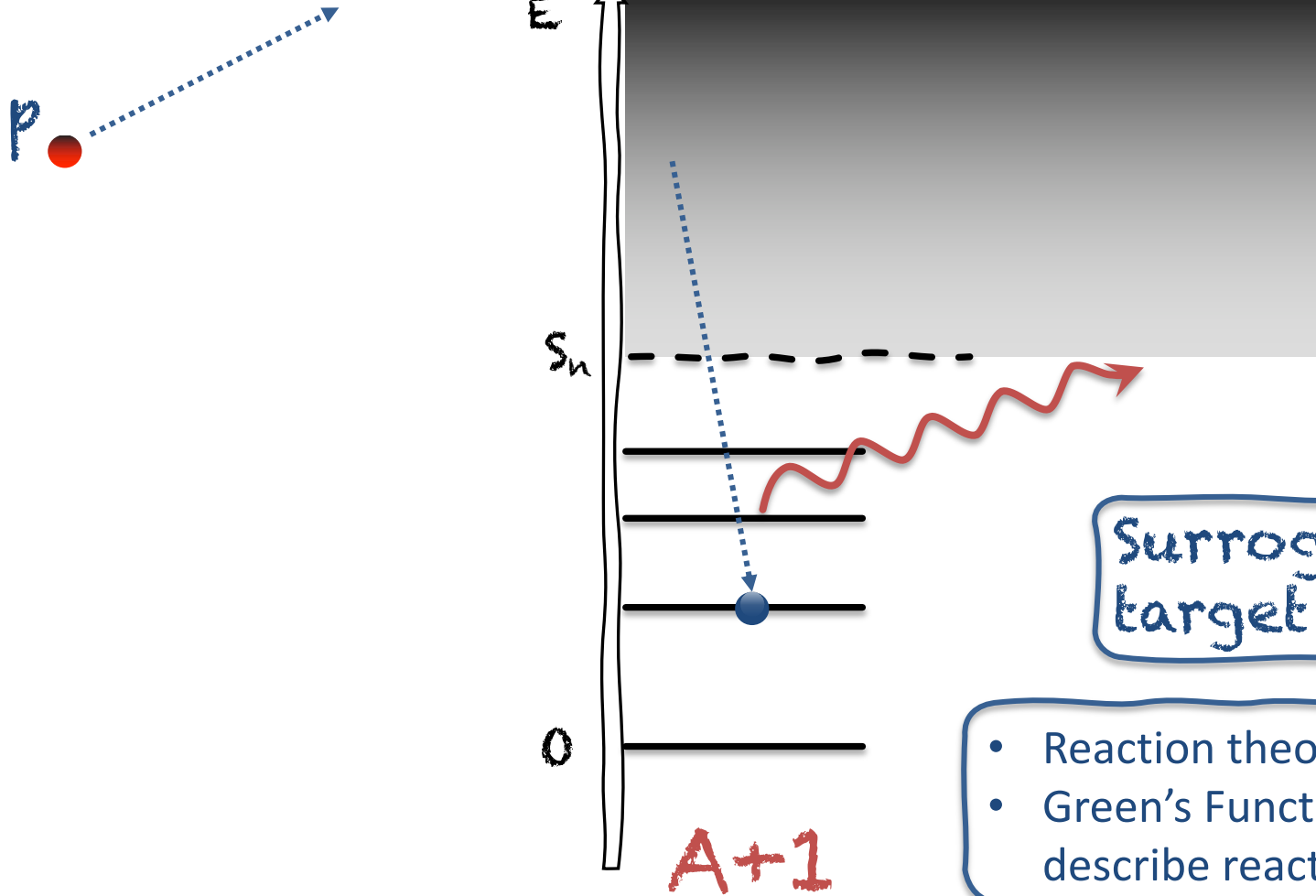
Surrogate:  $(d,p)$  reaction on target  $A$

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Surrogate: (d,p) reaction on target A

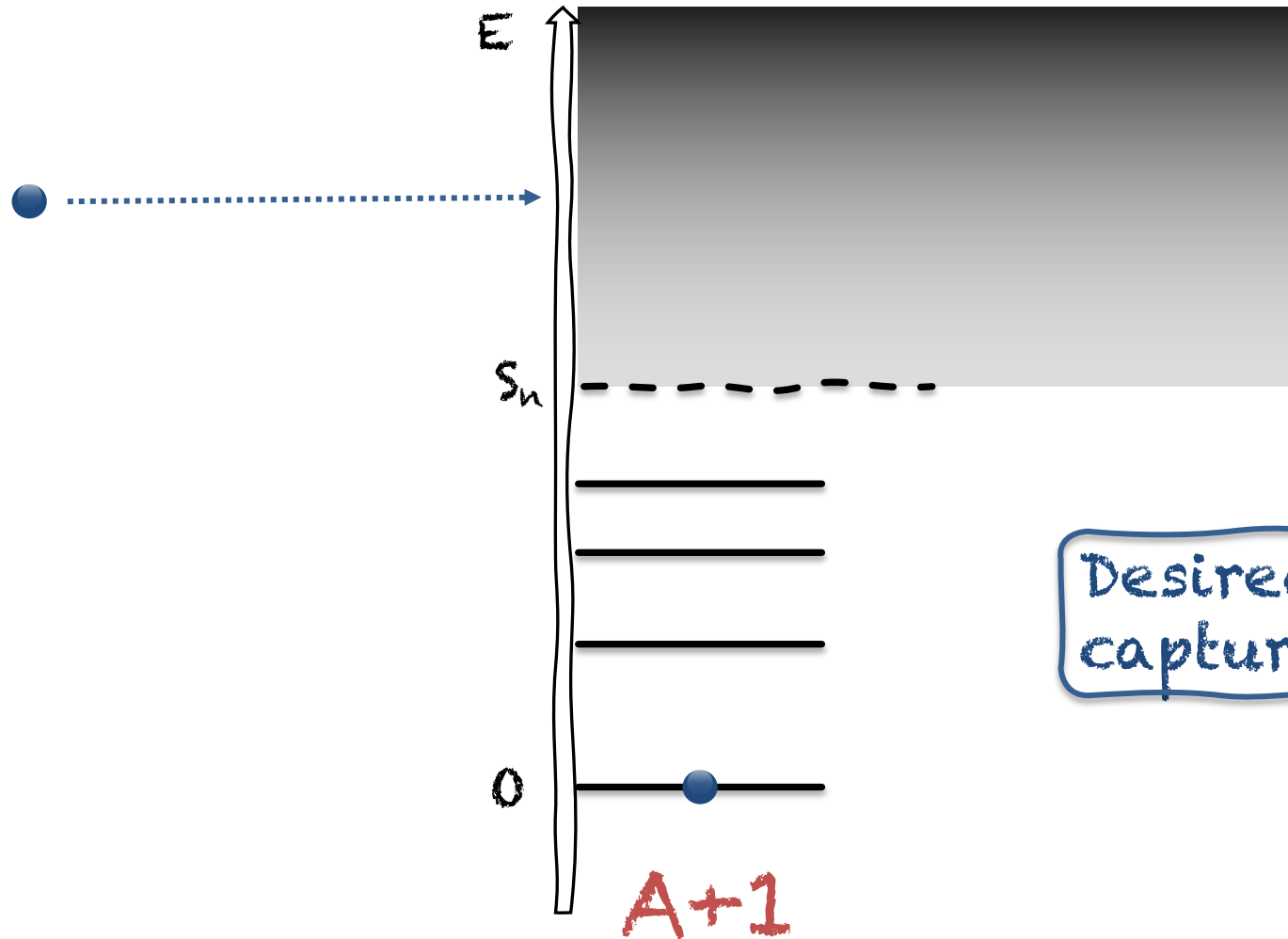
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Surrogate:  $(d,p)$  reaction on target  $A$

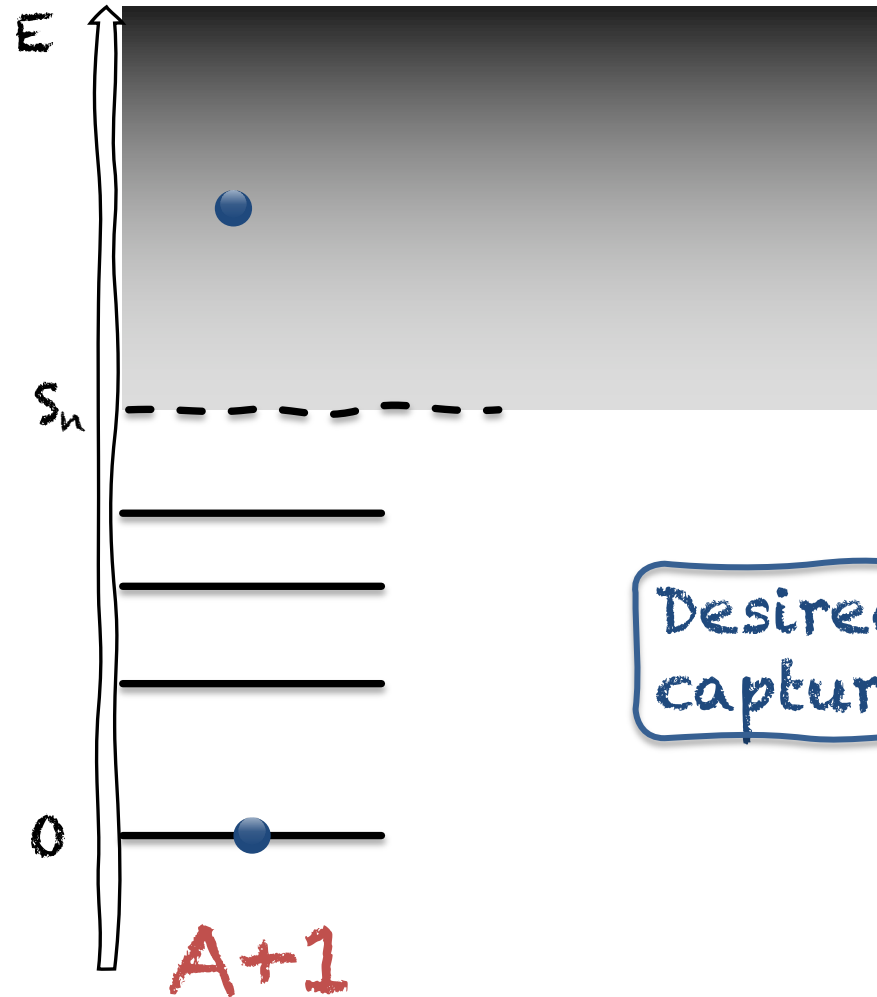
- Reaction theory needed to determine spin distribution
- Green's Function Transfer (GFT) formalism used to describe reaction process

# Using the SRM to infer ${}^{A+1}\text{X}(n,\gamma){}^{A+2}\text{X}$ from ${}^A\text{X}(t,p\gamma){}^{A+2}\text{X}$



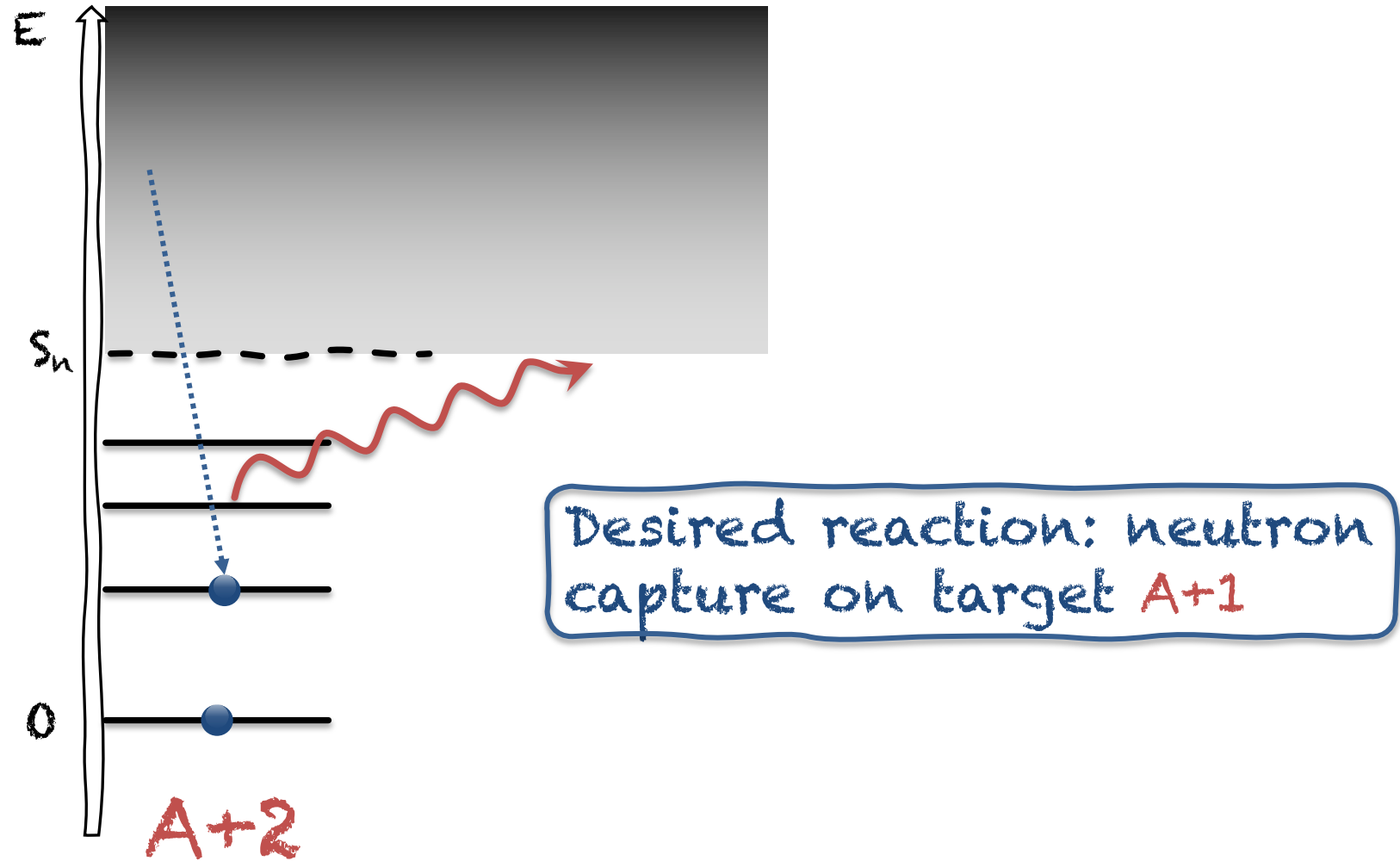
Desired reaction: neutron capture on target  $A+1$

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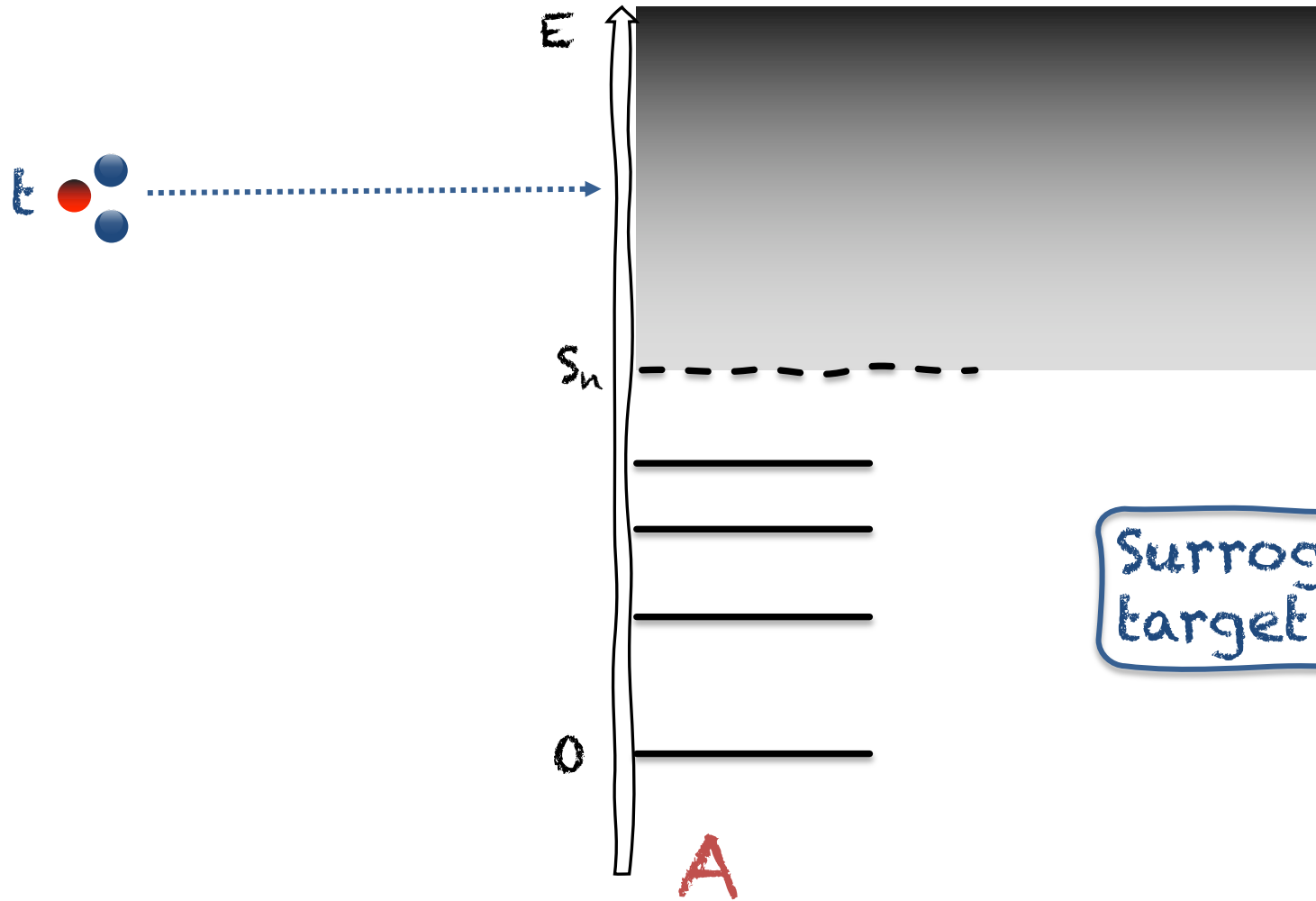


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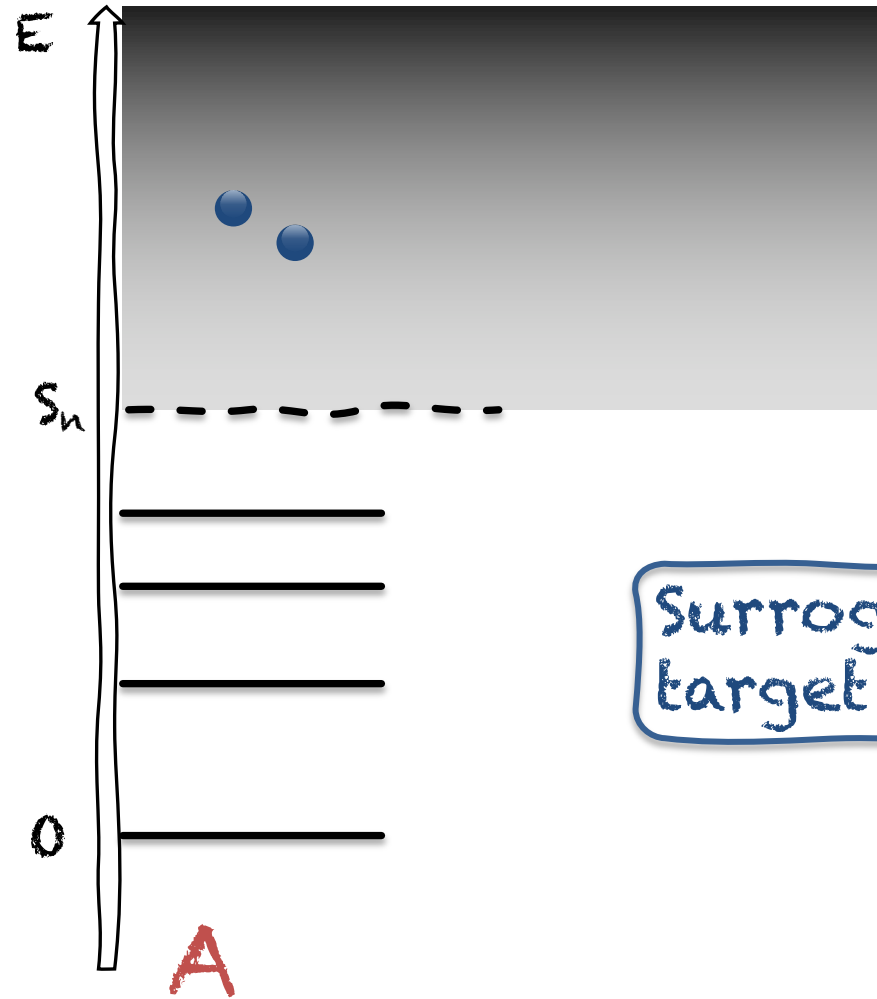
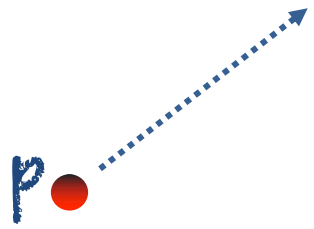
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Surrogate:  $(t,p)$  reaction on target  $A+1$

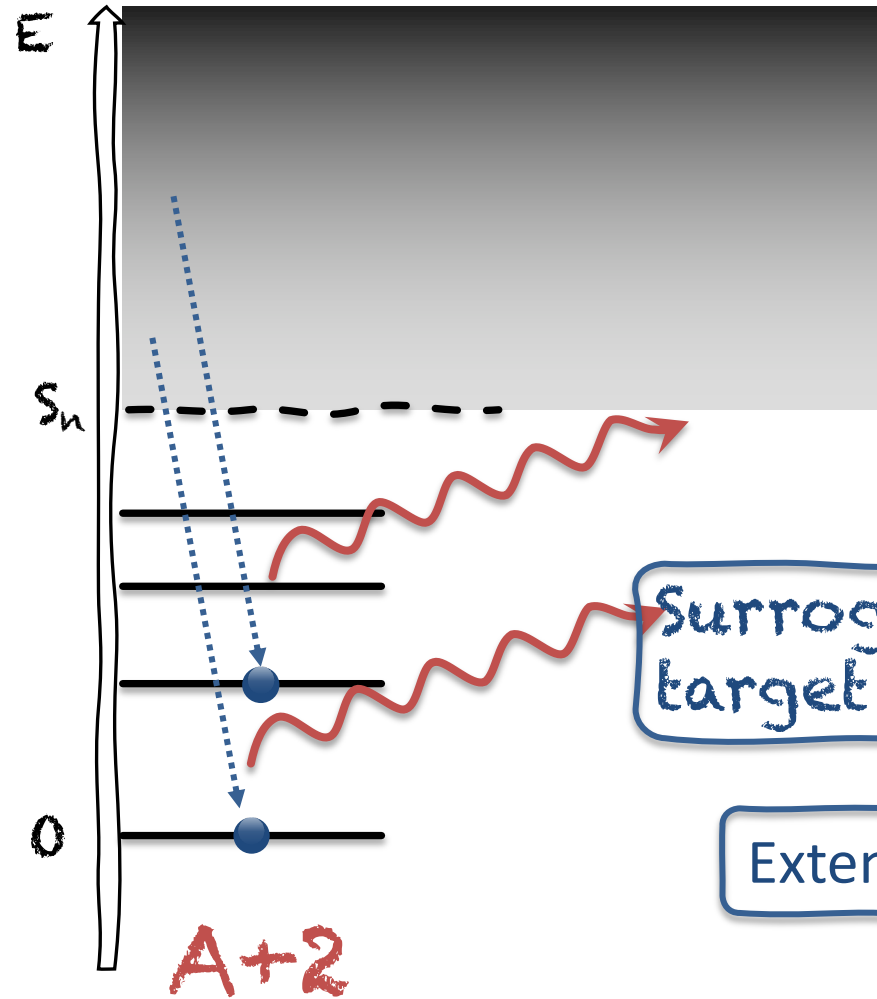
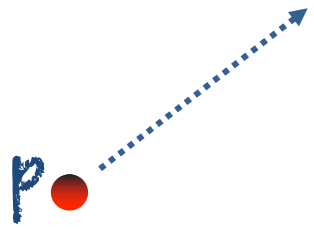


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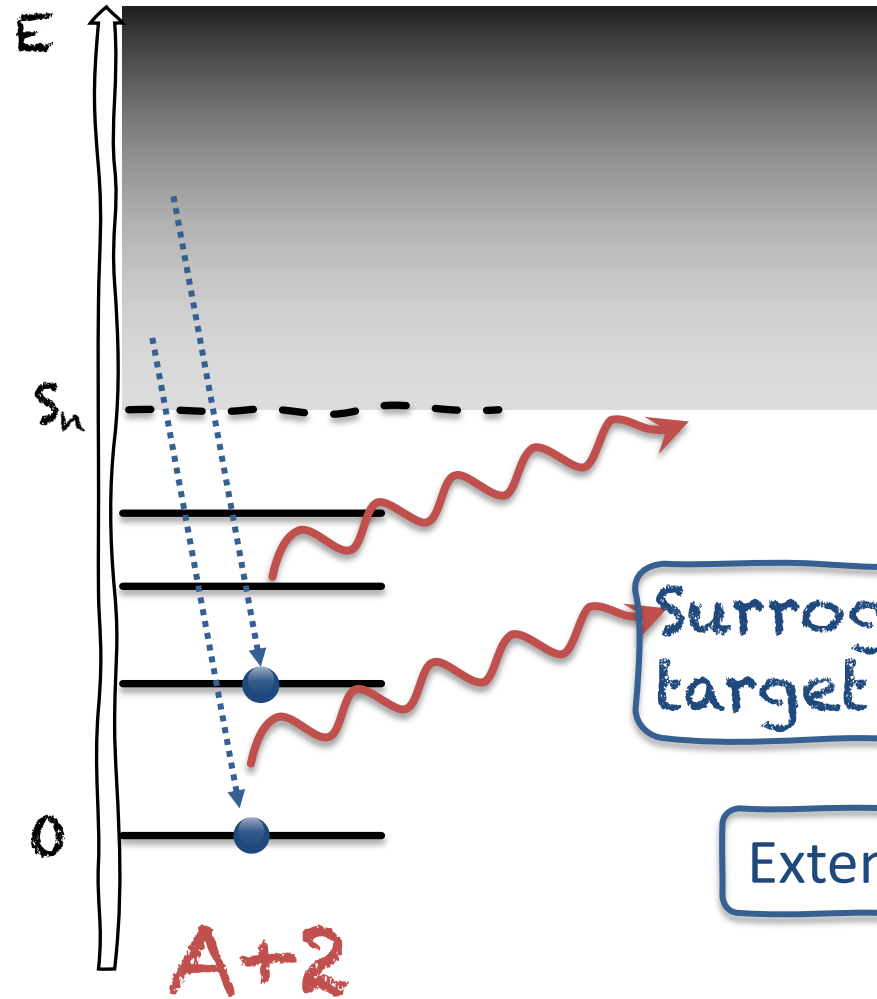
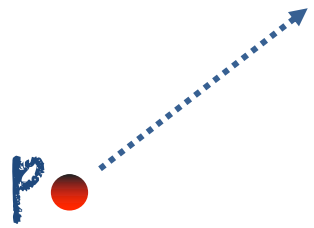
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Surrogate: (t,p) reaction on target  $A+1$  (A. Richards talk)

Extension of GFT to (t,p) reactions

# Using the SRM to infer $^{A+1}X(n,\gamma)^{A+2}X$ from $^AX(t,p\gamma)^{A+2}X$

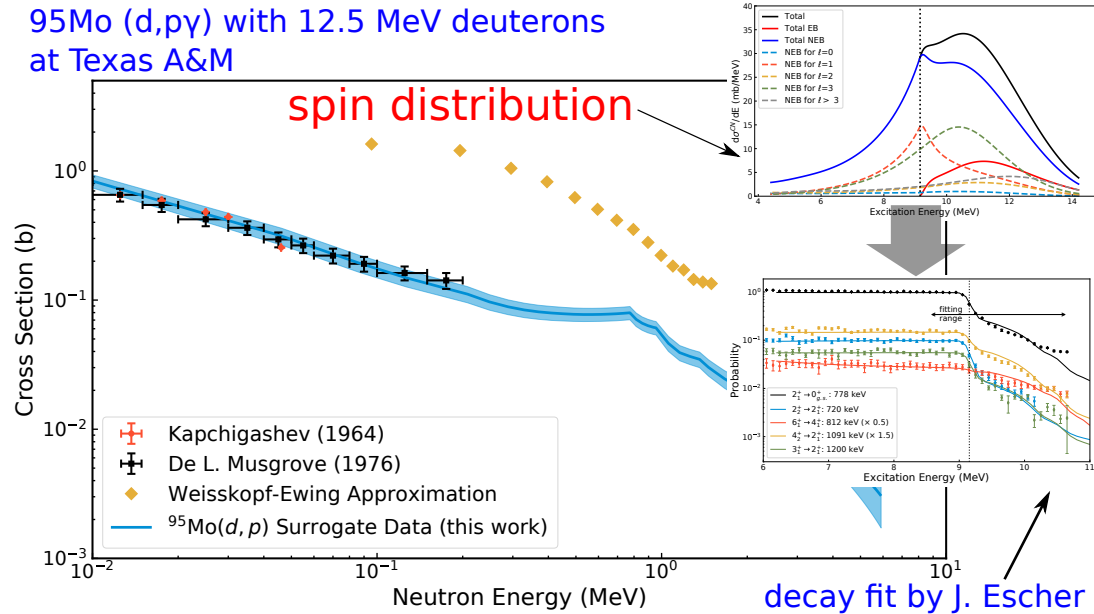


Possible extension to (t,pf)  
(talks by Devlin and Bulgac)

Surrogate: (t,p) reaction on target A+1

Extension of GFT to (t,p) reactions

# An opportunity to thoroughly benchmark the SRM with $^{95}\text{Mo}(n,\gamma)$

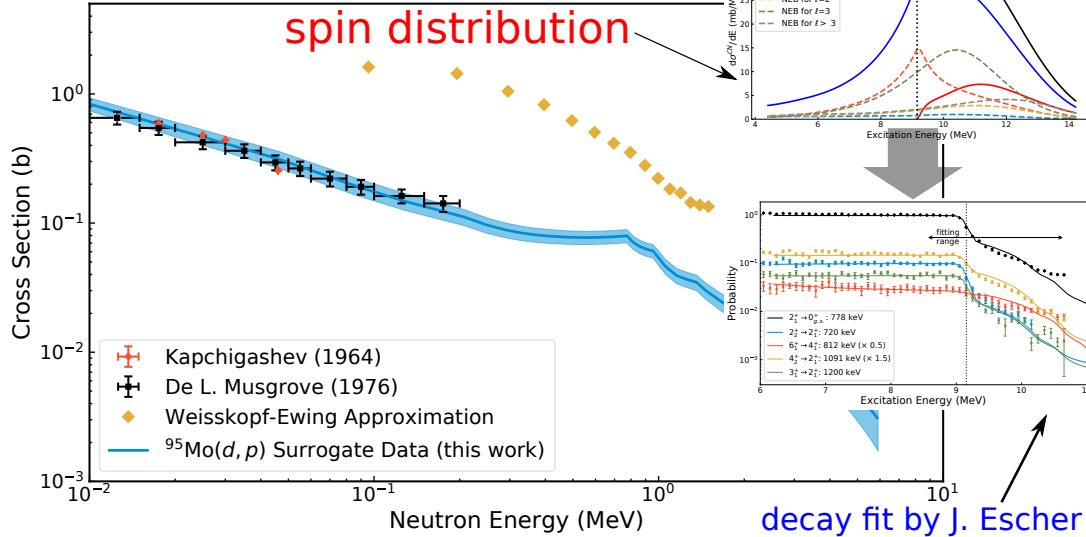


Ratkiewicz, Cizewski, Escher, GP, et al. Phys. Rev. Lett. 122052502 (2019)

- Excellent agreement with  $(n,\gamma)$  data.
- The fitted Hauser-Feshbach decay is used to infer  $(n,\gamma)$  rates.
- No previous knowledge of  $D_0$ , and/or  $\langle \Gamma_\gamma \rangle$  is needed.
- No need for separate determination of NLD and  $\gamma\text{SF}$ .

# An opportunity to thoroughly benchmark the SRM with $^{95}\text{Mo}(n,\gamma)$

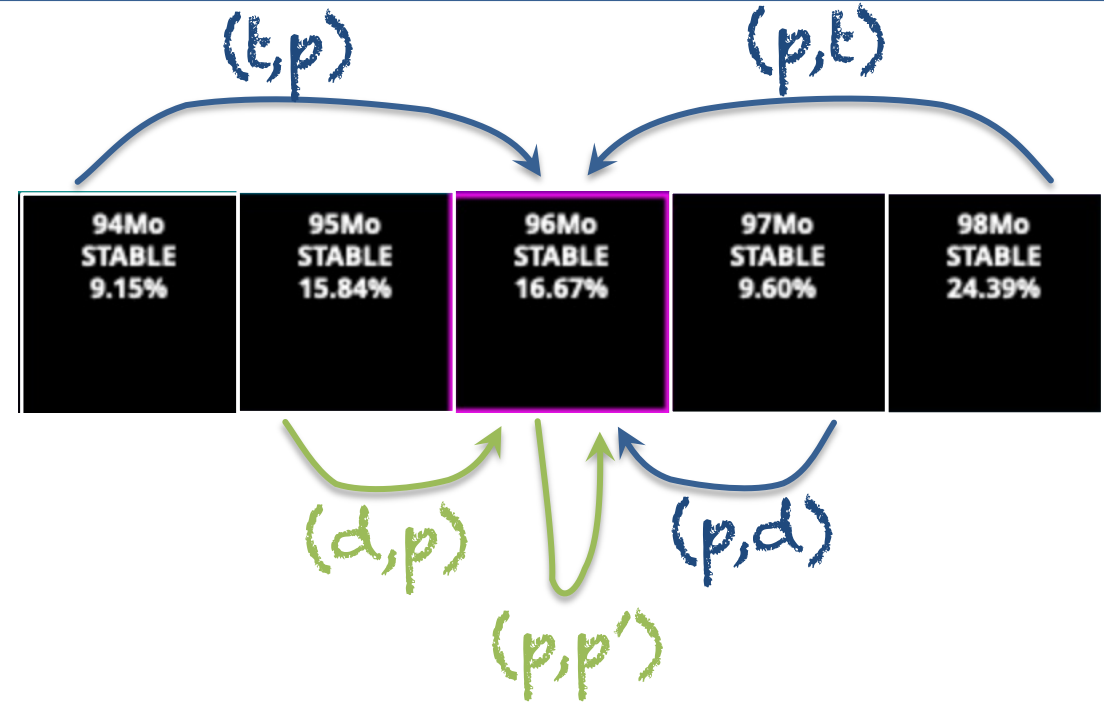
$^{95}\text{Mo}(d,p\gamma)$  with 12.5 MeV deuterons at Texas A&M



Ratkiewicz, Cizewski, Escher, GP, et al. Phys. Rev. Lett. 122052502 (2019)

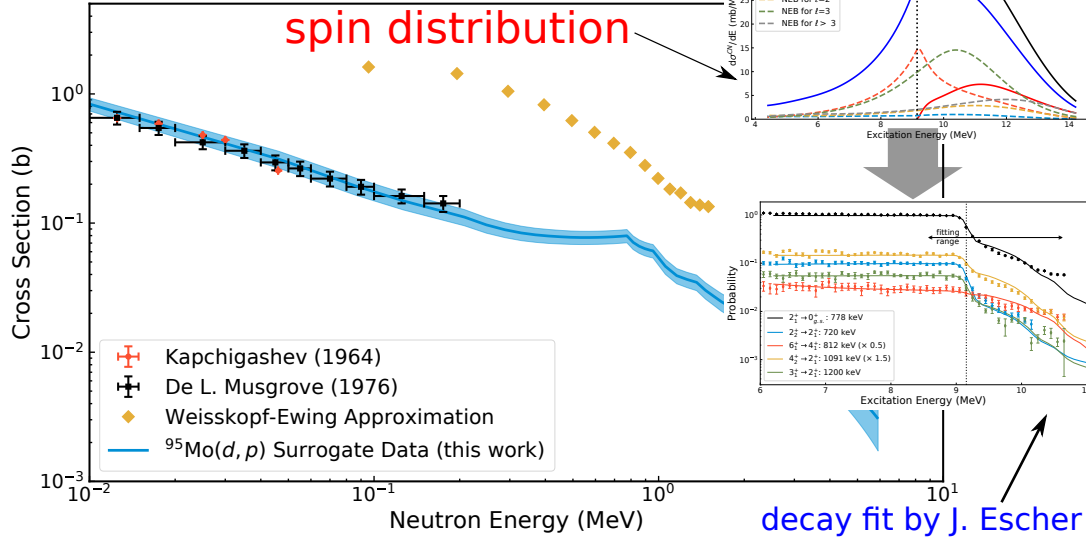
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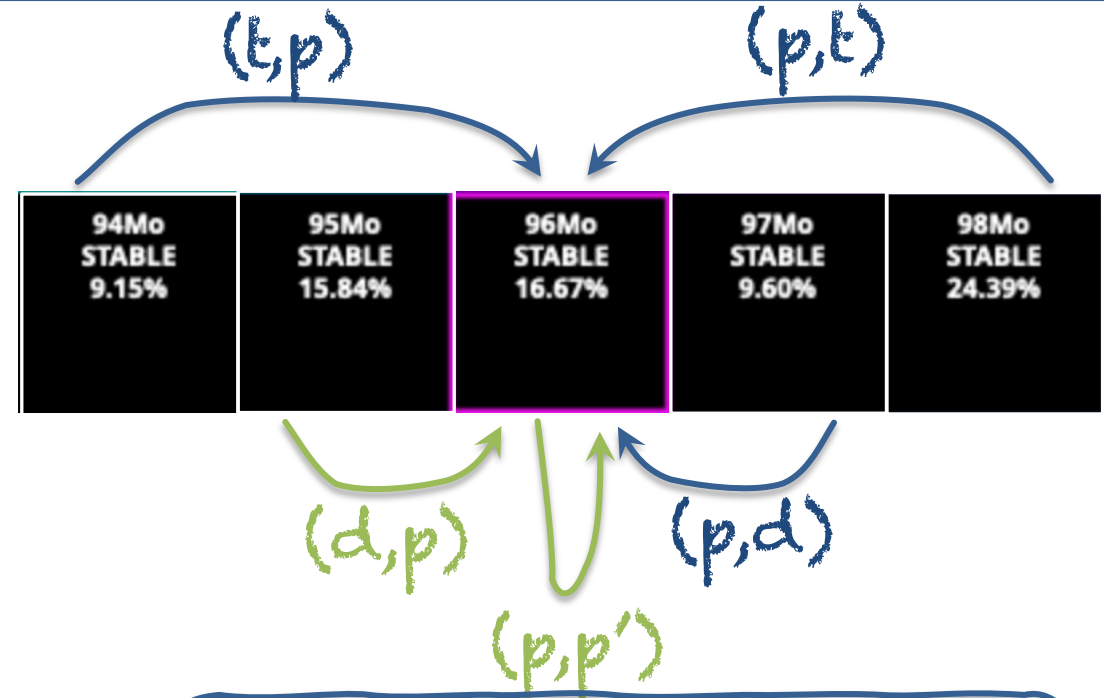
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- $^{94-98}\text{Mo}$  are all stable
- $^{95}\text{Mo}(n,\gamma)$  is known
- $^{95}\text{Mo}(d,p\gamma)$  and  $^{95}\text{Mo}(p,p'\gamma)$  have been measured
- Opportunity to benchmark many SRM techniques (A. McIntosh talk)

# International School of Physics “Enrico Fermi”



Deadline for applications:  
April 10

## COURSE 213 - NUCLEAR STRUCTURE AND REACTIONS FROM A BROAD PERSPECTIVE

27 June - 2 July 2024

### Directors

Francisco Barranco - University of Seville (Spain)

Enrico Vigezzi - INFN Milano (Italy)

### Scientific Secretary

Gregory Potel - Lawrence Livermore National Laboratory (USA)

*This School is dedicated to the memory of Ricardo A. Broglia.*

[https://www.sif.it/corsi/scuola\\_fermi/2024/213](https://www.sif.it/corsi/scuola_fermi/2024/213)



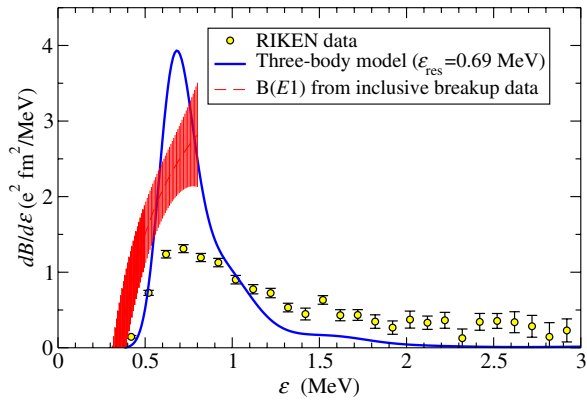
© Daniele Marucci - tremezzina.co

Thank you for your attention!

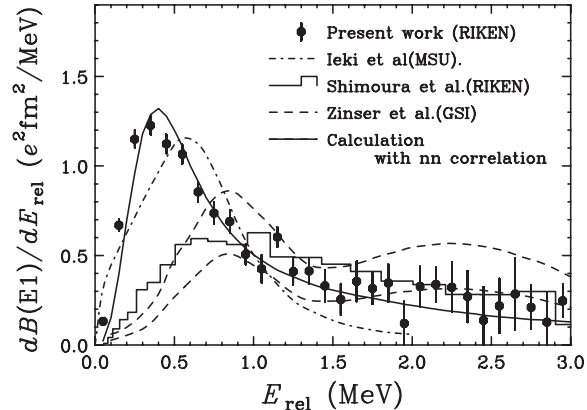


# Is there a pygmy resonance in $^{11}\text{Li}$ ? What's its structure?

## Coulomb breakup

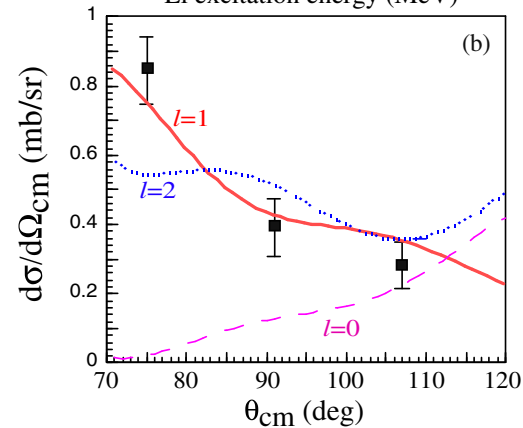
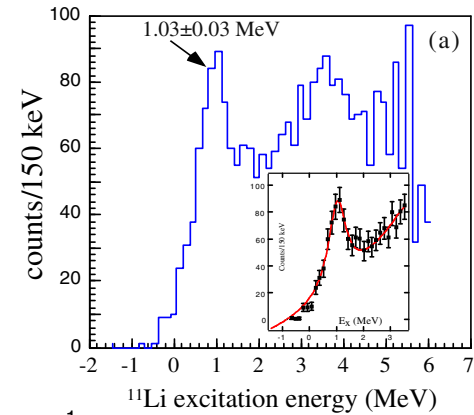


Fernández *et al.* PRL **110**, 142701 (2013)



Nakamura *et al.* PRL **96**, 252502 (2006)

## (d,d')

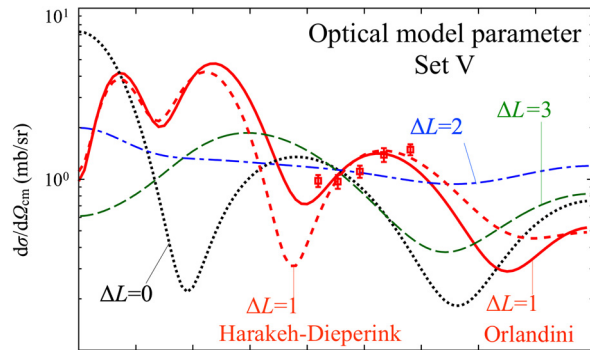
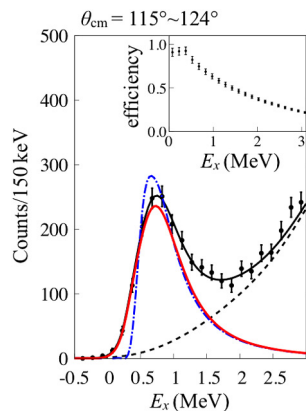


Kanungo *et al.* PRL **114**, 192502 (2015)

some questions to address:

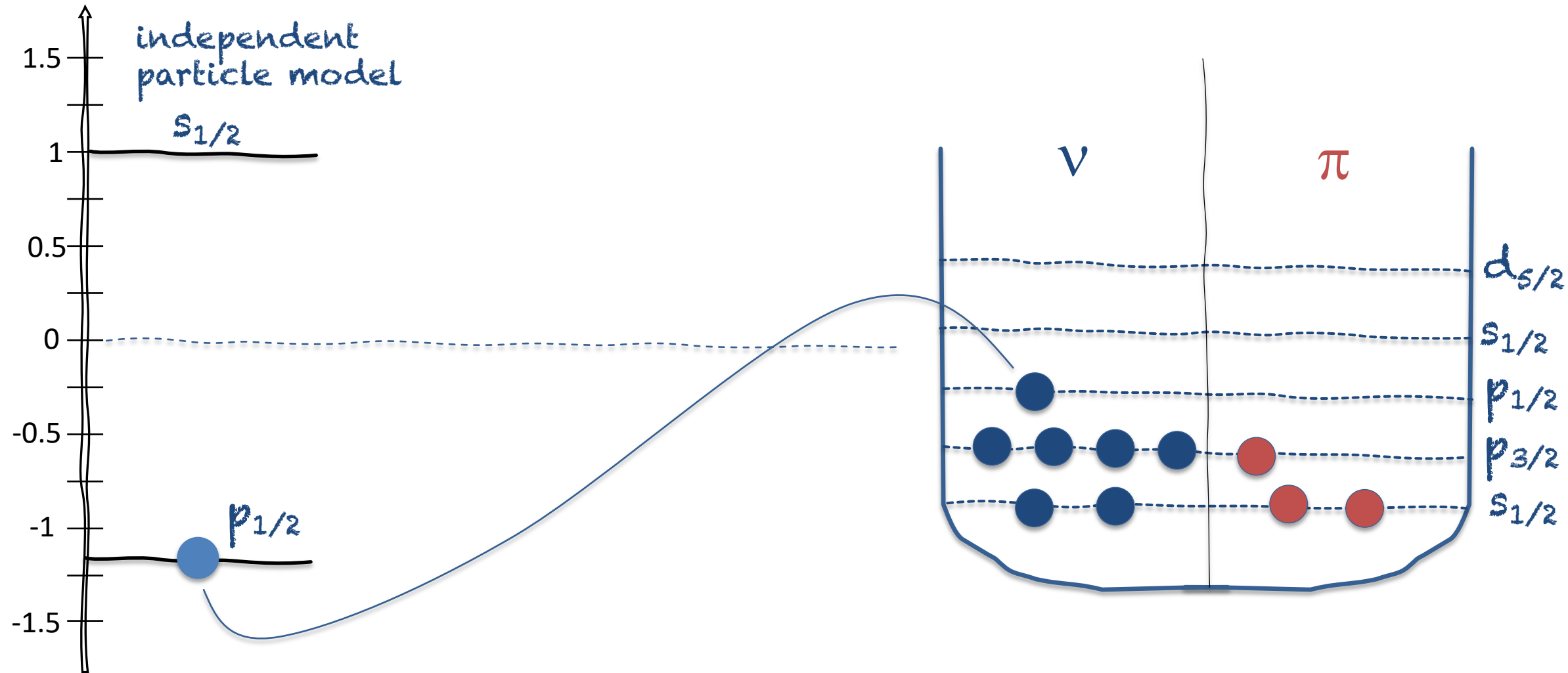
- How do we characterize the PDR?
- Is it distinct from the GDR?
- How does it compare with theory?

## (p,p')

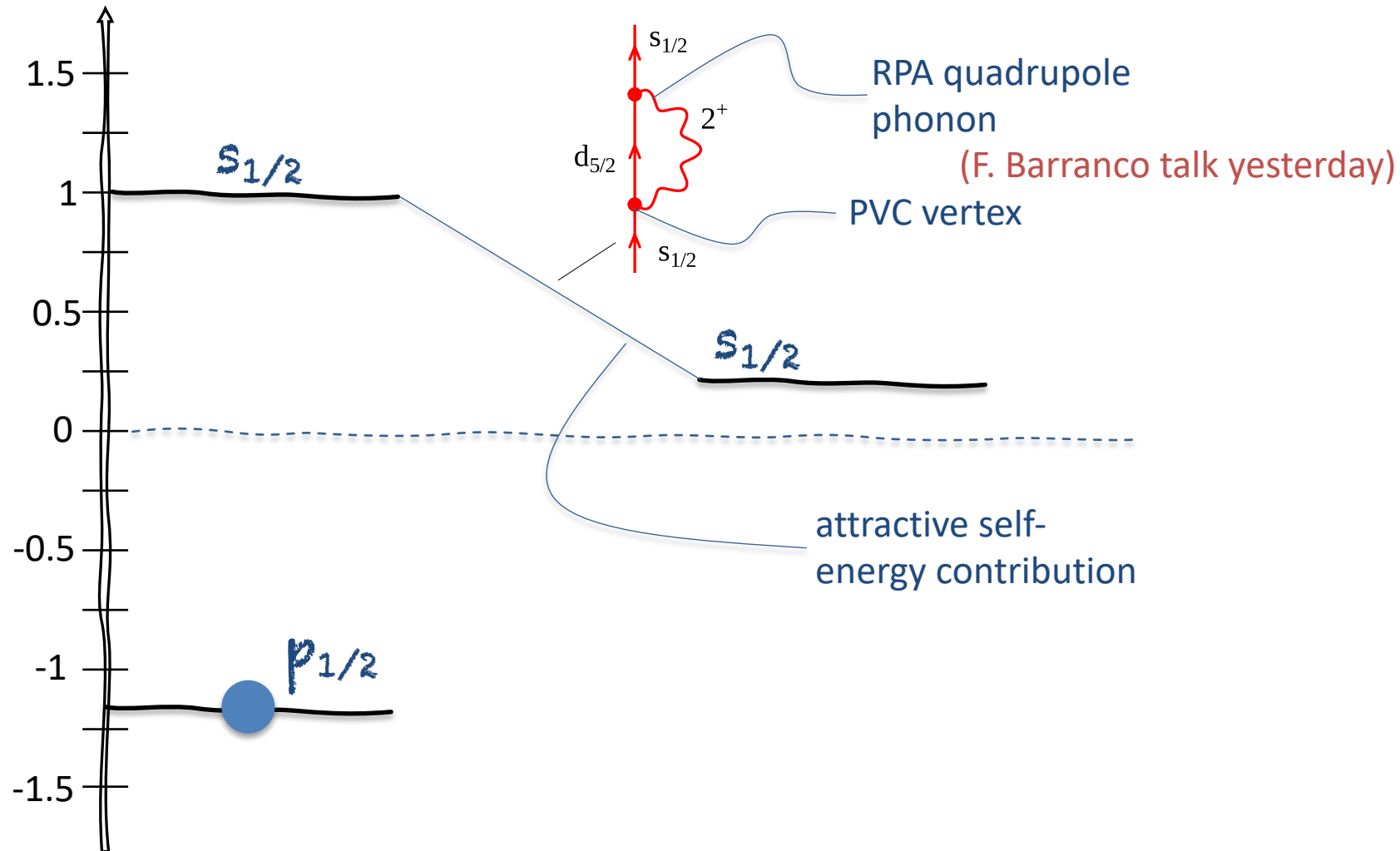


J. Tanaka *et al.* / Physics Letters B 774 (2017) 268–272

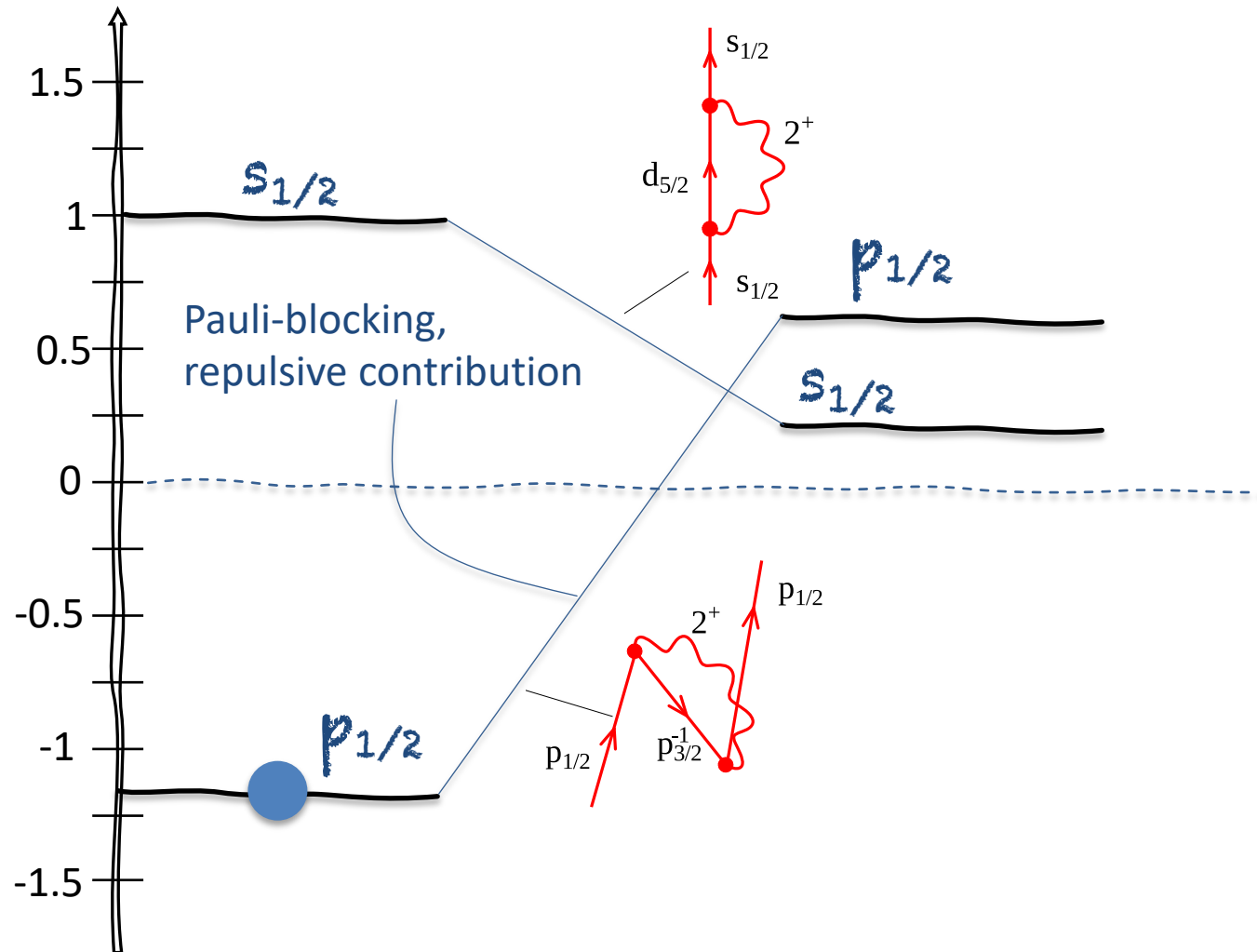
# Structure of $^{10}\text{Li}$ in nuclear field theory (NFT): the precursor of $^{11}\text{Li}$



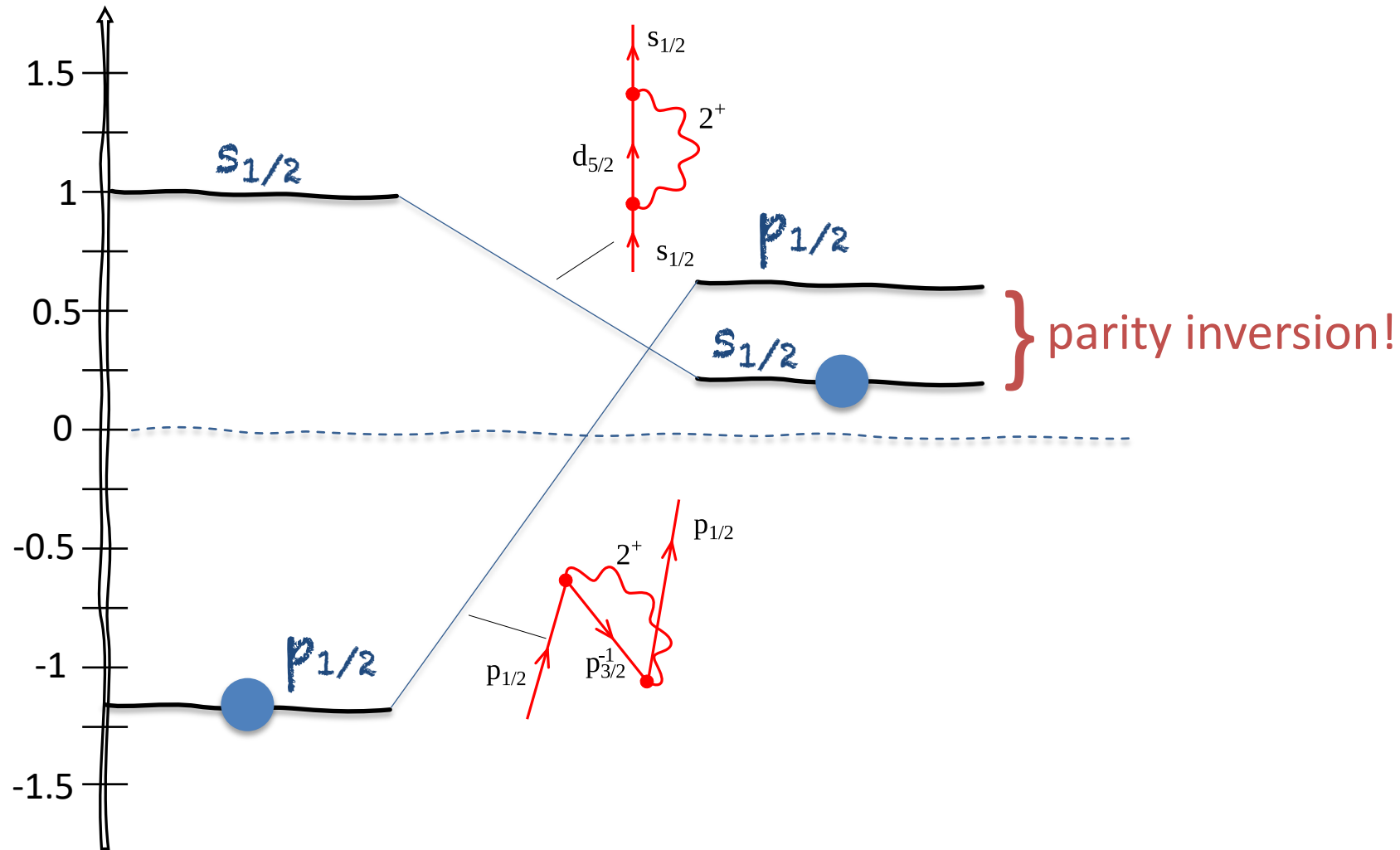
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Is the PDR a *bona fide* collective mode, distinct from GDR?

multi-messenger approach  
in order to characterize PDR

↓

standard probes:  $(\alpha, \alpha')$ ,  $(p, p')$   
 $(\gamma, \gamma')$

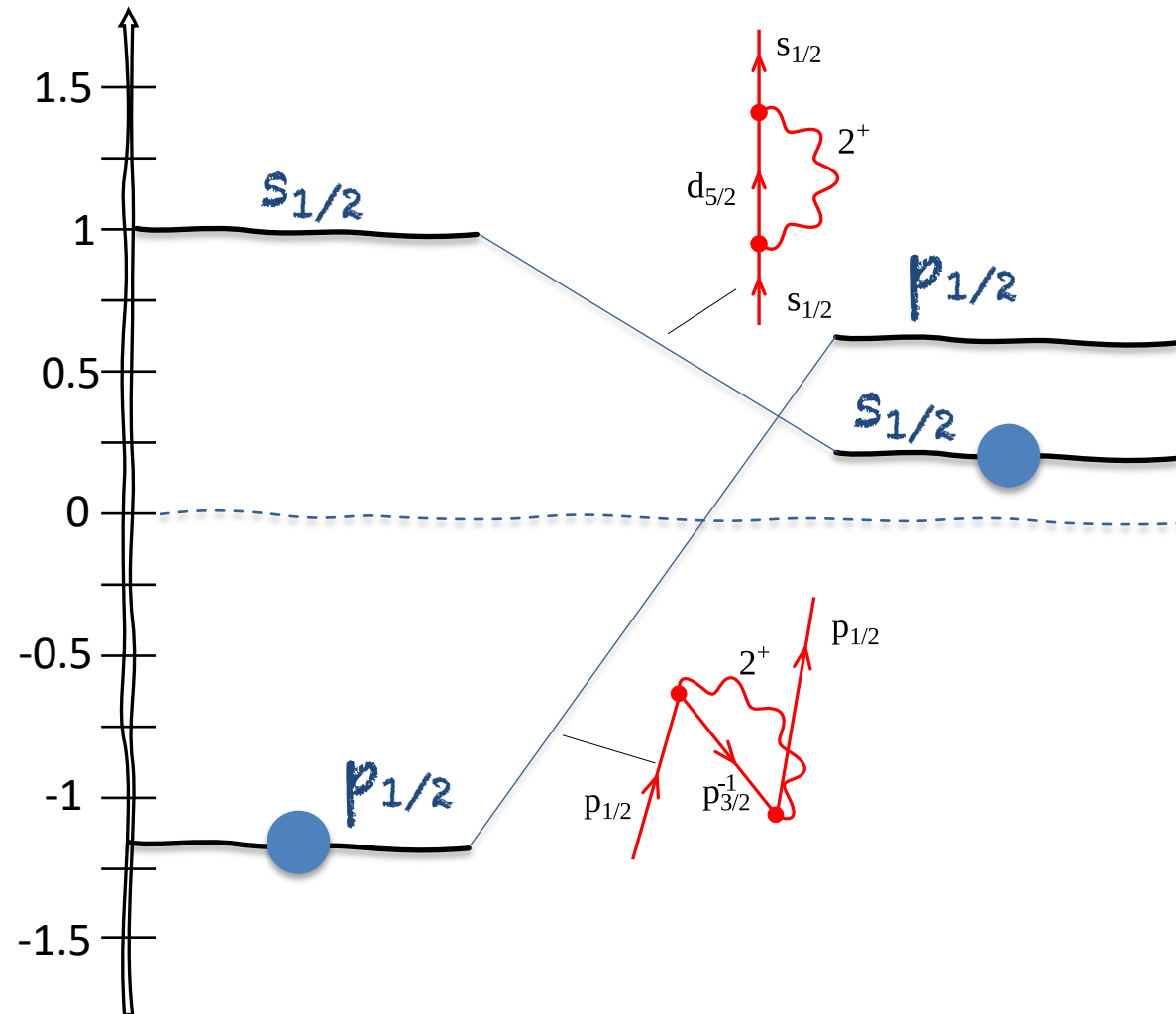
N. Nakatsuka et al.  
Physics Letters B  
**768** (2017) 387

populating the  $^{11}\text{Li}$  PDR  
with  $(t, p)$

Broglia et al. Eur. Phys. J. A  
(2019) **55**: 243

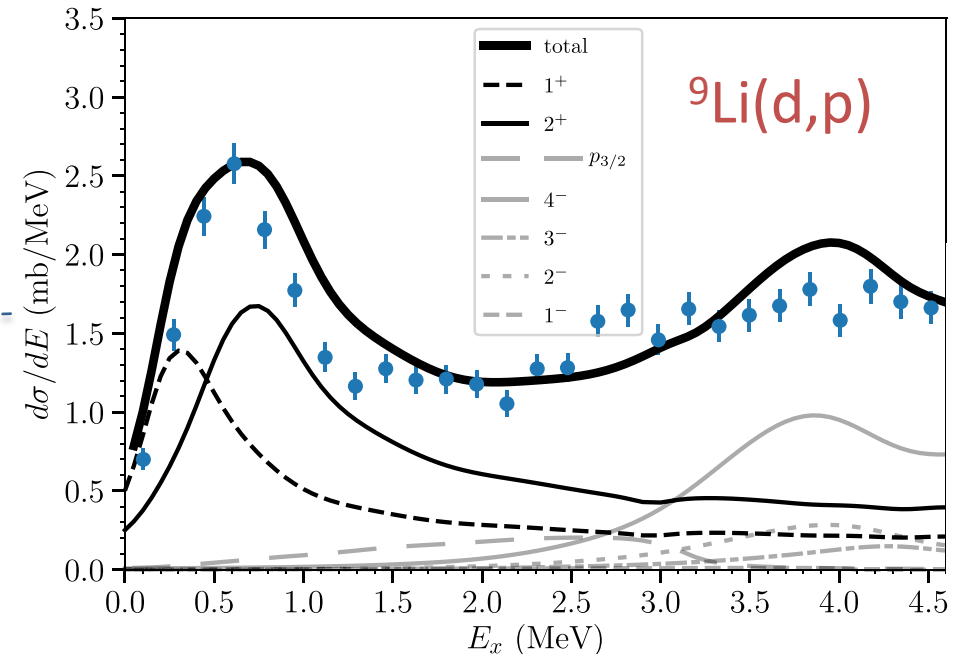
particle-particle correlations might be a distinctive feature of PDRs

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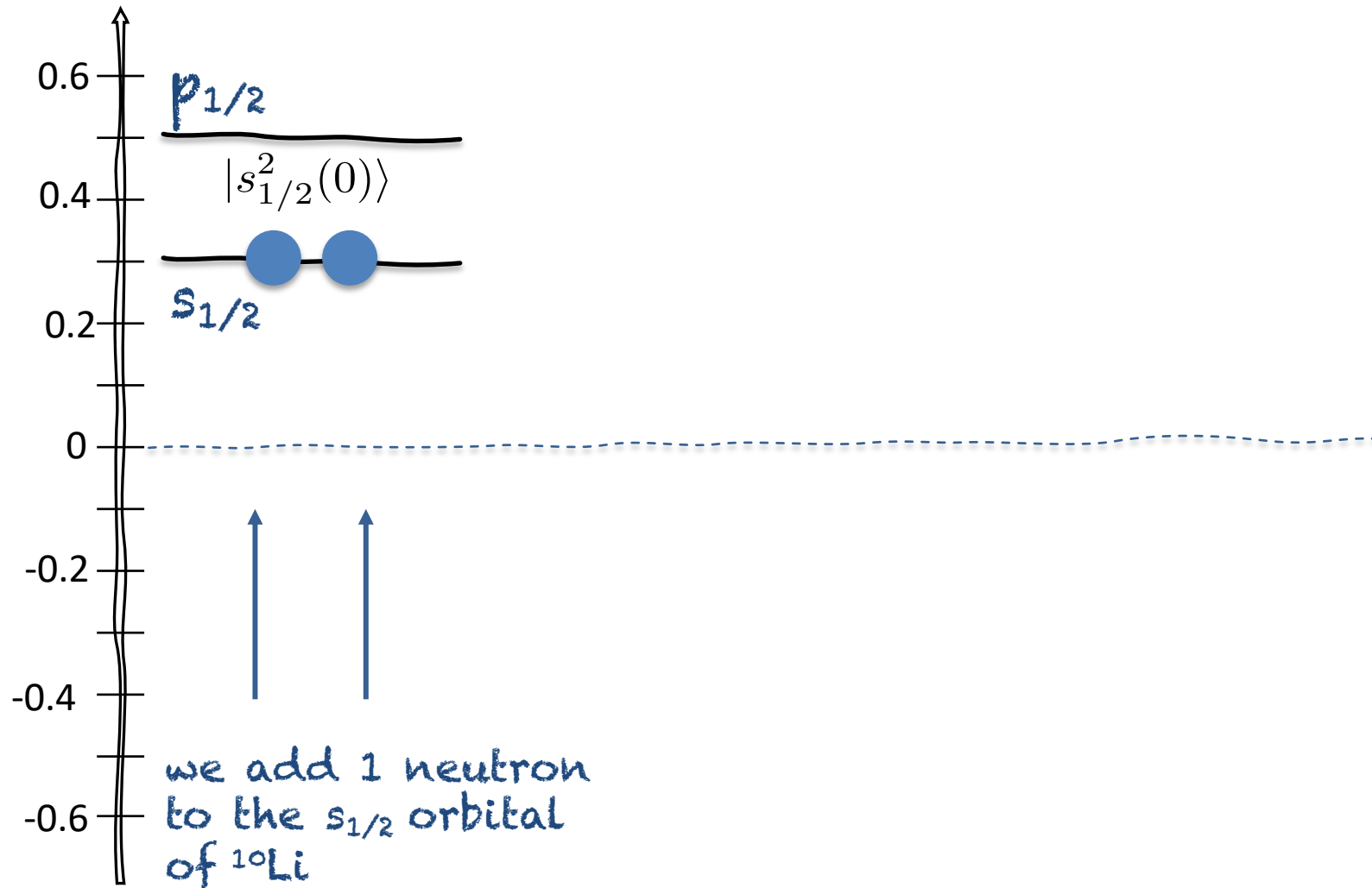
Cavallaro *et al.*, PRL **118**, 012701 (2017)

Barranco, GP, Vigezzi, Broglia PRC **101**, 031305(R) (2020)



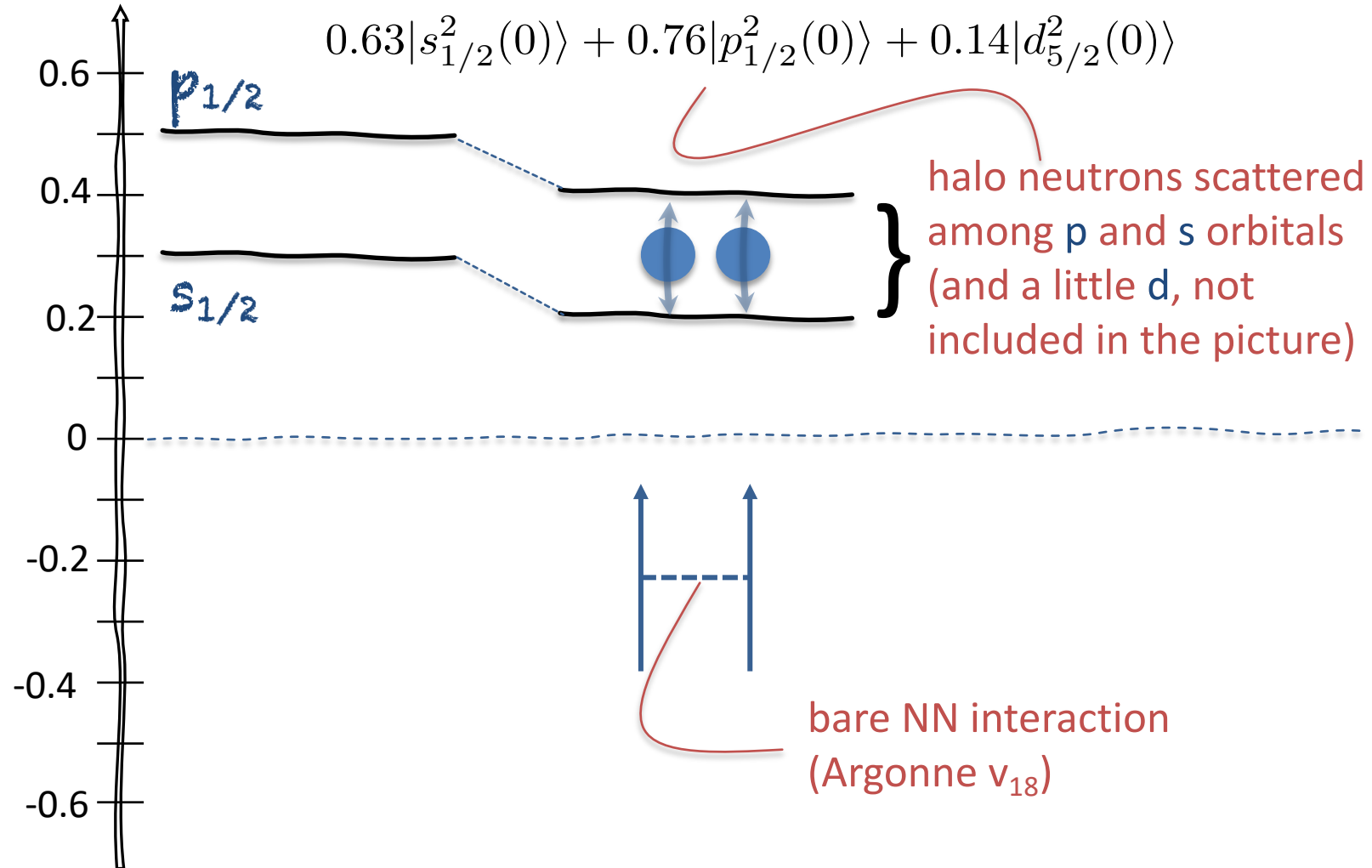
theoretical description validated by experiment

# Nuclear field theory (NFT) highlights the role of the PDR in $^{11}\text{Li}$ structure

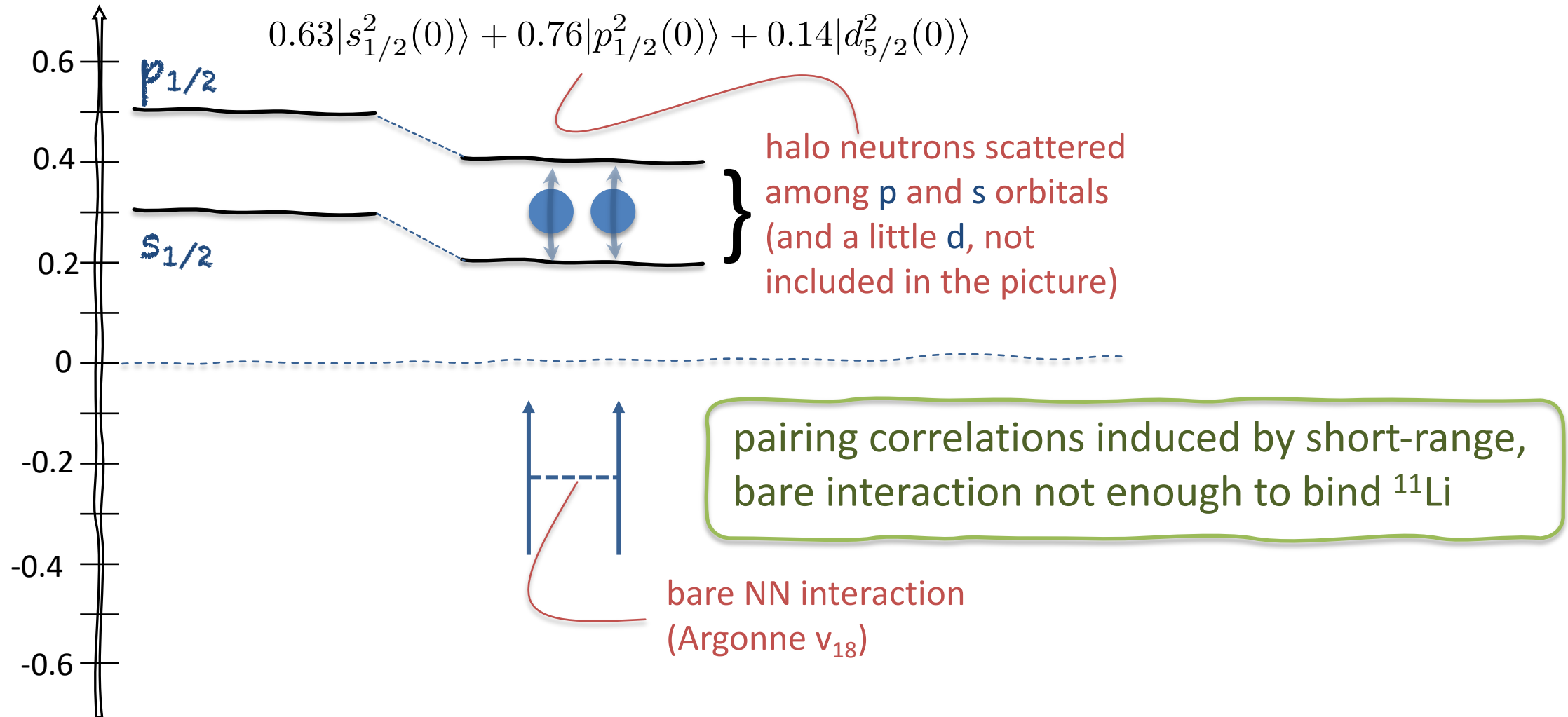




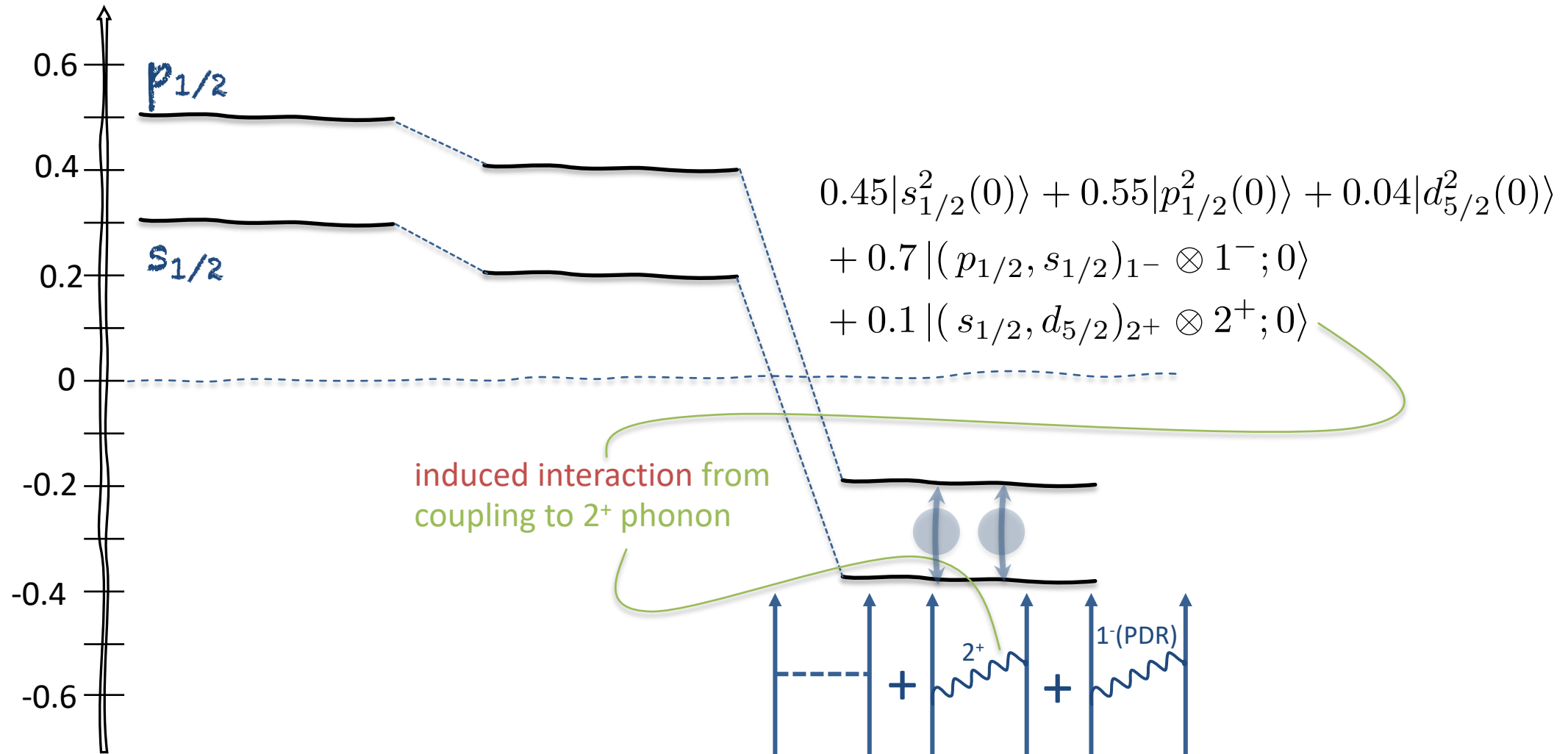
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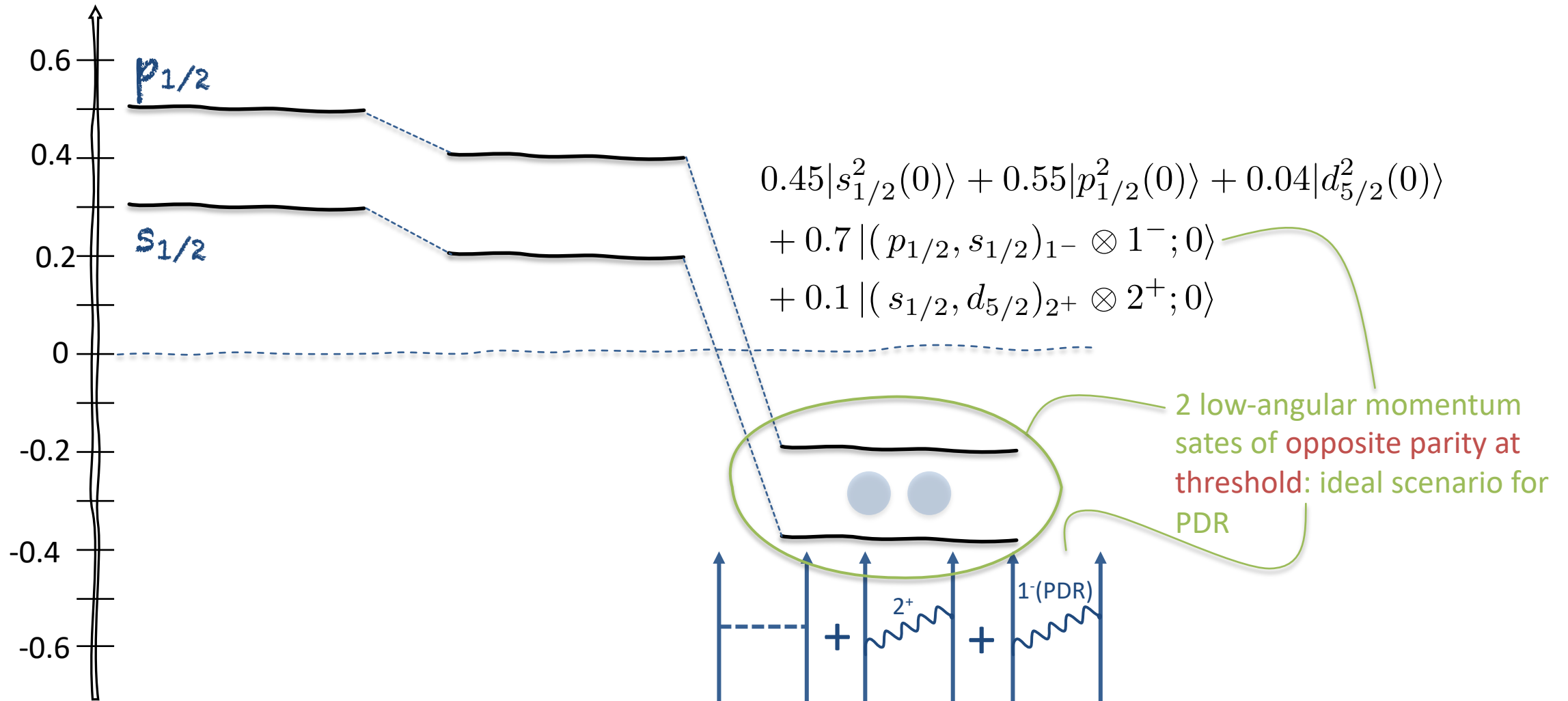
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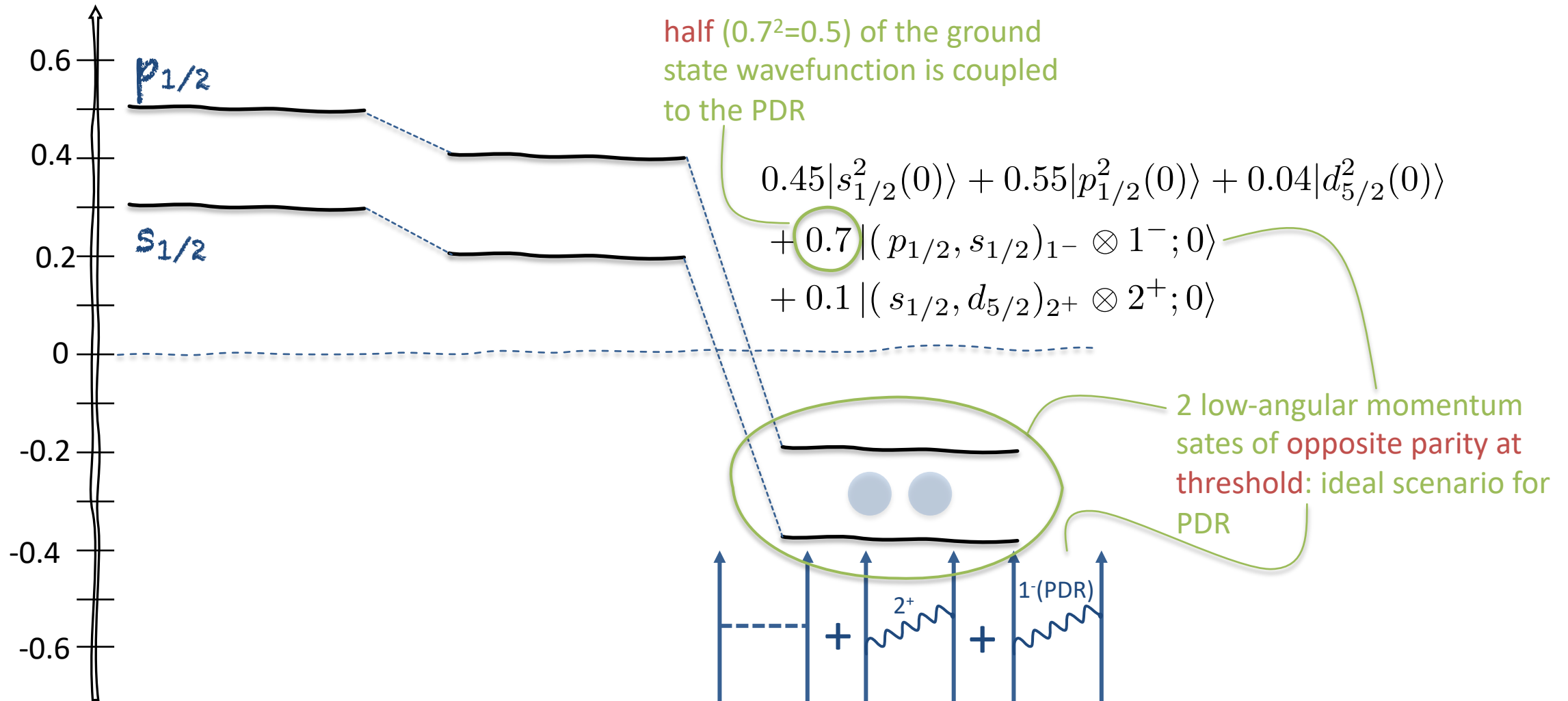
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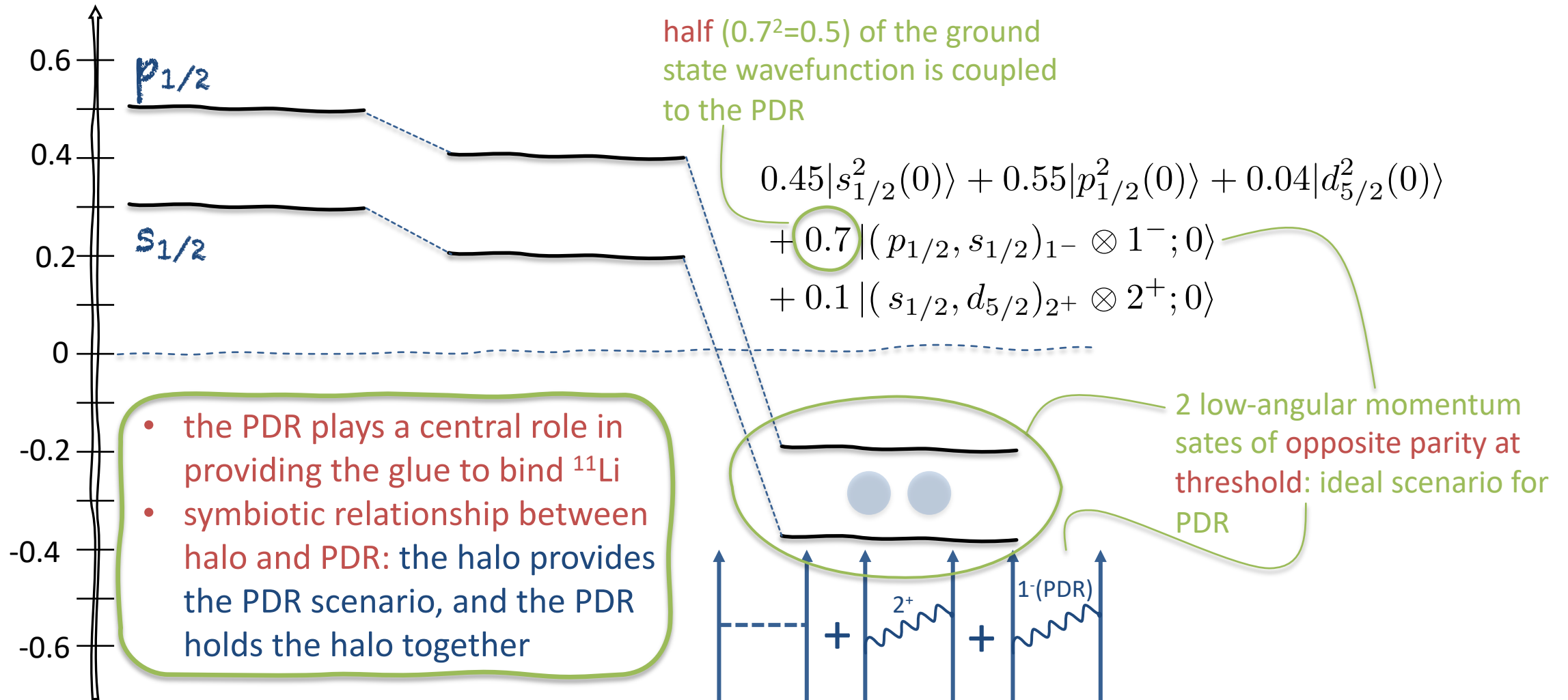
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# theory confirmed by $^{11}\text{Li}(p,t)^9\text{Li}(gs;E_x=2.69 \text{ MeV } 1/2^-)$

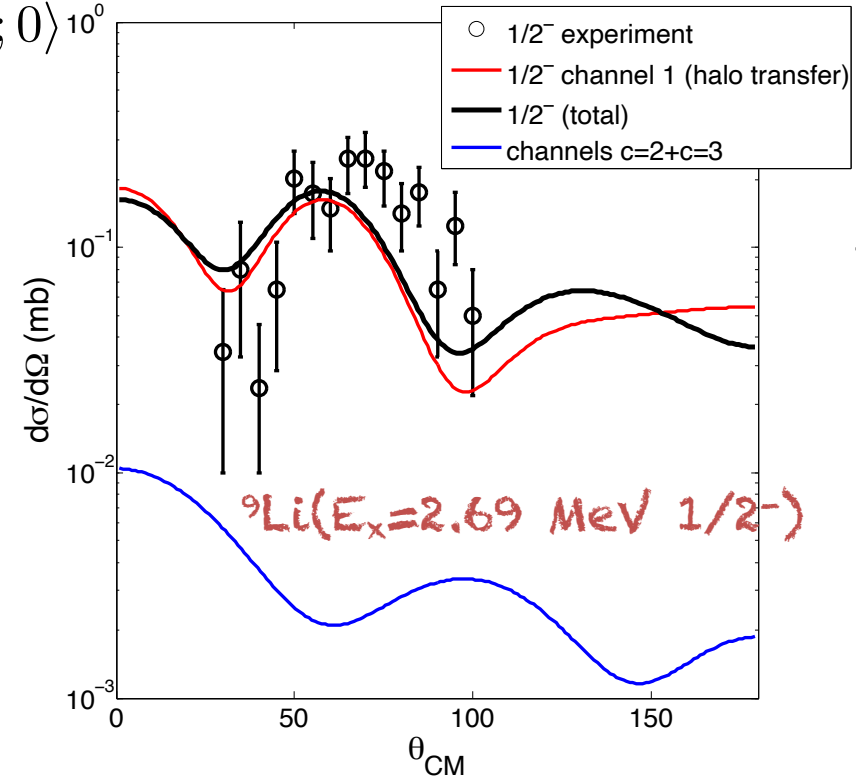
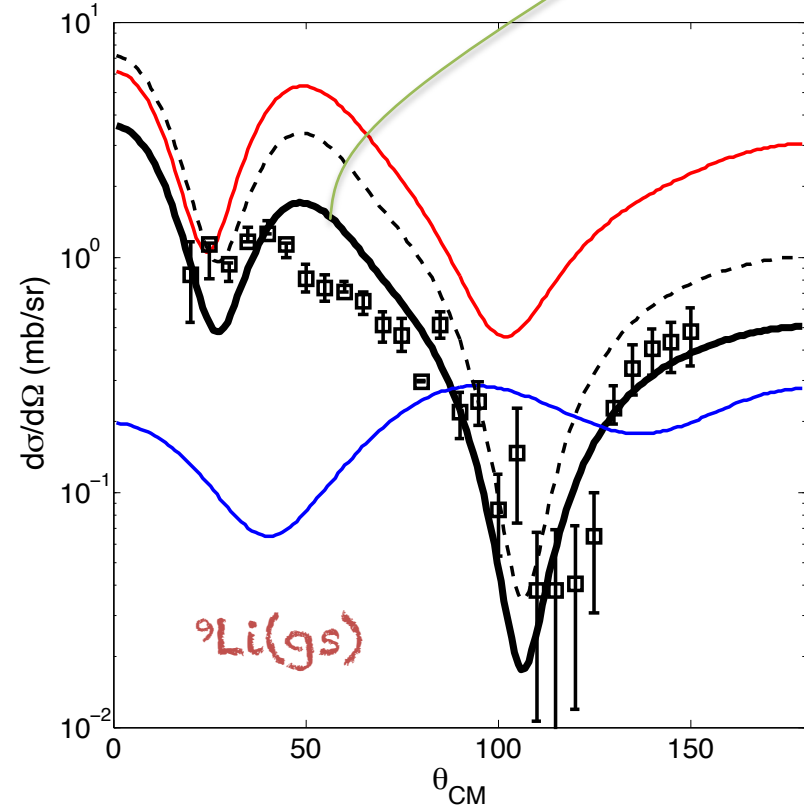
GP, Barranco, Vigezzi, Broglia  
PRL **105** 172502 (2010)

$$0.45|s_{1/2}^2(0)\rangle + 0.55|p_{1/2}^2(0)\rangle + 0.04|d_{5/2}^2(0)\rangle$$

$$+ 0.7 |(p_{1/2}, s_{1/2})_{1^-} \otimes 1^-; 0\rangle$$

$$+ 0.1 |(s_{1/2}, d_{5/2})_{2^+} \otimes 2^+; 0\rangle 10^0$$

reaction calculation in 2-order DWBA, dominated by successive transfer of the 2 neutrons (E. Vigezzi talk yesterday)



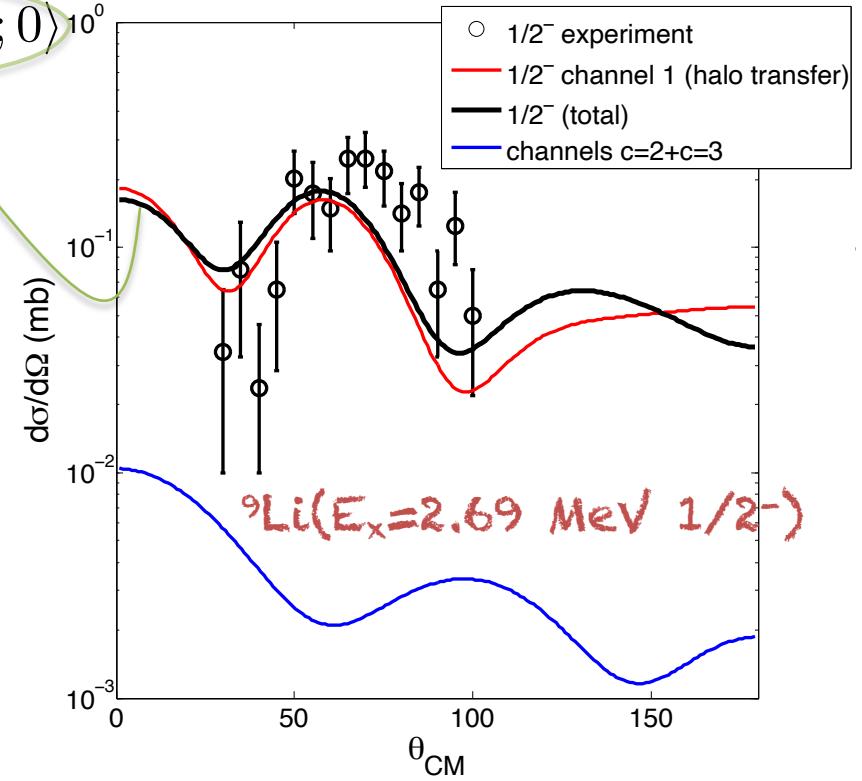
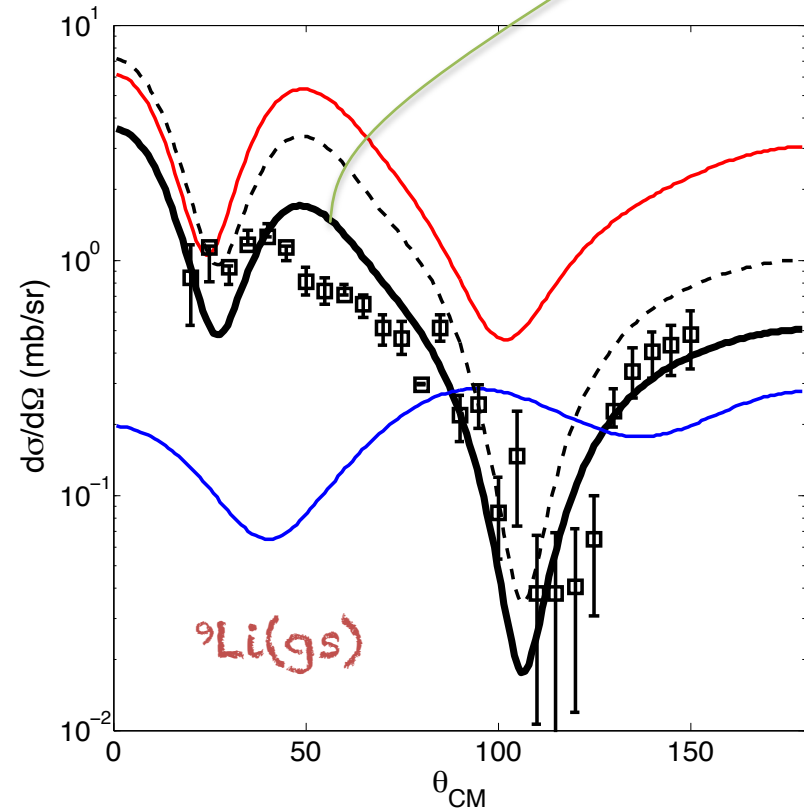
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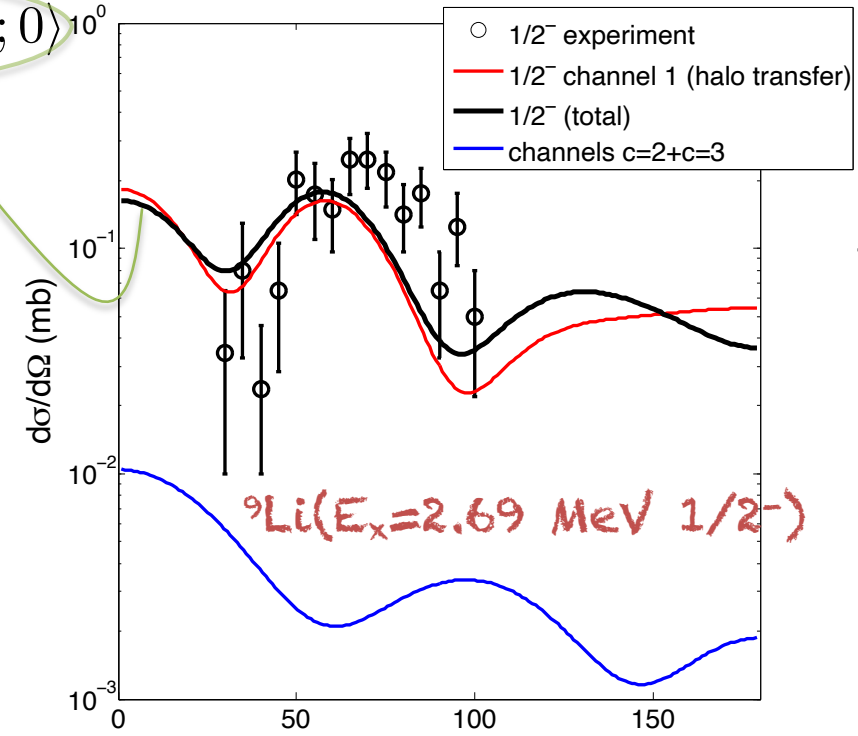
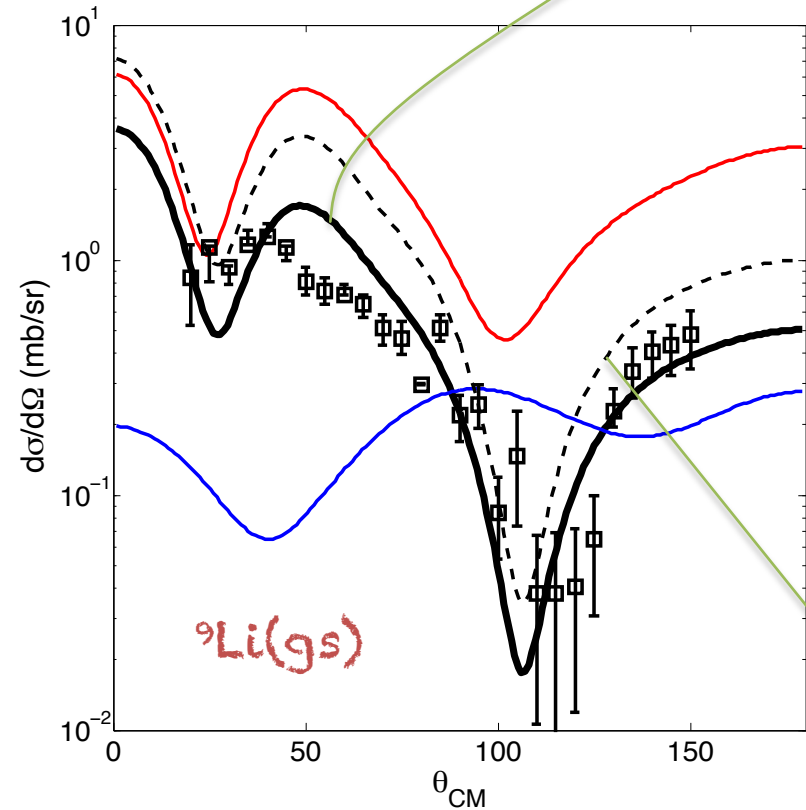
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$$0.63|s_{1/2}^2(0)\rangle + 0.76|p_{1/2}^2(0)\rangle + 0.14|d_{1/2}^2(0)\rangle$$

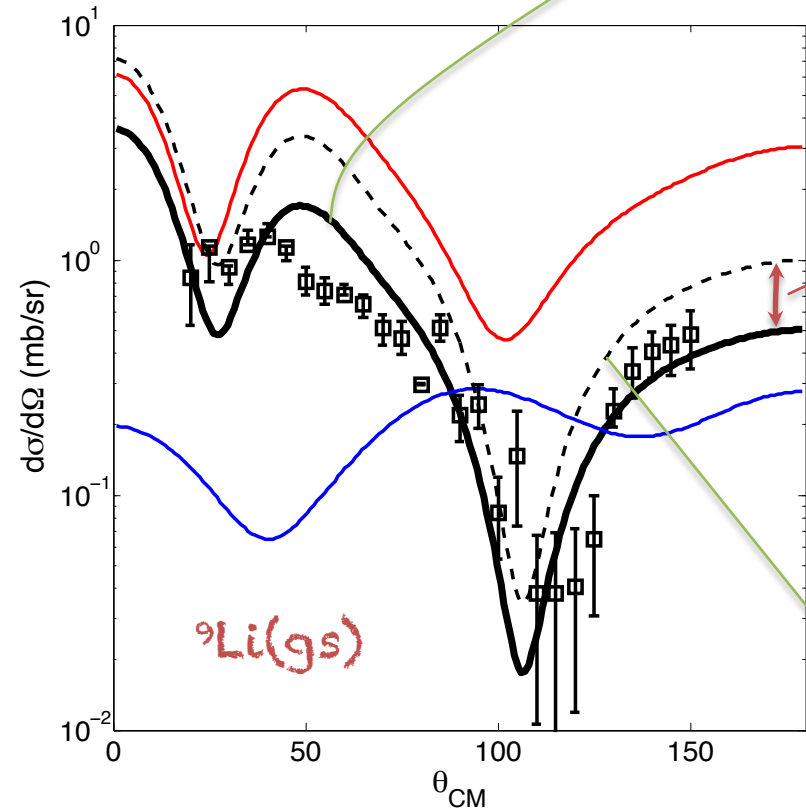
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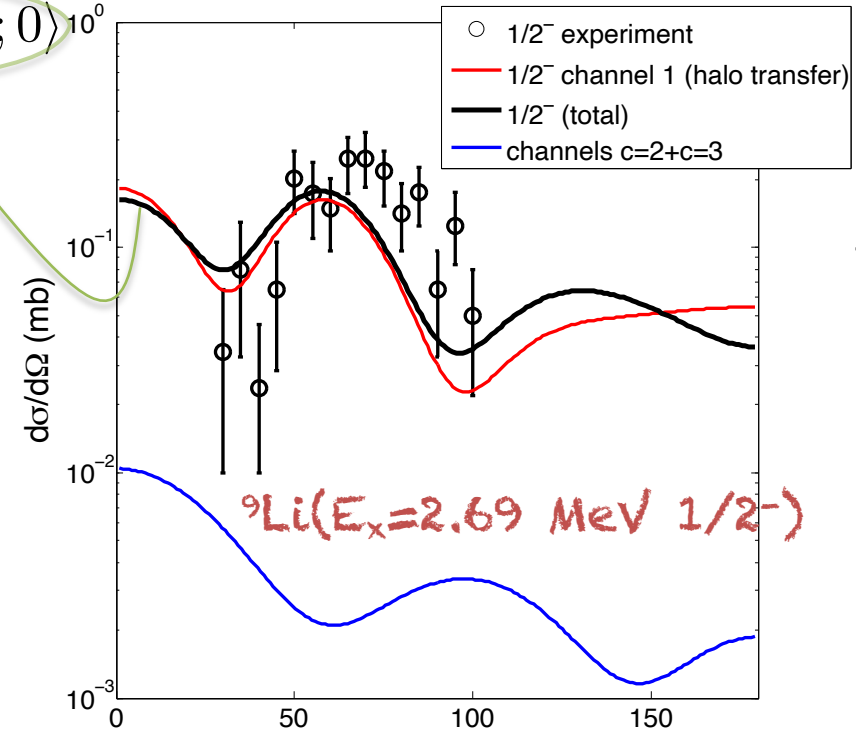
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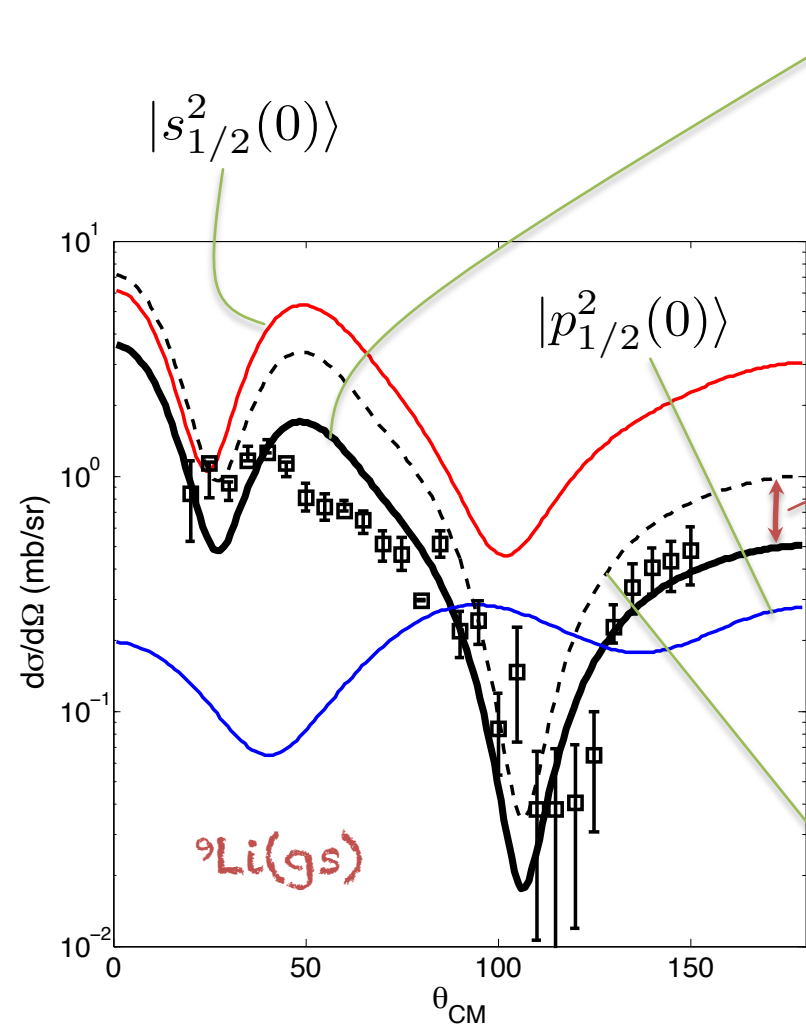


depletion of pp strength due to coupling with PDR



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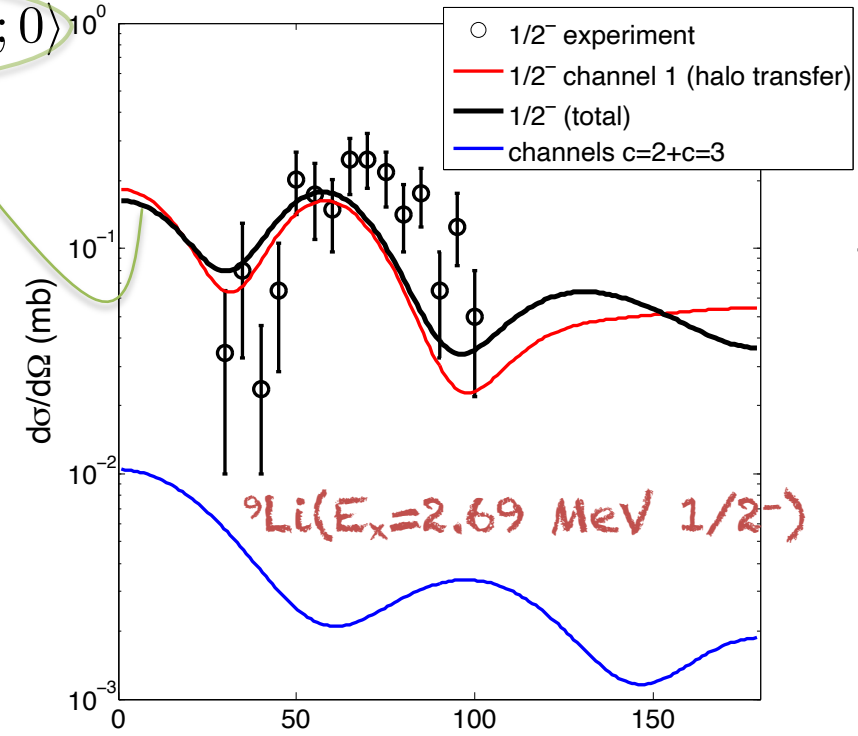


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# The PDR as a two-quasiparticle mode

- The **PDR** is rather well described in the harmonic approximation (RPA, QRPA) as a **two-quasiparticle mode**.
- Therefore, PDR in a nucleus  $A_0$  can be better **probed** with two-quasiparticle fields, i.e., particle-hole (**ph**), particle-particle (**pp**), and hole-hole (**hh**) fields.

*ph*

Coulomb, inelastic, and  $\gamma$ -induced excitation on  $A_0$ :

- $A_0(d,d')$   $A_0(\text{PDR})$
- $A_0(p,p')$   $A_0(\text{PDR})$
- $A_0(\alpha,\alpha')$   $A_0(\text{PDR})$
- $A_0(\gamma,\gamma')$   $A_0(\text{PDR})$
- $A_0(n,n')$   $A_0(\text{PDR})$
- $A_0(X,X')$   $A_0(\text{PDR})$

(Vandebrouck talk)

one-nucleon transfer on  $A_0-1$ :

- $A_0-1(d,p)$   $A_0(\text{PDR})$   
(Spieker, Weinert, and Khumalo talks)

*pp*

two-nucleon transfer on  $A_0-2$ :

- $A_0-2(t,p)$   $A_0(\text{PDR})$

**proposed  
in this talk**

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complementary classification of dipole modes

isovector



isoscalar

ph

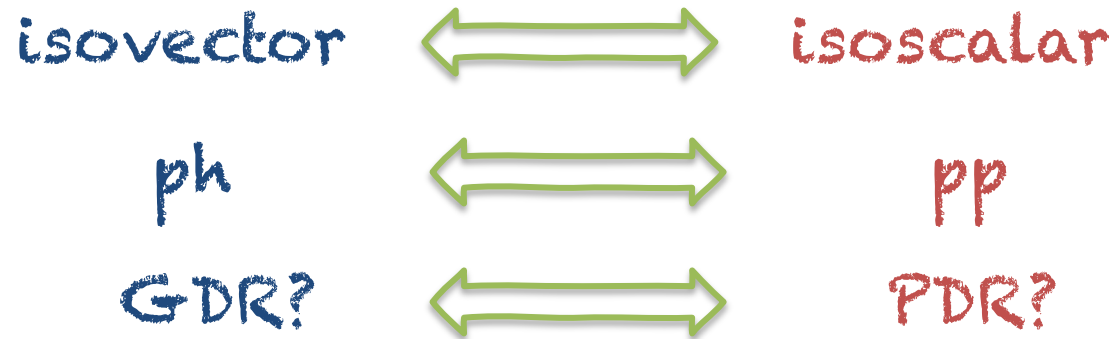


pp

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complementary classification of dipole modes



# we compute the $^{11}\text{Li}$ PDR structure in RPA

## 3 representative low-lying dipole RPA peaks

E=0.65 MeV				E=1.21 MeV				E=2 MeV						
<i>i</i>	<i>j</i>	$X_{ij}$	$Y_{ij}$	<i>i</i>	<i>j</i>	$X_{ij}$	$Y_{ij}$	<i>i</i>	<i>j</i>	$X_{ij}$	$Y_{ij}$			
$\nu$	$2s_{1/2}$	$1p_{1/2}$	-0.780	0.078	$\nu$	$2s_{1/2}$	$1p_{1/2}$	-0.119	0.048	$\nu$	$3s_{1/2}$	$1p_{1/2}$	-0.118	0.040
$\nu$	$3s_{1/2}$	$1p_{1/2}$	0.479	0.108	$\nu$	$3s_{1/2}$	$1p_{1/2}$	-0.748	0.074	$\nu$	$4s_{1/2}$	$1p_{1/2}$	-0.821	0.046
$\nu$	$4s_{1/2}$	$1p_{1/2}$	0.220	0.106	$\nu$	$4s_{1/2}$	$1p_{1/2}$	0.410	0.080	$\nu$	$5s_{1/2}$	$1p_{1/2}$	0.250	0.046
$\nu$	$5s_{1/2}$	$1p_{1/2}$	0.144	0.093	$\nu$	$5s_{1/2}$	$1p_{1/2}$	0.181	0.075	$\nu$	$6s_{1/2}$	$1p_{1/2}$	0.116	0.043
$\nu$	$6s_{1/2}$	$1p_{1/2}$	0.106	0.080	$\nu$	$6s_{1/2}$	$1p_{1/2}$	0.117	0.067	$\nu$	$1p_{3/2}$	$4d_{5/2}$	0.144	0.081
$\nu$	$1p_{3/2}$	$4d_{5/2}$	0.166	0.139	$\nu$	$1p_{3/2}$	$4d_{5/2}$	0.170	0.121	$\nu$	$1p_{3/2}$	$5d_{5/2}$	0.201	0.125
$\nu$	$1p_{3/2}$	$5d_{5/2}$	0.241	0.208	$\nu$	$1p_{3/2}$	$5d_{5/2}$	0.243	0.183	$\nu$	$1p_{3/2}$	$6d_{5/2}$	0.201	0.135
$\nu$	$1p_{3/2}$	$6d_{5/2}$	0.250	0.221	$\nu$	$1p_{3/2}$	$6d_{5/2}$	0.249	0.196	$\nu$	$1p_{3/2}$	$7d_{5/2}$	0.156	0.112
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## Pygmy resonances: what's in a name?

R A Broglia<sup>1,2,7</sup>, F Barranco<sup>3</sup>, A Idini<sup>4</sup>, G Potel<sup>5</sup> and E Vigezzi<sup>6</sup>

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## Pygmy resonances: what's in a name?

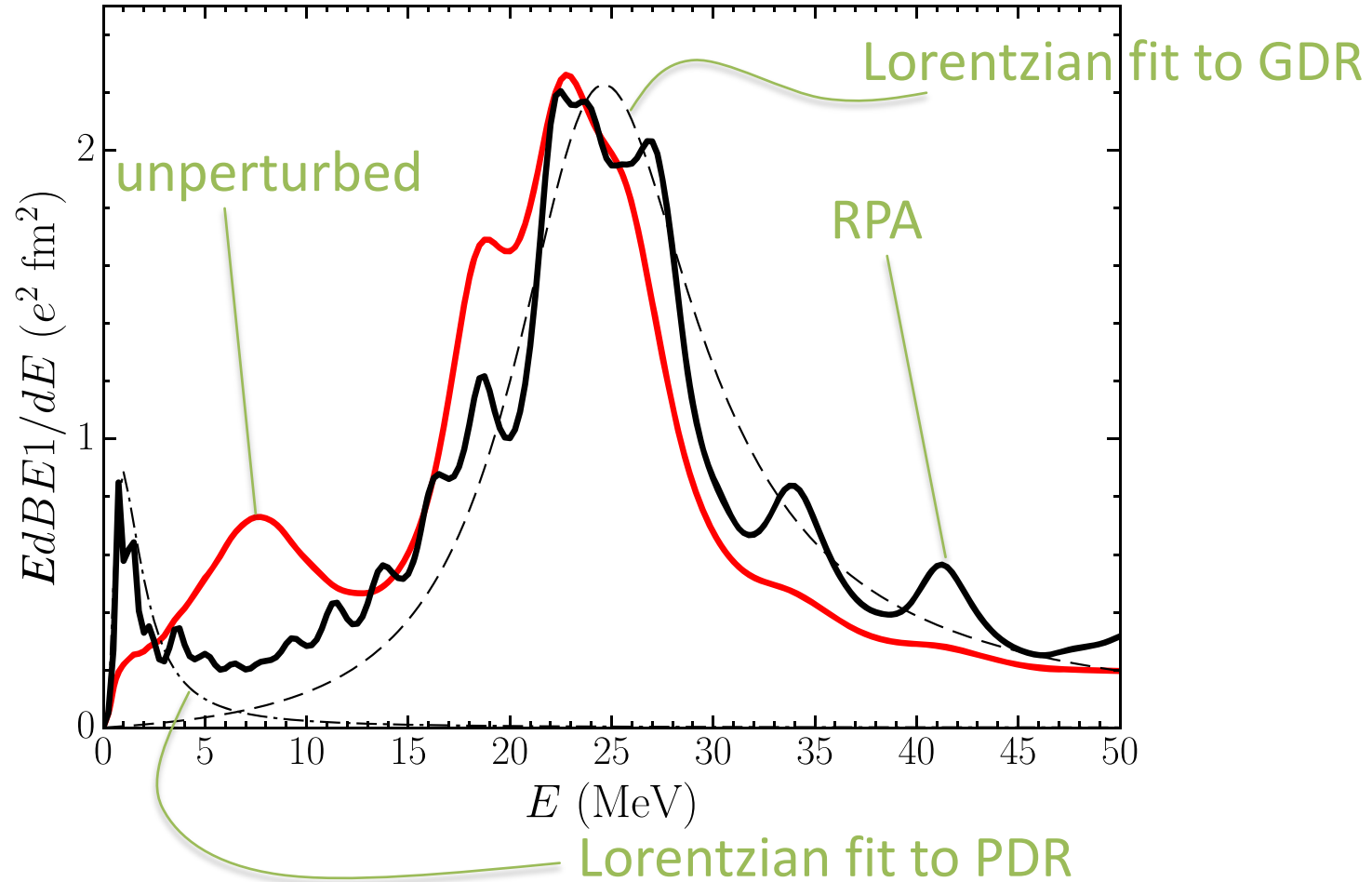
R A Broglia<sup>1,2,7</sup>, F Barranco<sup>3</sup>, A Idini<sup>4</sup>, G Potel<sup>5</sup> and E Vigezzi<sup>6</sup>

largest components are  
2-quasiparticle neutron  
halo  $(s_{1/2} p_{1/2})_1$ - states



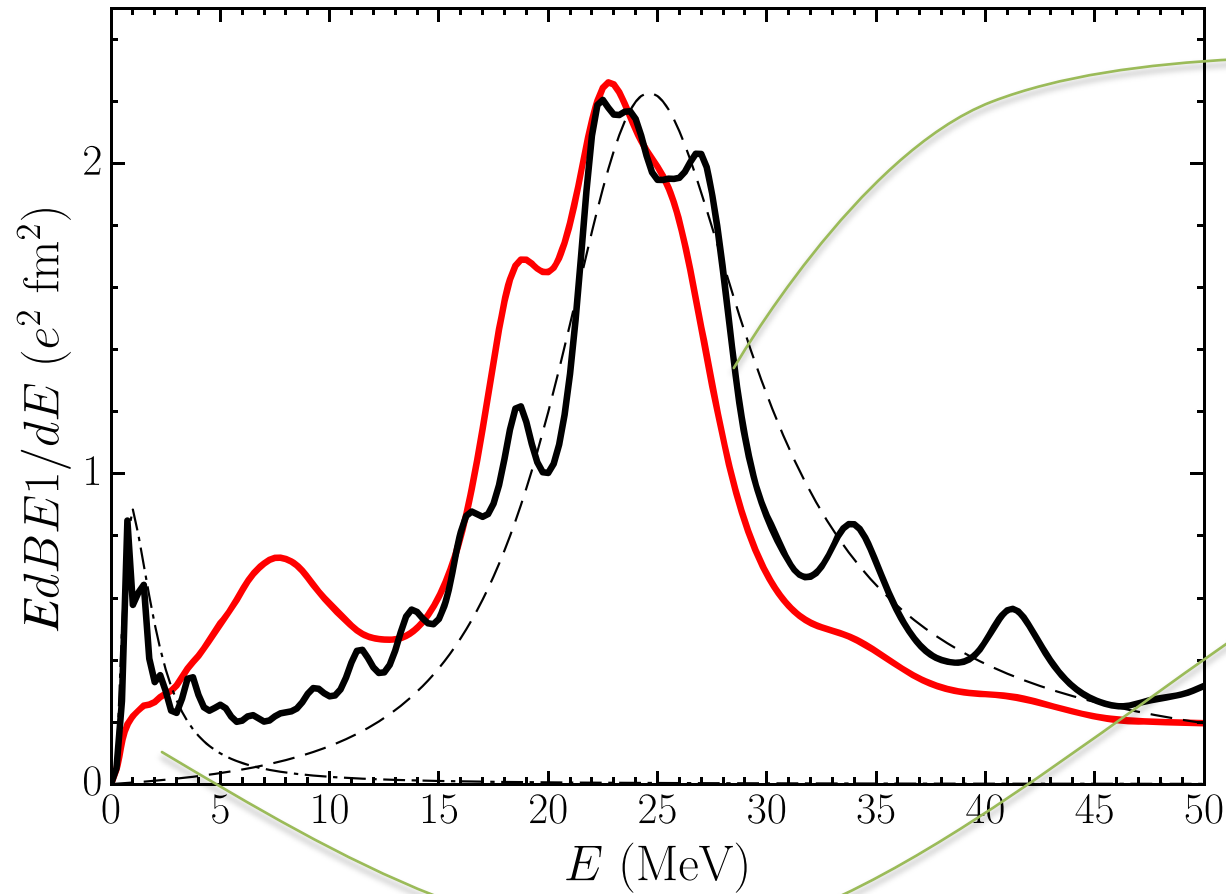
# the PDR exhausts about 8% of the EWSR

dipole response function

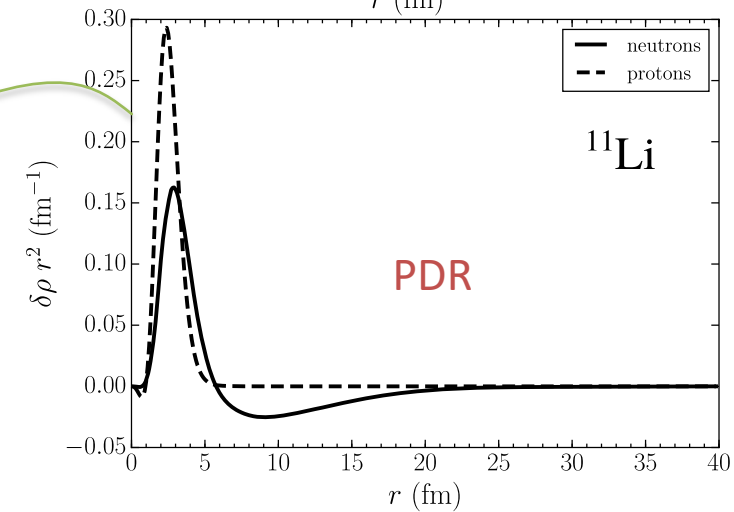
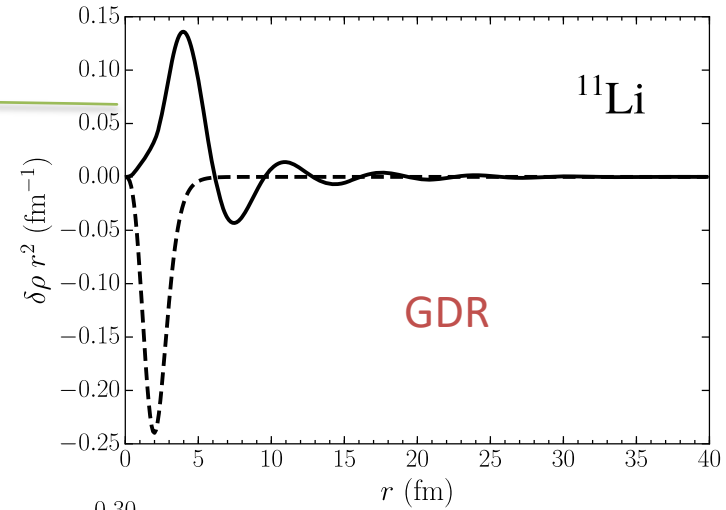


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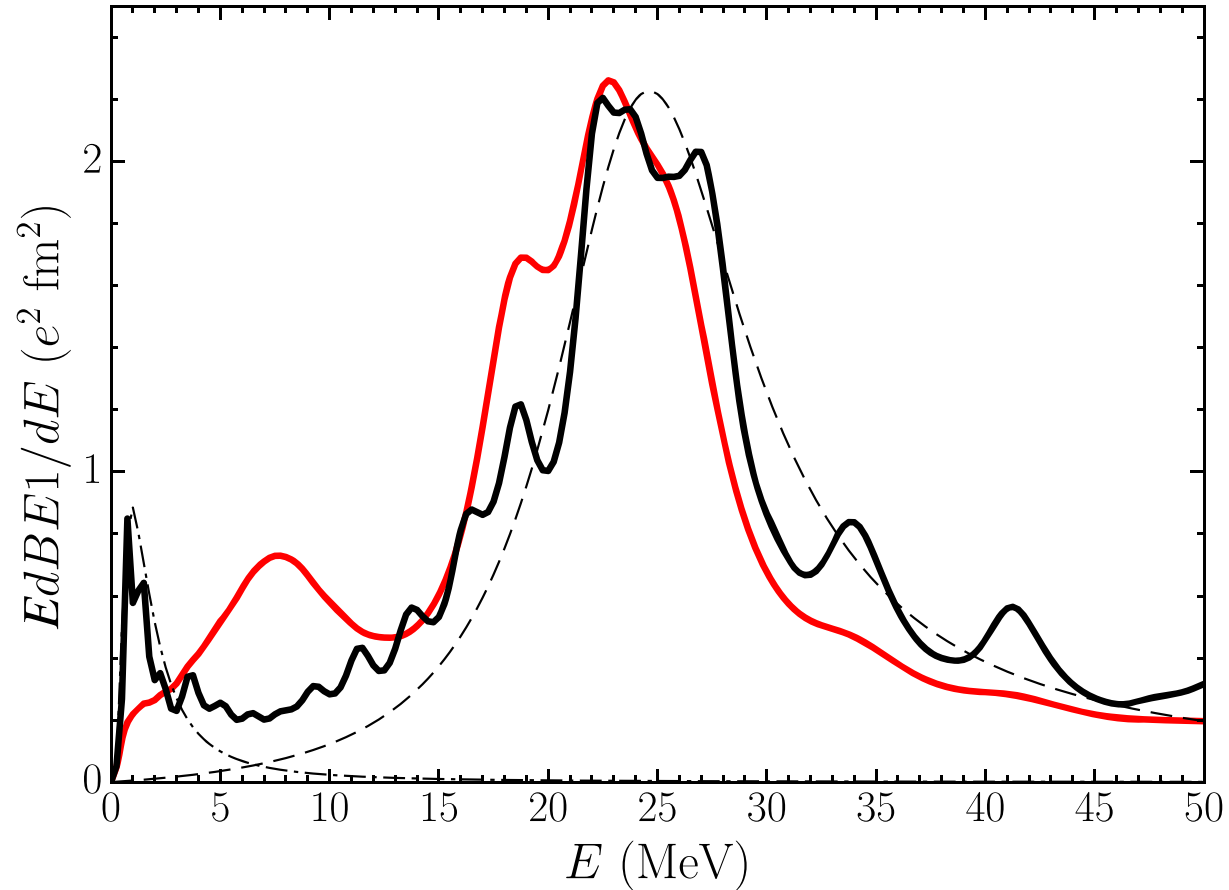


transition densities



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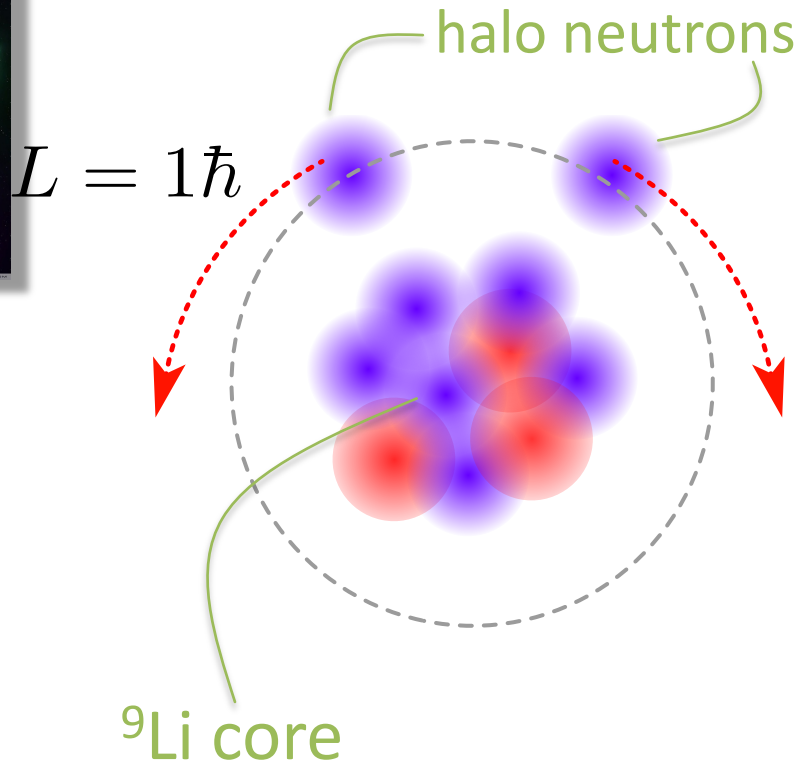
dipole response function



experiment approved at FRIB to probe the whole dipole response with  $(p, p')$ .  
Spokepersons: Ayyad, Zamora

# the PDR has the structure of an elementary quantum vortex

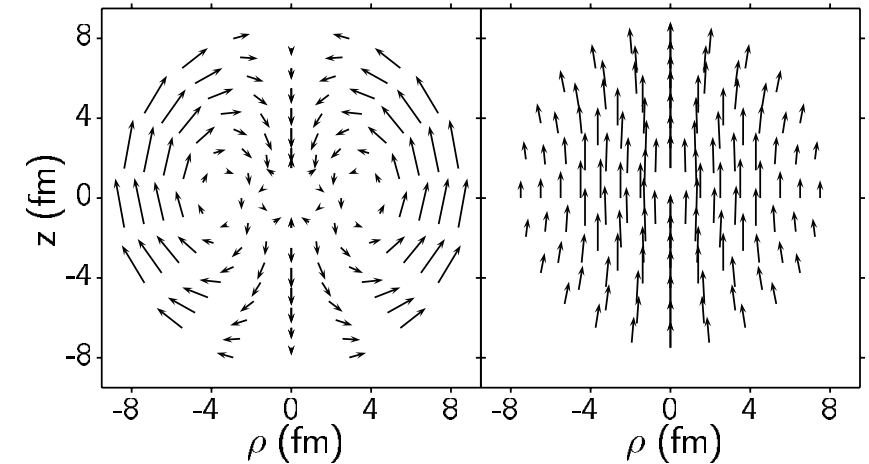
structure of a multipolar (1<sup>-</sup>) Cooper pair:  
elementary quantum vortex



velocity field of <sup>208</sup>Pb dipole states

$E_x = 6.5 - 10.5$  MeV

$E_x > 10.5$  MeV



Ryezayeva *et al.* PRL **89** (2002) 272502

- Is vorticity a signature of PDR?
- Is there an experimental signature for it?

# Probing the $^{11}\text{Li}$ PDR with 2-neutron transfer

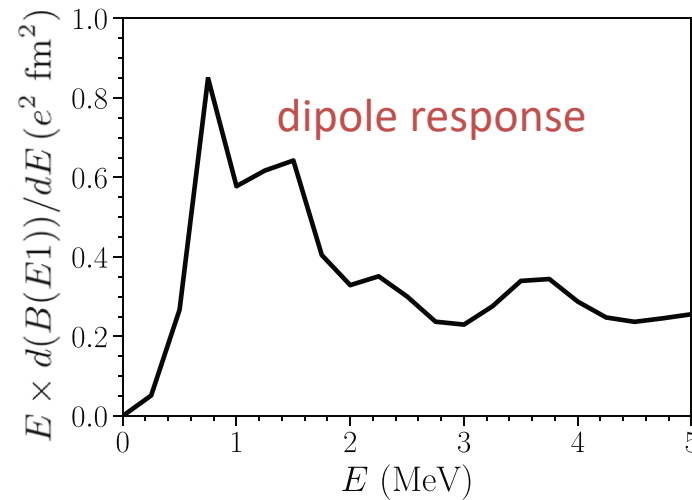
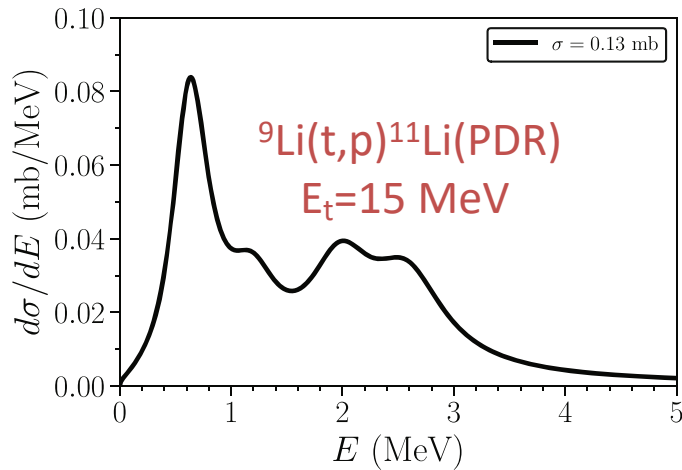
Eur. Phys. J. A (2019) 55: 243  
DOI 10.1140/epja/i2019-12789-y

THE EUROPEAN  
PHYSICAL JOURNAL A

Regular Article – Theoretical Physics

## Characterization of vorticity in pygmy resonances and soft-dipole modes with two-nucleon transfer reactions\*

R.A. Broglia<sup>1,2</sup>, F. Barranco<sup>3</sup>, G. Potel<sup>4,a</sup>, and E. Vigezzi<sup>5</sup>



- we predict the **population of the PDR** with the 2-neutron transfer reaction  $^{9}\text{Li}(t,p)^{11}\text{Li}(\text{PDR})$ , with cross section  $\sigma=0.3\text{mb}$
- **shape** of differential cross section very similar to that of the **dipole response**
- **absolute value** of cross section is a measure of the **pp** nature of the PDR

# Probing the $^{11}\text{Li}$ PDR with 2-neutron transfer

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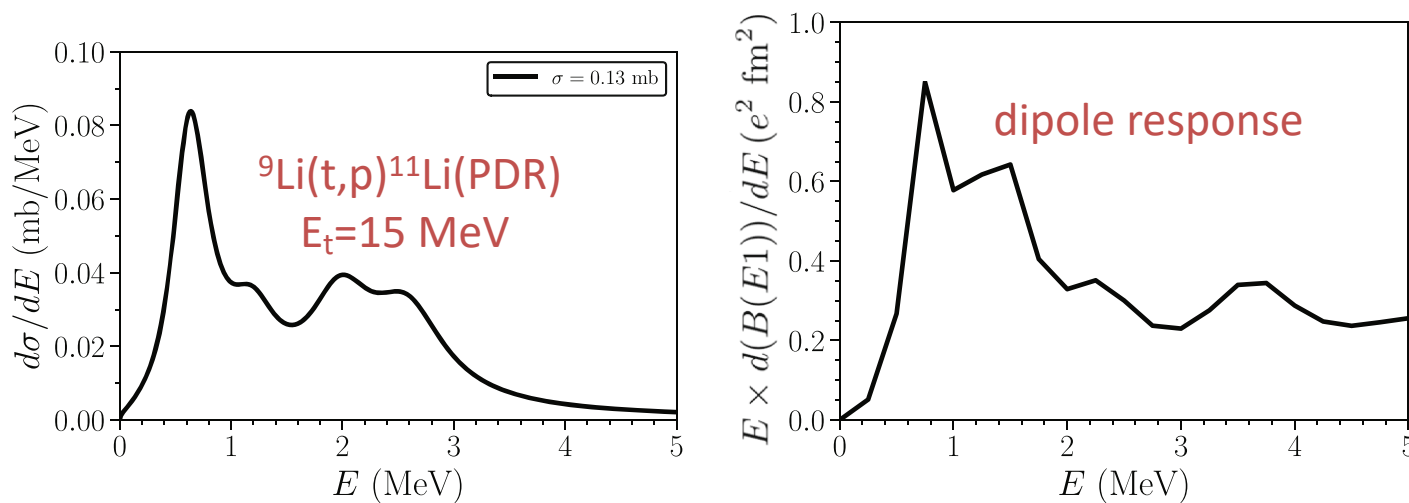
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EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

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Probing the  $^{11}\text{Li}$  low-lying dipole strength via  $^9\text{Li}(t,p)$  with the ISS



Y. Ayyad<sup>1</sup>, E. Vigezzi<sup>2</sup>, G. Potel<sup>3</sup>, R. Broglia<sup>4,5</sup>, B.P. Kay<sup>6</sup>,  
A.O. Macchiavelli<sup>7</sup>, H. Alvarez-Pol<sup>8</sup>, F. Barranco<sup>9</sup>, D. Bazin<sup>1,10</sup>, M. Caamaño<sup>8</sup>,  
A. Ceulemans<sup>11</sup>, J. Chen<sup>1</sup>, H.L. Crawford<sup>7</sup>, B. Fernández-Domínguez<sup>8</sup>, S.J. Freeman<sup>12</sup>,  
L.P. Gaffney<sup>13</sup>, C.R. Hoffman<sup>6</sup>, R. Kanungo<sup>14</sup>, C. Morse<sup>7</sup>, O. Poleshchuk<sup>11</sup>, R. Raabe<sup>11</sup>,  
C.A. Santamaria<sup>7</sup>, D.K. Sharp<sup>12</sup>, T. L. Tang<sup>6</sup>, K. Wimmer<sup>15</sup>, A.H. Wuosmaa<sup>16</sup>

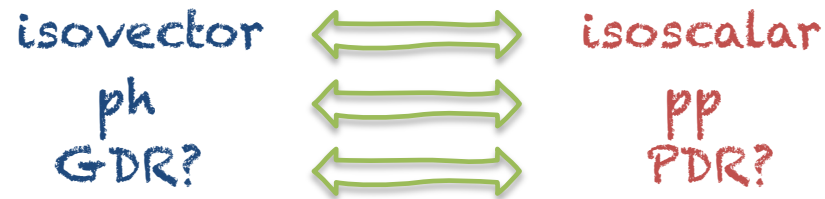
experiment approved at ISOLDE facility  
(CERN). Spokepersons: Ayyad, Vigezzi

# Conclusions

- the PDR plays an important role in the structure of the exotic two-neutron halo nucleus  $^{11}\text{Li}$ : halo-PDR symbiotic nature
- our calculations point to a strong *pp* component of the PDR, as opposed to the more *ph* nature of the GDR

talks by Vandebrouck,  
Spieker, Weinert,  
Khumalo

complementary classification of dipole modes



- PDR of  $^{11}\text{Li}$  as a *vortical* excitation of the halo. Extrapolable to *neutron skins*?
- Approved experiments:  $^{11}\text{Li}(p,p')^{11}\text{Li}^*$  @ FRIB, and  $^9\text{Li}(t,p)^{11}\text{Li}(\text{PDR})$  @ ISOLDE

- along with (d,p) and (n,n'), (t,p) to join the ranks of *novel probes to the PDR*
- personal wish: (t,p) measurements on nuclei with *neutron skin*. Maybe with new FSU triton beam?



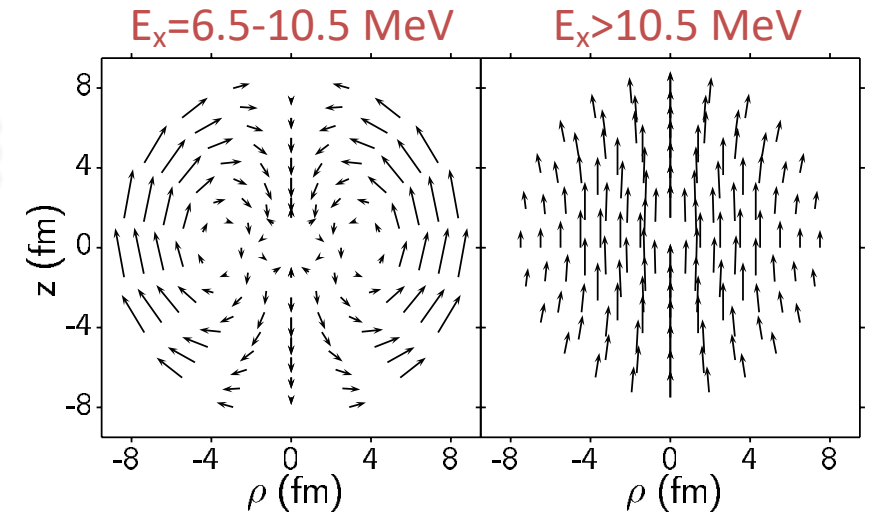


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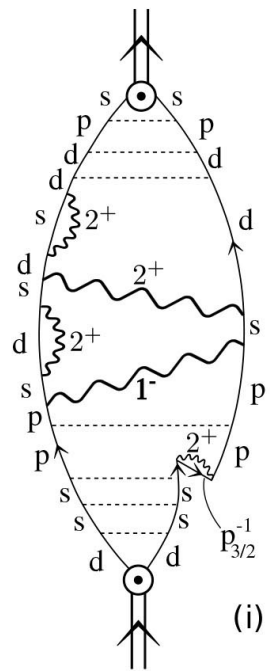
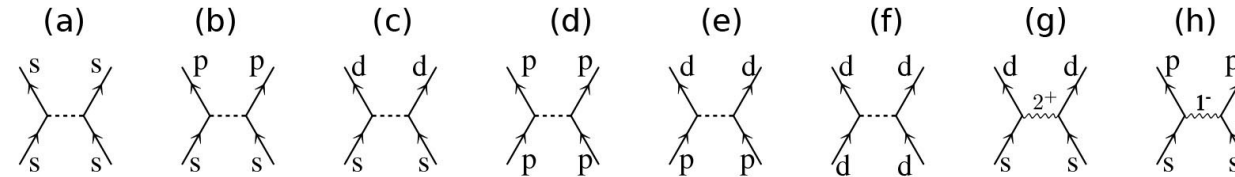
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					$\pi$	$1p_{3/2}$	$1d_{5/2}$	0.322	0.294					

velocity field of  $^{208}\text{Pb}$  dipole states

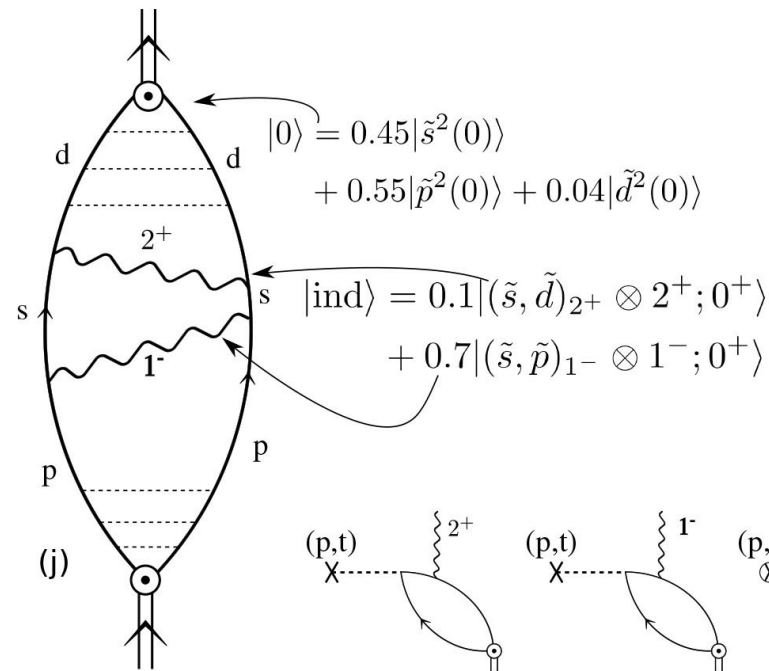


Ryezayeva *et al.* PRL **89** (2002) 272502

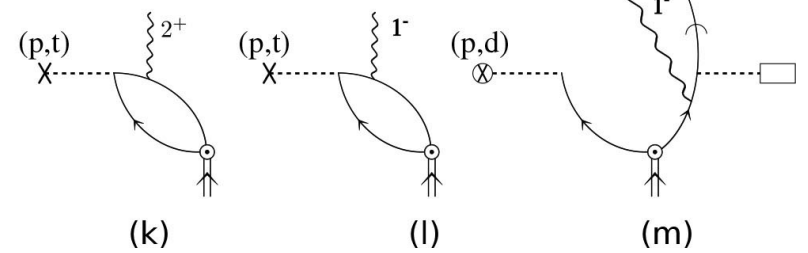
# Ground state of $^{11}\text{Li}$



$s \rightarrow s_{1/2}$   
 $p \rightarrow p_{1/2}$   
 $d \rightarrow d_{5/2}$



$|\tilde{0}\rangle = |0\rangle + |\text{ind}\rangle$



we compute the  $^{11}\text{Li}$  PDR structure and the  $^9\text{Li}(t,p)^{11}\text{Li}$ (PDR)  
cross section

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# proposal to measure ${}^9\text{Li}(t,p){}^{11}\text{Li}(\text{PDR})$ approved at ISOLDE

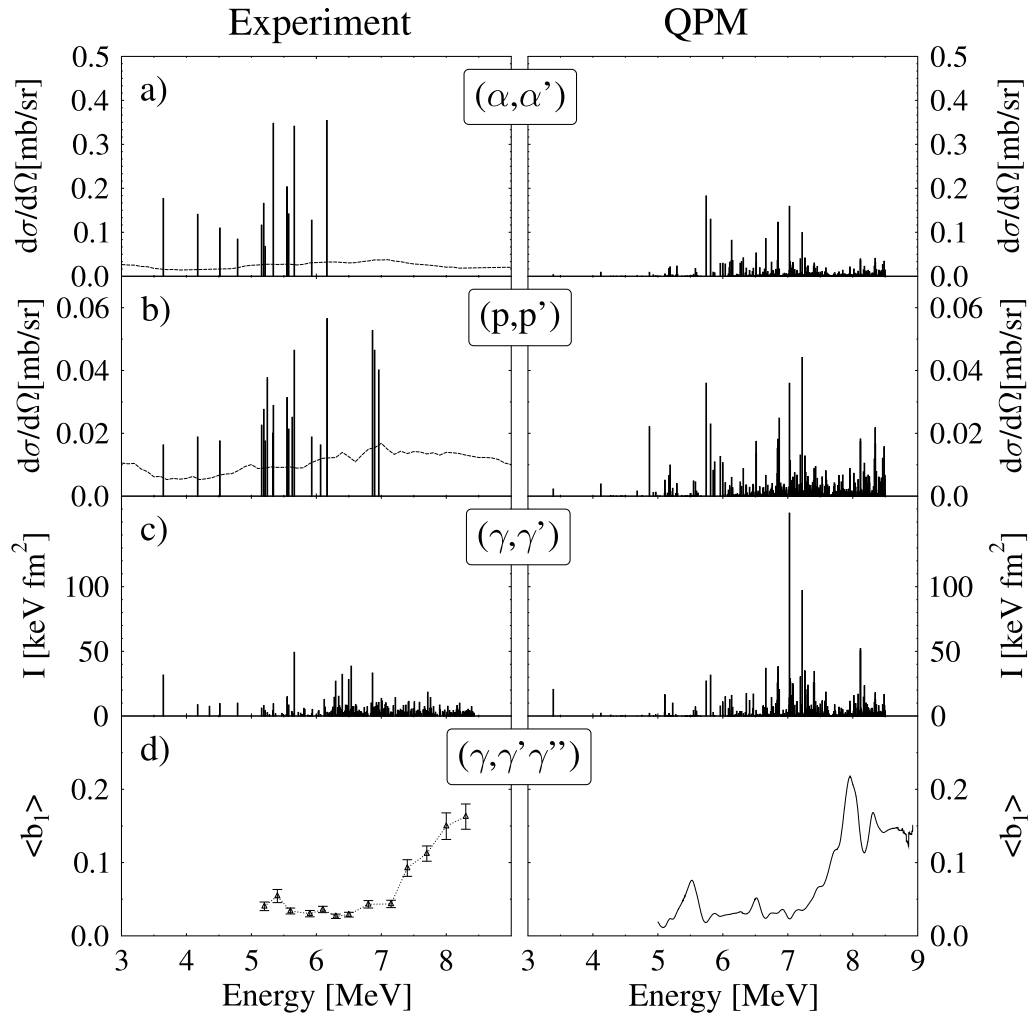
EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

Probing the  ${}^{11}\text{Li}$  low-lying dipole strength via  ${}^9\text{Li}(t,p)$  with the  
ISS

September 22, 2020

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A.O. Macchiavelli<sup>7</sup>, H. Alvarez-Pol<sup>8</sup>, F. Barranco<sup>9</sup>, D. Bazin<sup>1,10</sup>, M. Caamaño<sup>8</sup>,  
A. Ceulemans<sup>11</sup>, J. Chen<sup>1</sup>, H.L. Crawford<sup>7</sup>, B. Fernández-Domínguez<sup>8</sup>, S.J. Freeman<sup>12</sup>,  
L.P. Gaffney<sup>13</sup>, C.R. Hoffman<sup>6</sup>, R. Kanungo<sup>14</sup>, C. Morse<sup>7</sup>, O. Poleshchuk<sup>11</sup>, R. Raabe<sup>11</sup>,  
C.A. Santamaria<sup>7</sup>, D.K. Sharp<sup>12</sup>, T. L. Tang<sup>6</sup>, K. Wimmer<sup>15</sup>, A.H. Wuosmaa<sup>16</sup>

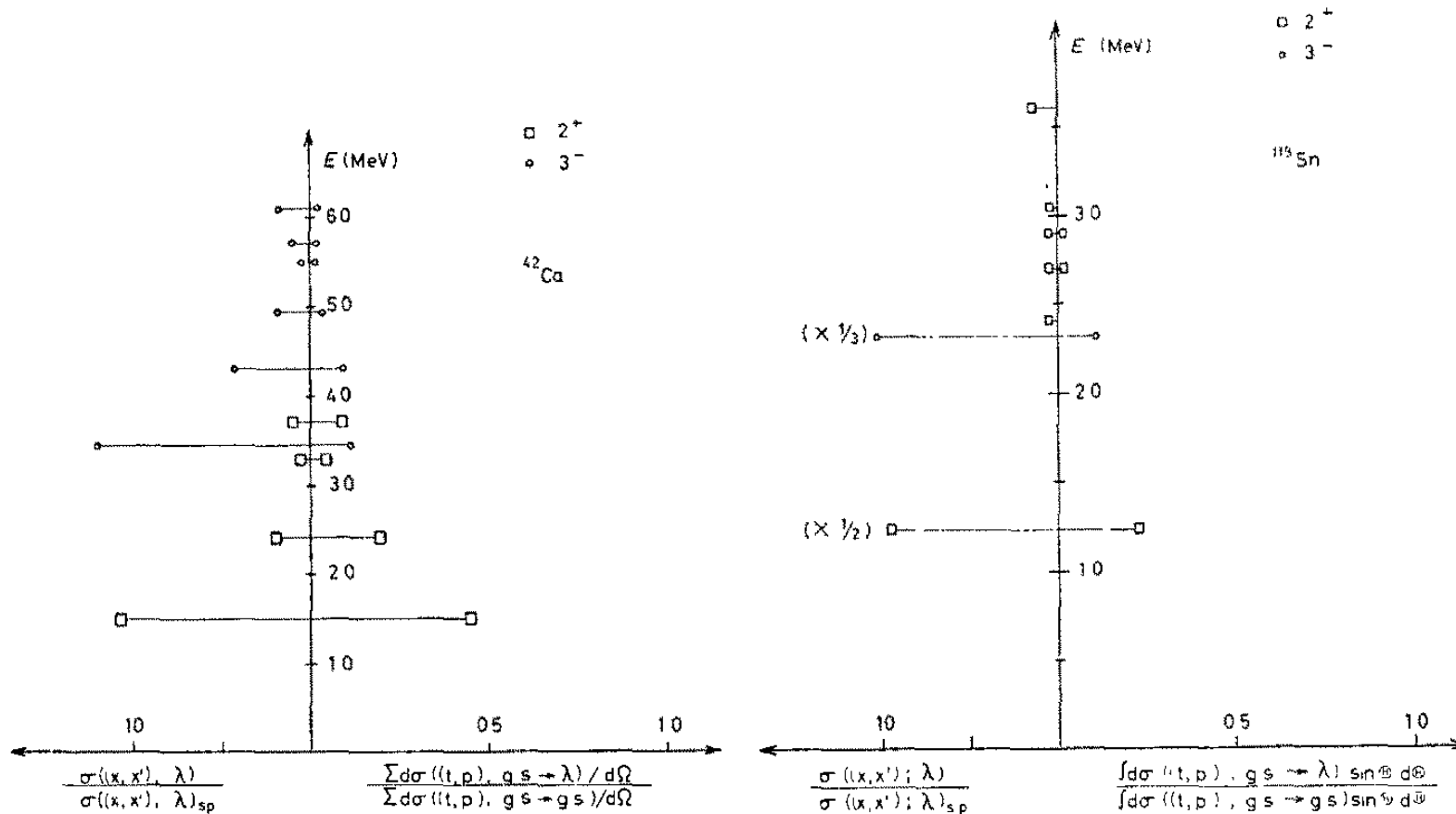
# the structure of the PDR can be addressed with different probes



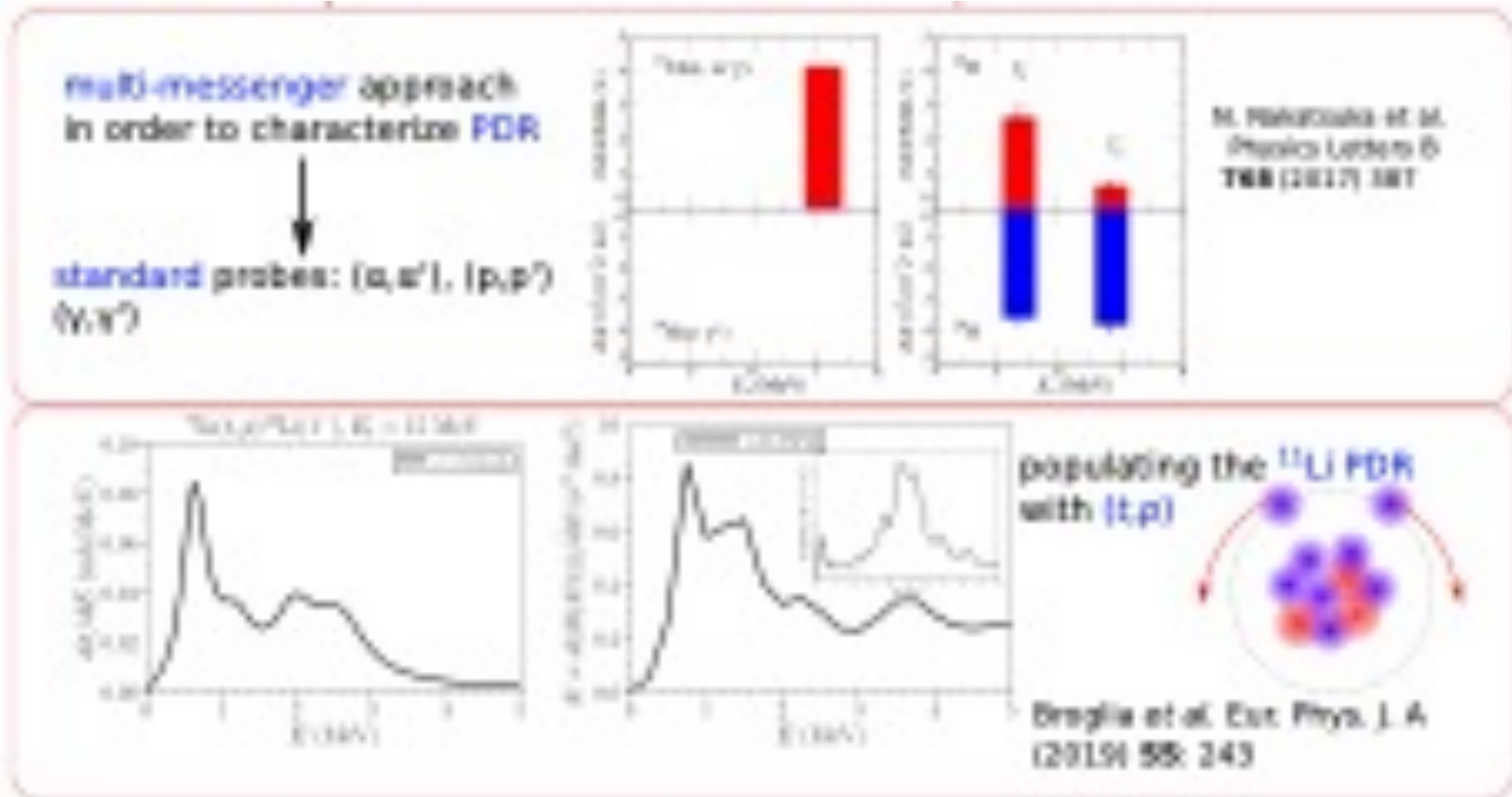
Vandebrouck talk

Savran 2018

# Inelastic excitation and two-nucleon transfer populate the same states

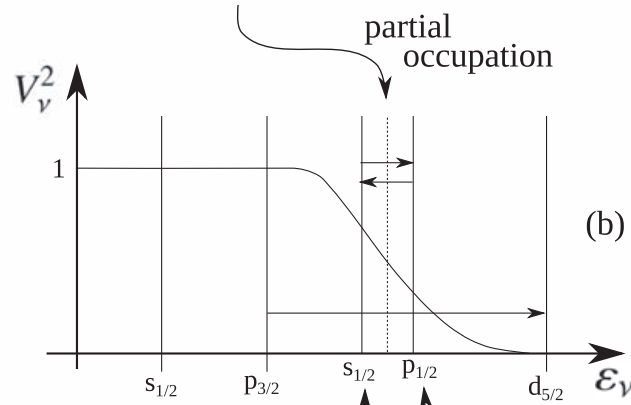


# Two neutron transfer, a novel probe for the PDR?



# Low-lying dipole strength

$$|0\rangle_v = |0\rangle + 0.7|(p_{1/2}, s_{1/2})_{1^-} \otimes 1^-; 0\rangle + 0.1|(s_{1/2}, d_{5/2})_{2^+} \otimes 2^+; 0\rangle$$



$$|0\rangle = 0.55|p_{1/2}^2\rangle + 0.45|s_{1/2}^2\rangle + 0.04|d_{5/2}^2\rangle$$

$$|1^-, \text{pygmy}\rangle = \alpha \Gamma_{\text{pygmy}}^\dagger |\text{halo}\rangle + \beta \Gamma_{\text{GDR}}^\dagger |\text{core}\rangle$$

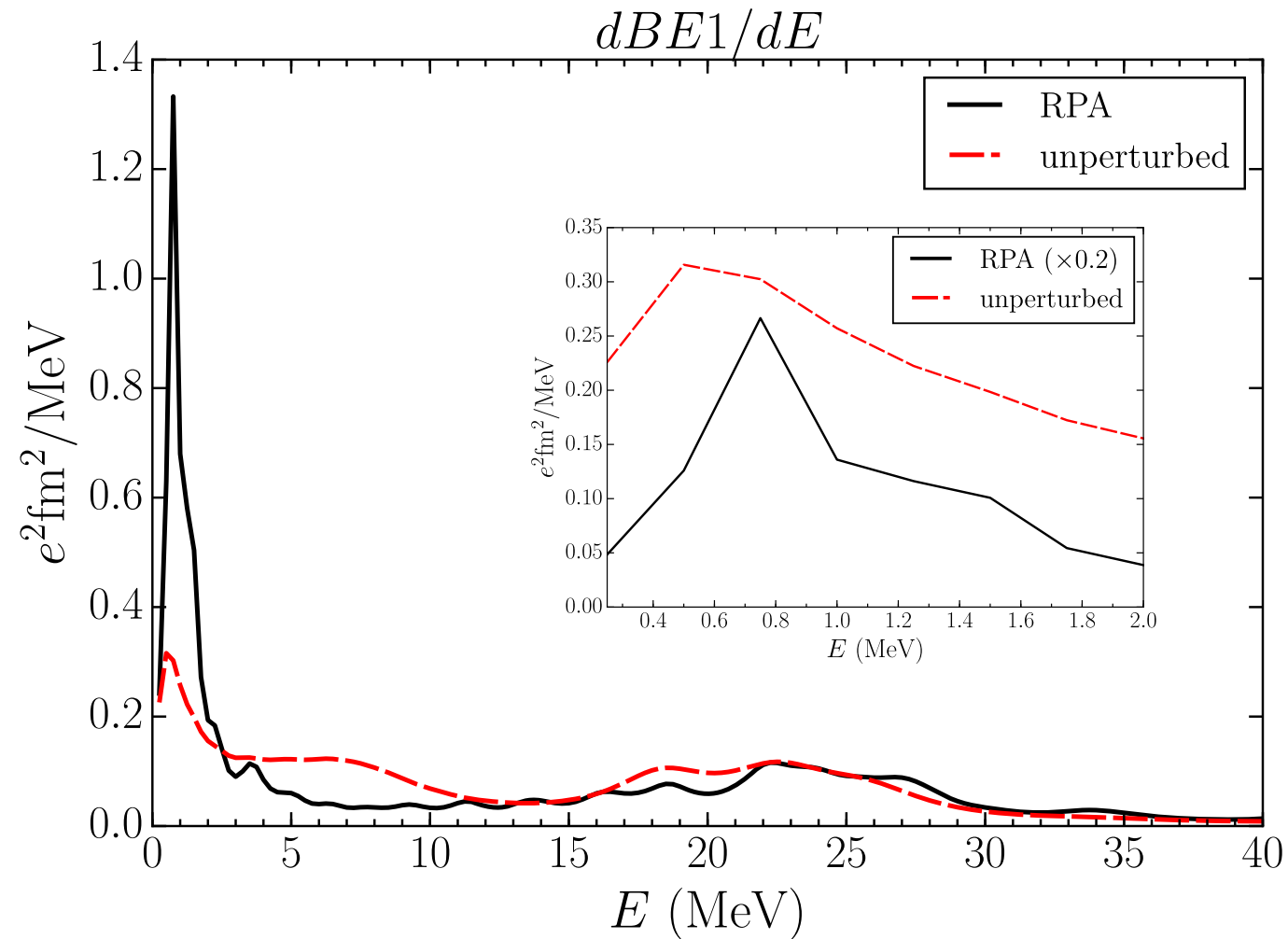
(a)  $\alpha^2 \gg \beta^2$

	$1p_{1/2}^{-1}2s_{1/2}$	$1p_{1/2}^{-1}3s_{1/2}$	$1p_{1/2}^{-1}4s_{1/2}$	$1p_{1/2}^{-1}1d_{3/2}$	$1p_{3/2}^{-1}4d_{5/2}$	$1p_{3/2}^{-1}5d_{5/2}$	$1p_{3/2}^{-1}6d_{5/2}$
X	-0.780	0.479	0.220	0.103	0.166	0.241	0.250
Y	0.078	0.108	0.106	0.075	0.139	0.208	0.221

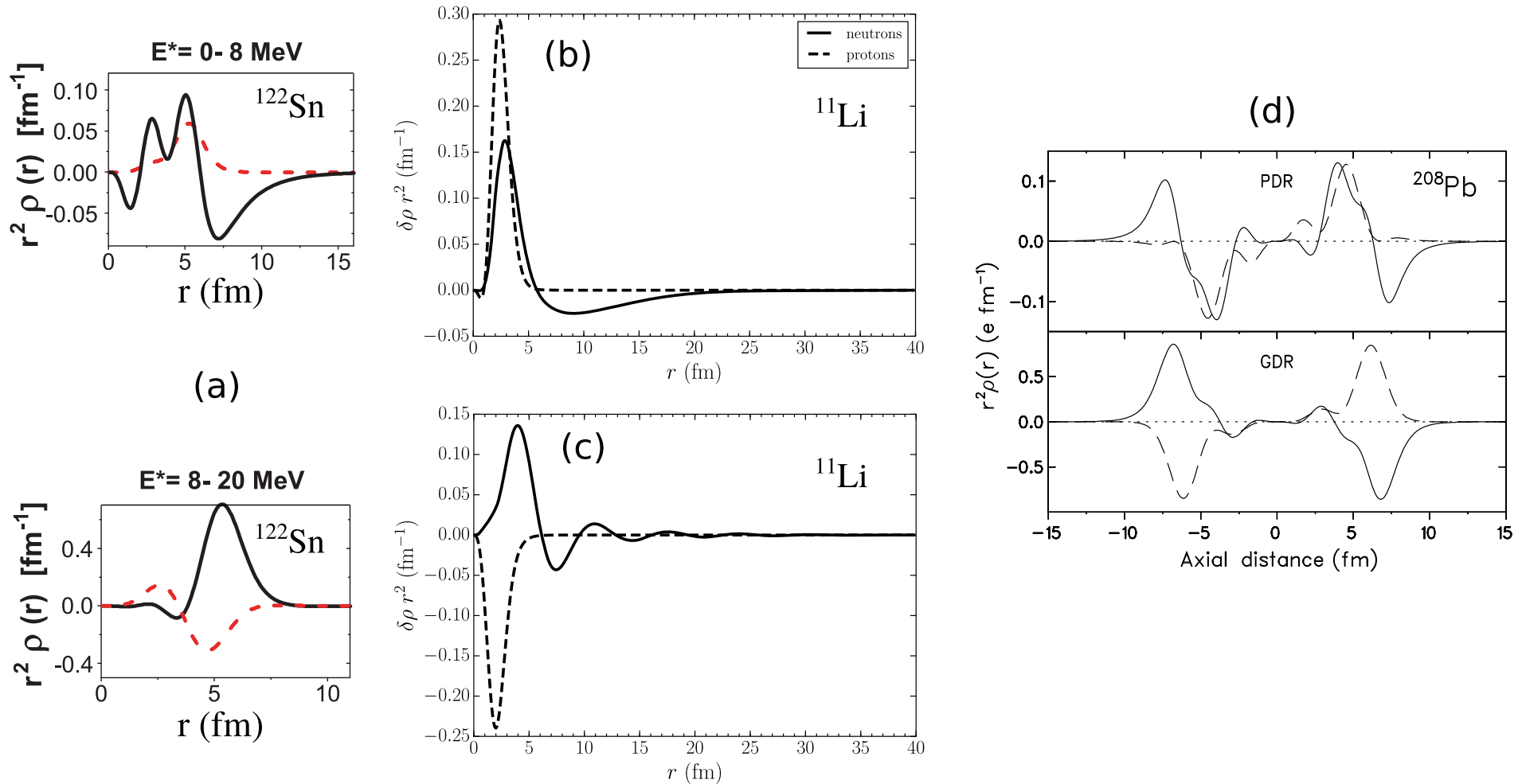
8% EWSR  $E_{1^-} \approx 0.7 \text{ MeV}$



# Full dipole strength

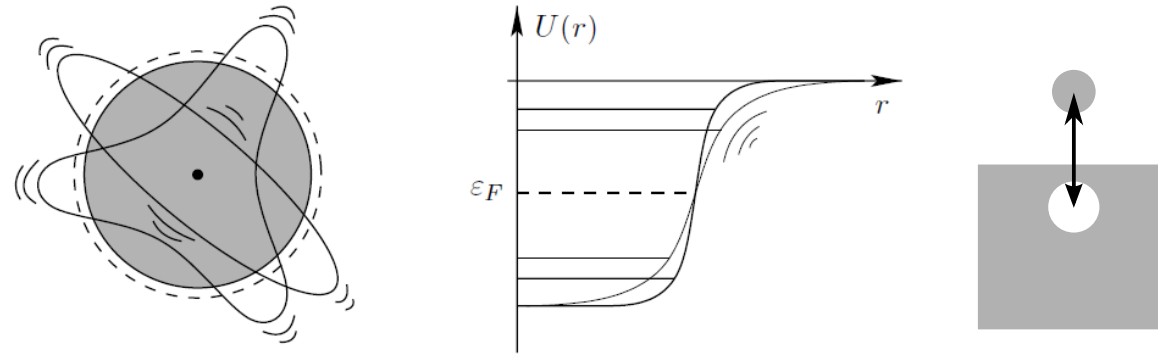


# Transition densities

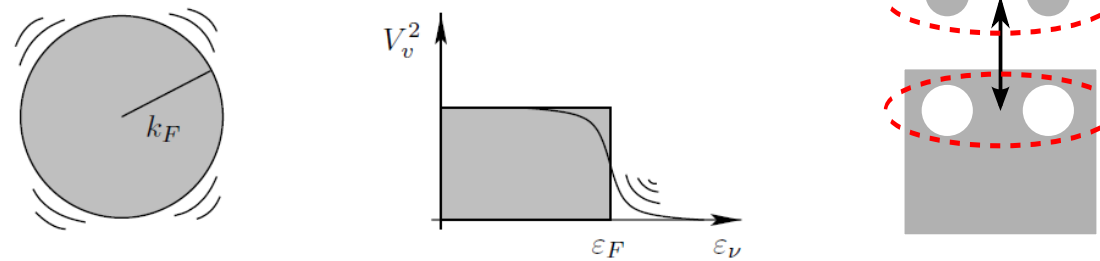


# Deformations in 3D space and in gauge space

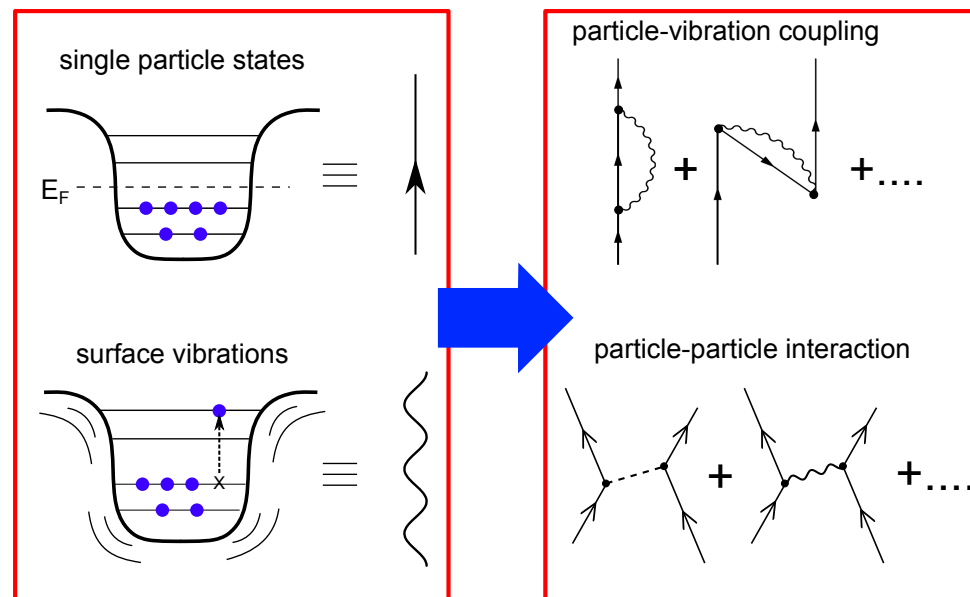
## 3D-surface deformations



## Fermi surface deformations



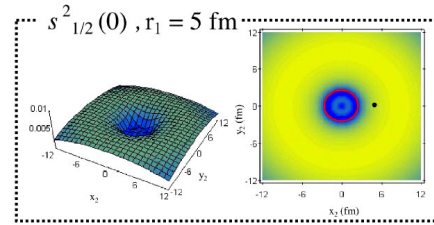
# NFT



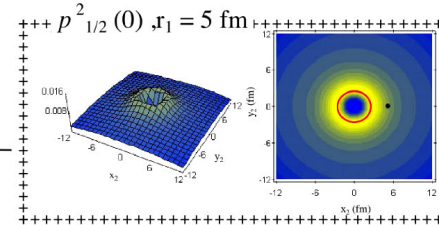
quasiparticles, multiplets, fragmentation

comparison with experiment

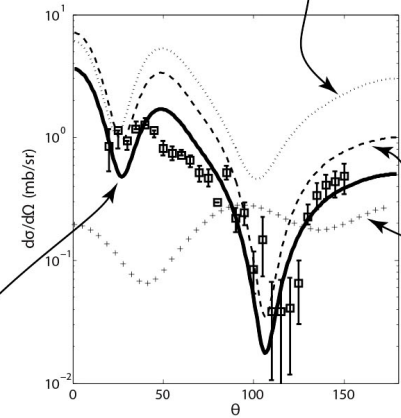
# $^{11}\text{Li}$ summary



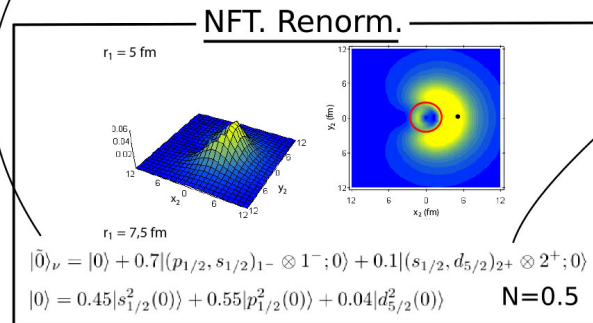
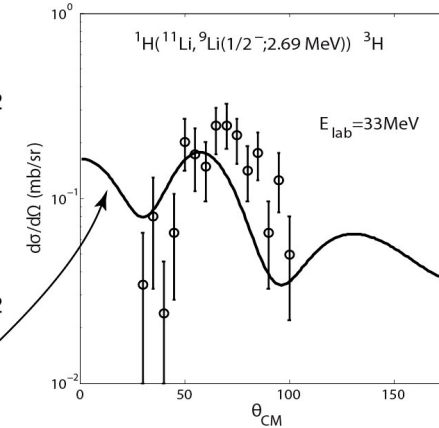
Barranco et al  
EPJ, A11 (2001) 305



Tanihata et al  
PRL, 100 (2008) 192502



Potel et al  
PRL, 105 (2010) 172502



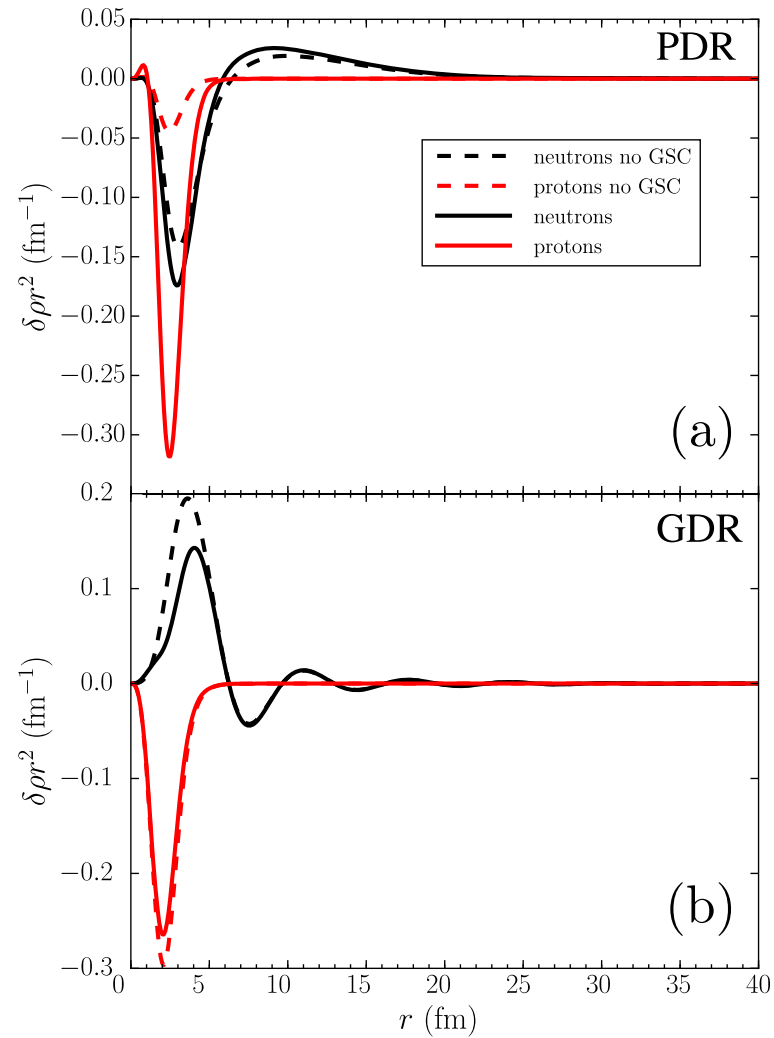
Barranco et al  
EPJ, A11 (2001) 305

$$|\tilde{0}\rangle_\nu = |0\rangle$$

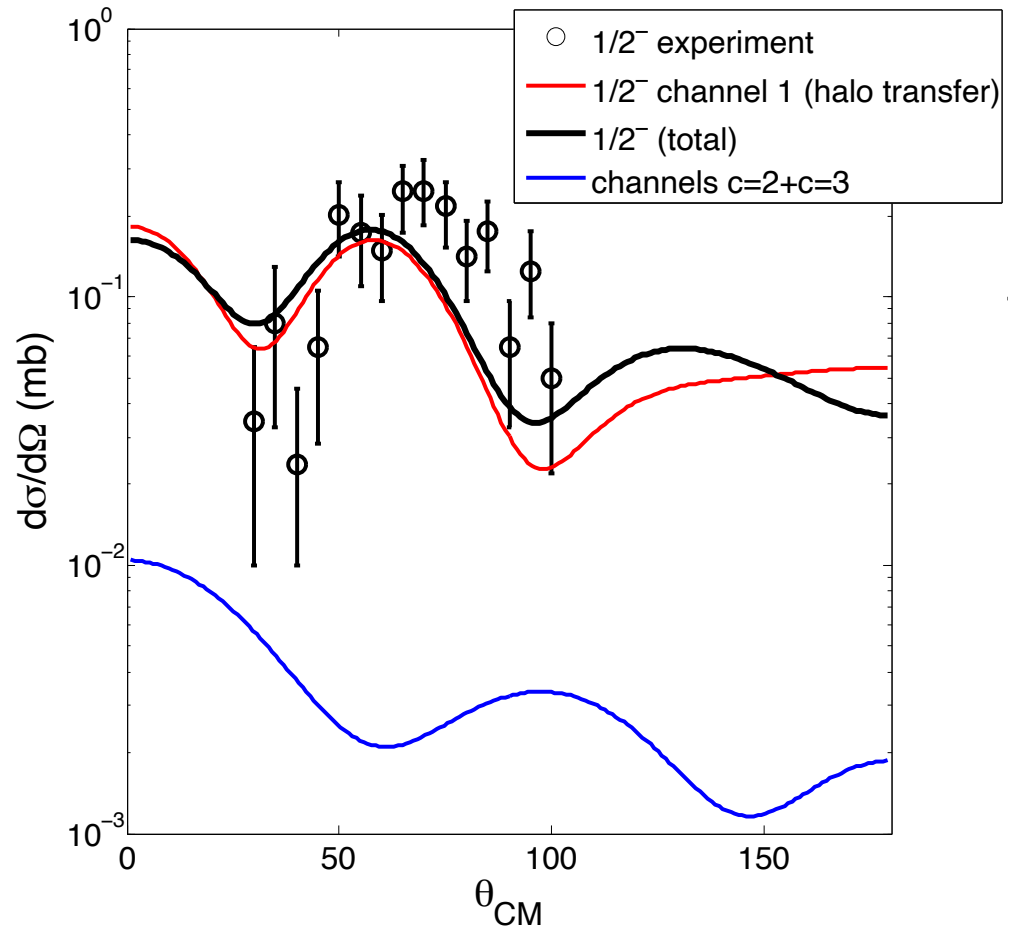
$$|0\rangle = 0.63|s^2_{1/2}(0)\rangle + 0.77|p^2_{1/2}(0)\rangle + 0.06|d^2_{5/2}(0)\rangle$$

$$N=1$$

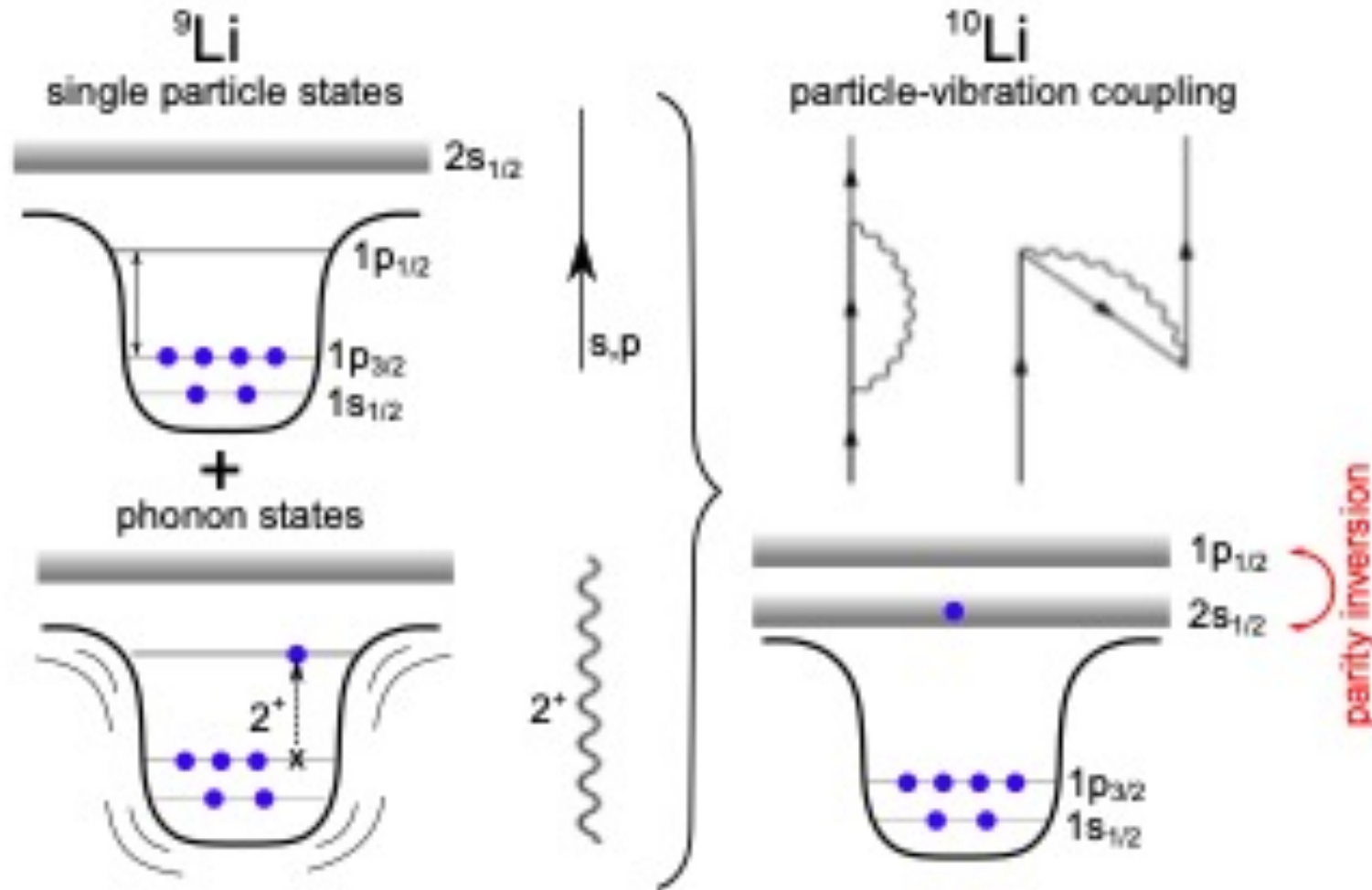
# Role of ground state correlations



# Transition to the first $1/2^-$ (2.69 MeV) excited state of ${}^9\text{Li}$



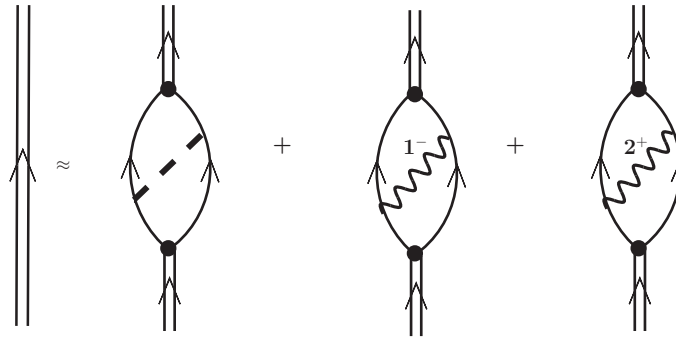
# From ${}^9\text{Li}$ to ${}^{10}\text{Li}$ ...





## ... and from $^{10}\text{Li}$ to $^{11}\text{Li}$

$^{11}\text{Li} = ^9\text{Li}$  core + 2-neutron halo (single Cooper pair). According to Barranco *et al.* (2001), the two neutrons correlate by means of the **bare interaction** (accounting for  $\approx 20\%$  of the  $^{11}\text{Li}$  binding energy) and by exchanging  $1^-$  and  $2^+$  **phonons** ( $\approx 80\%$  of the binding energy)

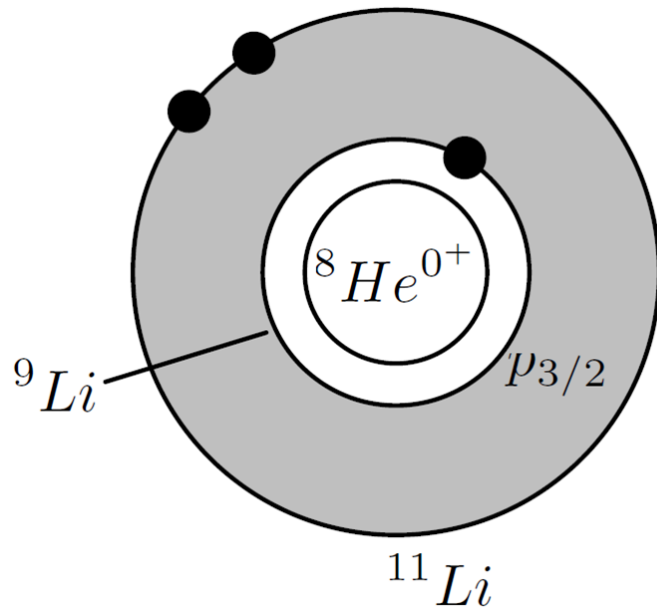


Within this model, the  $^{11}\text{Li}$  wavefunction can be written as

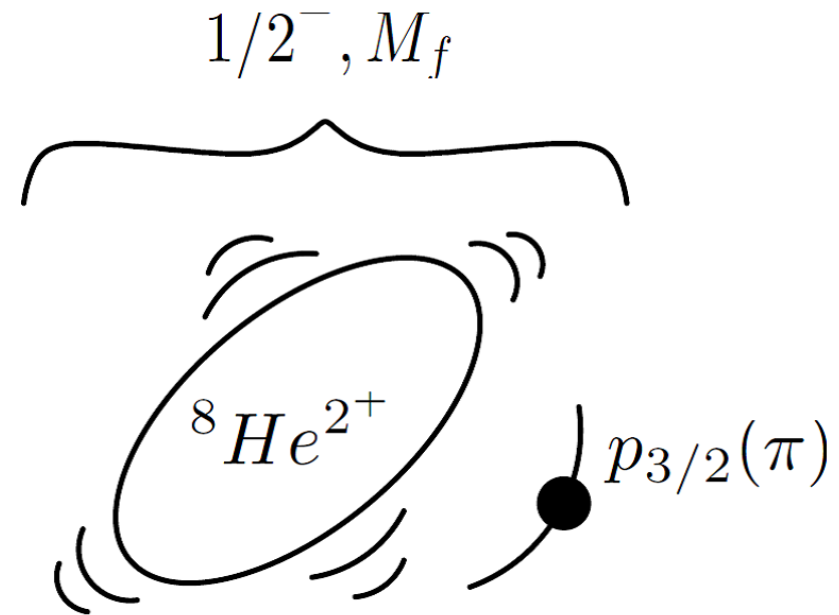
$$|\tilde{0}\rangle = 0.45|s_{1/2}^2(0)\rangle + 0.55|p_{1/2}^2(0)\rangle + 0.04|d_{5/2}^2(0)\rangle \\ + 0.70|(ps)_{1-} \otimes 1^-; 0\rangle + 0.10|(sd)_{2+} \otimes 2^+; 0\rangle.$$

Note that the  $p_{3/2}$  proton doesn't play any role and is not taken into account.

# $^{11}\text{Li}(p,t)^9\text{Li}(1/2^-)$



Schematic depiction of  $^{11}\text{Li}$



First excited state of  $^9\text{Li}$

# Spontaneous symmetry breaking in nuclei

