

# Charged Particle Emissions in High-Frequency Alternative Electric Fields

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# Reference

**Dong Bai, Daming Deng, and Zhongzhou Ren,**  
*Charged Particle Emissions in High-Frequency Alternative Electric Fields*, arXiv:1805.02379 (to appear on Nuclear Physics A)

# Outline

**1** Introduction

**2** Formalism

**3** Results

**4** Summary

# Charged Particle Emissions + ...

Charged particle emissions play an important role in nuclear physics.

- **$\alpha$  decay**: discovered in 1899; first application of Quantum Mechanics in nuclear physics;  
Phenomenological approach: density dependent cluster model, coupled channels method, etc;  
Microscopic approach: cluster-configuration shell model; quartetting wave function approach, etc.
- **Proton emission**: discovered in the 1960s.
- **Cluster radioactivity**: discovered in the 1980s.

$\alpha$  decay, proton emission, and cluster radioactivity could be described systematically using unified decay rules. (see, e.g., Ni, Ren, Dong, and Xu, 2008)

## ... + High-Frequency Alternative Electric Fields

Recently, a few works have been devoted to  $\alpha$  decays in strong electromagnetic fields, partially inspired by the upcoming powerful laser facilities in the near future.

- 1 D. P. Kis and R. Szilvasi, J. Phys. G **45**, 045103 (2018).
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- 3 S. Misicu and M. Rizea, Open Phys. **14**, 81 (2016).
- 4 I. V. Kopytin and A. S. Kornev, Phys. At. Nucl. **77**, 53 (2014).
- 5 S. Misicu and M. Rizea, J. Phys. G **40**, 095101 (2013).
- 6 H. M. Castañeda Cortes, etc, Phys. Lett. B **723**, 401 (2013).

In our work, we study charged particle emissions in high-frequency alternative electric fields. By “high frequency”, we mean the frequencies of alternative electric fields (photon energies  $\hbar\omega$ ) are much higher than the  $Q$  values of charged particle emissions, i.e.

- $\hbar\omega \gg Q_\alpha \sim 10$  MeV for  $\alpha$  decay,
- $\hbar\omega \gg Q_p \sim 1$  MeV for proton emission,
- $\hbar\omega \gg Q_c \sim 50$  MeV for cluster radioactivity.

High-frequency alternative electric fields correspond approximately to high-frequency laser fields in the **dipole approximation**. Our study could be viewed as a benchmark for future theoretical studies of charged particle emissions in realistic laser fields.

# Formalism

We start with the time-dependent Schrödinger equation

$$i\hbar \frac{\partial \Psi(\mathbf{r}, t)}{\partial t} = \left[ \frac{1}{2\mu} (\mathbf{P} - Q_{\text{eff}} \mathbf{A}(t))^2 + V(\mathbf{r}) \right] \Psi(\mathbf{r}, t), \quad (1)$$

with  $\mathbf{A}(t) = \mathbf{A}_0 \sin \omega t$  giving rise to the alternative electric field,  $\mu = M_c M_d / (M_c + M_d)$  being the reduced mass,  $Q_{\text{eff}} = eZ_{\text{eff}} = e(Z_c A_d - Z_d A_c) / (A_c + A_d)$  being the effective charge, and  $V(\mathbf{r})$  being the Coulomb potential.

# Hennenberger Transformation

By using the **Hennenberger transformation**

$$\Omega_h(t) = \exp \left[ \frac{i}{\hbar} \int_{-\infty}^t \left( -\frac{Q_{\text{eff}}}{\mu} \mathbf{A} \cdot \mathbf{P} + \frac{Q_{\text{eff}}^2}{2\mu} \mathbf{A}^2 \right) d\tau \right], \quad (2)$$

we could obtain a new equation for the new wave function

$$\Phi = \Omega_h(t)\Psi$$

$$i\hbar \frac{\partial \Phi(\mathbf{r}, t)}{\partial t} = \left[ \frac{1}{2\mu} \mathbf{P}^2 + V(\mathbf{r} - \mathbf{S}(t)) \right] \Phi(\mathbf{r}, t),$$

$$\mathbf{S}(t) = \frac{Q_{\text{eff}}}{\mu} \int_{-\infty}^t \mathbf{A}(\tau) d\tau. \quad (3)$$

$V(\mathbf{r} - \mathbf{S}(t))$  is known as the Hennenberger potential.  $\mathbf{S}(t)$  is known as the quiver displacement for the charged particle moving in alternative electric fields.



# High-Frequency Limit

- We can expand the Hennenberger potential  $V(\mathbf{r} - \mathbf{S}(t))$  in terms of Fourier series. It is well-established in theoretical laser-atom physics that, it is the static component that dominates over the rest Fourier components in the high-frequency limit.
- Explicitly, the static component is given by

$$V_0(\mathbf{r}) = \frac{1}{T} \int_0^T V(\mathbf{r} - \mathbf{S}(t)) dt. \quad (4)$$

In the following, we work with only the static component  $V_0(\mathbf{r})$ .

# Differential Penetrability

The differential and total penetrabilities are calculated by using the WKB approximation. The differential penetrability is given by

$$P(\Theta, \theta_\lambda) = \exp \left( -2 \int_{R_t(\theta_\lambda)}^{R(\Theta)} \sqrt{\frac{2\mu}{\hbar^2} [U(r) - Q]} dr \right), \quad (5)$$

$$U(r) = \frac{\hbar^2}{2\mu r^2} L(L+1) + V_0(r, \Theta, \theta_\lambda, S_0). \quad (6)$$

$\Theta$  is the angle between  $\mathbf{r}$  and  $\mathbf{S}(x)$ . Here, we consider the possibility of the cluster or daughter nucleus to be axially deformed.  $\theta_\lambda$  measures the angle between  $\mathbf{r}$  and the symmetric axis of the deformed nucleus.

# Total Penetrability

The total penetrability could be estimated by

$$P = \frac{1}{4} \int_0^\pi d\theta_\lambda \sin \theta_\lambda \int_0^\pi d\Theta \sin \Theta P(\Theta, \theta_\lambda). \quad (7)$$

# Results

- We present numerical results concerning the impacts of high-frequency alternative electric fields on **proton emission**,  **$\alpha$  decay**, and **cluster radioactivity**.
- Adimensional parameter  $D$ :

$$D = S_0/R_{d0} \propto \frac{Z_{\text{eff}} \sqrt{I}}{\mu R_{d0} \omega^2}, \quad (8)$$

with  $S_0$  the quiver amplitude,  $R_{d0}$  the average radius of the daughter nucleus,  $Z_{\text{eff}}$  the effective charge,  $\mu$  the reduced mass,  $I$  the intensity of the electric field, and  $\omega$  the frequency.

# Anisotropic Effects

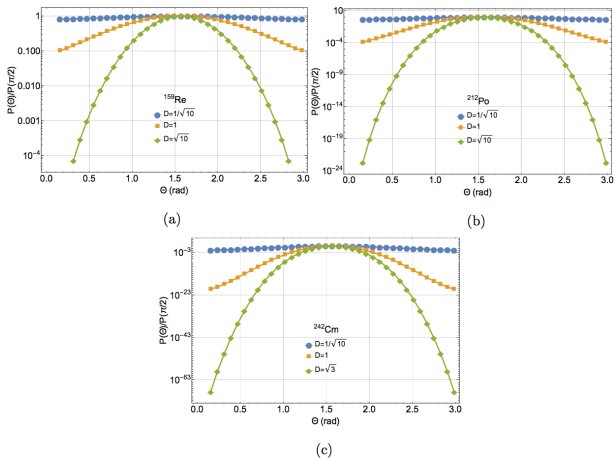


FIG. 1: Differential barrier penetrability normalized to its maximal value at  $\Theta = \pi/2$  with different values of  $D$  for (a) the proton emitter  $^{159}\text{Re}$  with the orbital angular momentum  $L = 5$ , (b) the  $\alpha$  emitter  $^{212}\text{Po}$ , and (c) the  $^{34}\text{Si}$  emitter  $^{242}\text{Cm}$ .

# Total penetrability versus $D$

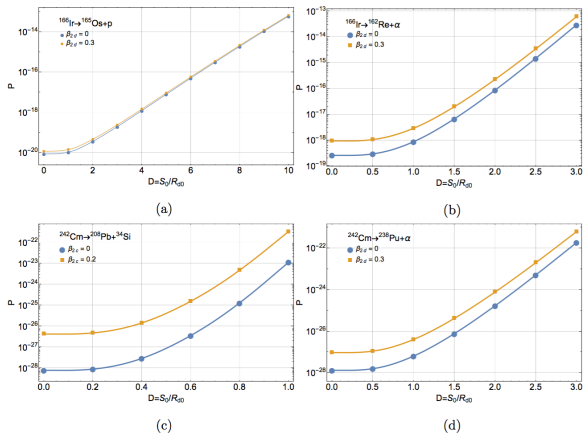


FIG. 2: Total penetrability versus  $D = S_0/R_{d0}$  with different assumptions on their deformations for (a) the proton-emission channel of  $^{166}\text{Ir}$  with the orbital angular momentum given by  $L = 2$ , (b) the  $\alpha$ -decay channel of  $^{166}\text{Ir}$ , (c) the  $^{34}\text{Si}$ -radioactivity channel of  $^{242}\text{Cm}$ , and (d) the  $\alpha$ -decay channel of  $^{242}\text{Cm}$ .

# Shifted Geiger-Nuttall Law

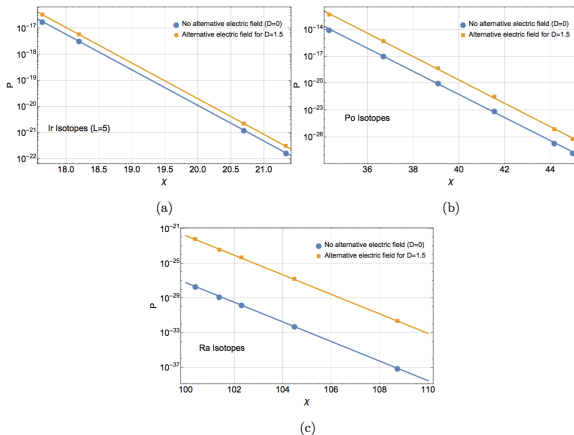


FIG. 3: Total penetrability versus the Coulomb-Sommerfeld parameter  $\chi$  for (a) Ir isotopes as proton emitters, (b) Po isotopes as  $\alpha$  emitters, and (c) Ra isotope as  $^{14}\text{C}$  emitters in the absence of alternative electric fields ( $D = 0$ ) and in the presence of alternative electric fields with  $D = 1.5$ .

# Competition Between Decay Modes

We also study the competitions between different decay modes.

## ■ $\alpha$ decay vs proton emission:

For  $^{166}\text{Ir}$ , the branching ratios of the  $\alpha$ -decay and proton-emission channels being 93% and 7%, respectively. When switching on strong high-frequency electric fields, the  $D$  values for these two decay channels satisfy approximately  $D_p/D_\alpha \sim 15$ . Take  $D_\alpha \approx 0.5$ . When put in such strong high-frequency alternative electric fields, the total penetrability of the  $\alpha$ -decay channel of  $^{166}\text{Ir}$  remains roughly to be at the same orders of magnitude, while for the proton-emission channel we have  $D_p \approx 7.5$ , corresponding to the total penetrability being enhanced by about five orders of magnitude. The results here indicate that, when  $^{166}\text{Ir}$  is placed in strong high-frequency alternative electric fields, its dominant decay mode may be changed from  $\alpha$  decay to proton emission.



■  **$\alpha$  decay vs cluster radioactivity:**

For  $^{242}\text{Cm}$ , the  $D$  values for the  $^{34}\text{Si}$ -radioactivity and  $\alpha$ -decay channel satisfy  $D_c/D_\alpha \sim 0.17$ . Take  $D_\alpha \approx 3$ . The total penetrability of the  $\alpha$ -decay channel is increased by about five orders of magnitude.

Correspondingly,  $D_c \approx 0.5$ , and the total penetrability of the  $^{34}\text{Si}$ -radioactivity channel is enhanced by a factor less than one order of magnitude. Therefore, the  $^{34}\text{Si}$ -radioactivity channel becomes even more suppressed in the presence of strong high-frequency alternative electric fields.

# Summary

In this work, we study charged particle emissions in high-frequency alternative electric fields, including

- anisotropic effects induced by high-frequency alternative electric fields,
- the relation between total penetrabilities and the  $D$  values,
- shifted Geiger-Nuttall laws,
- competition between different decay modes.

As high-frequency alternative electric fields correspond to high-frequency laser fields in the dipole approximation, our study could be viewed as a benchmark for future theoretical studies.

# Thanks!