NZ equilibration in two and three bodies dynamically deformed nuclear systems
($^{70}$Zn$^+$ $^{70}$Zn @ 35 MeV/nucleon)

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Systems studied: $^{70}\text{Zn} + ^{70}\text{Zn}$ at 35 MeV per nucleon using NIMROD
Velocity gradient and surface tension amplifies instabilities
- Simultaneous or double rupture?
- 3F separated first?
- Fragments aligned? String of pearls?
- Fragments aligned with the Vcm vector?
Time-dependence of NZ equilibration examining composition of HF-LF emitted from PLF* vs the breakup alignment angle (serves as clock for equilibration)

Variation of composition vs alignment angle shows exponential behavior for LF & HF, suggesting 1st-order kinetics, for all systems studied

Yield and measured composition, used to extract an estimate for purely dynamical component

Small systematic effects in composition for reactions of relatively n-poor projectile with n-rich target

No significant differences in rate cts between systems of different initial composition

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Symmetrize Dalitz plot

2Z’s are approximately equal
1Z is different (and bigger)
Velocity distributions of HF, LF and 3F

- Dashed lines = beam velocity (i.e. 0.27c) and mid-velocity (i.e. 0.13c).
- The three of them peaked above mid-velocity (indicating that HF, LF and 3F originate from the PLF*).
- LF (3F) produced at velocities > than mid-velocity and < than the HF (LF). HF produced closer to beam velocity.

Hierarchy in the velocity distributions (correlated to the charge sorting):

HF forward from LF, and both are forward respect to 3F.
Rupture scenarios:

Who is separating first?

Example of the rupture scenario where $Z_3$ separates first

First rupture

Second rupture
Rupture scenarios: Angular distributions

- Statistical contribution (color hatches)
- ZH forward from ZL, and both forward from Z3
- Peak in the angular yield when Z3 and ZL separate first
- When ZH separates first, the dynamical contribution seems to be smaller that when Z3 or ZL separate first
Rupture scenarios: correlations between the angles of both breakings

Another way to show the angular correlation

More dyn-dyn and dyn-stad combinations

More stad-dyn combinations

More dyn-dyn and stad-dyn combinations

Preliminary

Looks like HF is not separating first
Angles between the relatives velocities &
Angle between the projections of HF, LF and 3F velocities, in a plane perpendicular to Vcm

Cartoon of a plane perpendicular to Vcm and a plane formed by the three fragments

asymmetric angular projection
plane perpendicular to Vcm
+
symmetric angles on the relatives velocity plane of the 3 fragments

Plane perpendicular to Vcm
Plane of the relatives velocities
Angles between the projections of HF, LF and 3F velocities, in a plane perpendicular to Vcm

The majority of events populate combinations of (180°,0°,180°)

→ Two fragments are closer to each other, and apart from the other one.
Angles between the relatives velocities

Plane of the relatives velocities

VrelHF3F
VrelHFLF
VrelLF3F

Plane formed by the 3 fragments

It looks like red, blue and green angles are similar (slightly following $r > b > g$)
Two fragments seemingly closer to each other and apart from the third one

Combining both:
. Relative velocities’ plane is oblique to Vcm
. The three fragments don’t seem to be aligned

The three angles are approximately similar
The angular momentum is controlling the rupture, because it is occurring in preferential planes.

The rotation is perpendicular to the direction of the movement.

The system breaks due to rotation and in a double rupture, where the plane of the Vrels is the plane perpendicular to the angular momentum, (very oblique to Vcm)
Comparison to Boltzmann-Langevin One Body (BLOB):

Something else we want to explore...

BLOB calculation:
Violent nuclear reaction dynamics, neck fragmentation

Dynamical transport model

Unifies in a common approach the description of fluctuations in nuclear matter, and a predictive description of the disintegration of nuclei into nuclear fragments

Characterize the very fast early stages of the collision process which are out of equilibrium

Sizable neck fragments

work in progress

70Zn+70Zn 35AMeV (b=5.7) producing 45Ca, 40Cl, 6Li,d (at 400fm/c)

https://www.youtube.com/watch?v=l5ul-iux1ik
Paolo Napolitani

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Summary

Studied **time dependence of the NZ equilibration**, examining composition of fragments from the PLF* vs angle (serves as clock for the equilibration). Composition follows exponential behavior suggesting **first-order kinetics**. We extracted a purely **dynamical composition component**, found **target effects** and no significant differences in rate constants among HF-LF or different systems.

- Hierarchy in the velocity distributions (strongly correlated to the charge sorting)
- Sizes: one big, two smaller and similar.
- The relative velocities’ plane is oblique to Vcm and the three fragments don’t seem to be aligned.

**The physics is dominated by the angular momentum, so the system breaks due to rotation and in a double rupture scenario.**

**Comparing with dynamical transport models (BLOB), with sizable neck fragments**
Thank you!

SJY group and collaborators:


Department of Energy
DE-FG02-93ER40773

Welch Foundation
A-1266
Backup Slides
Neutron Ion Multidetector for Reaction Oriented Dynamics (NIMROD)

Multidetector array for reactions between massive target and projectiles:
- Total of 228 detector modules arranged in 14 annular rings (2-3 detectors/module)
- Projectile energies go from 20MeV to 4GeV
- $4\pi$ coverage (3.6° to 167.0°) = nearly complete geometrical coverage
- excellent isotopic ID
Angular (α) distributions:

- Lifetime of PLF* correlated with rotation angle:
  \[ \alpha = \arccos\left(\frac{\vec{v}_{cm} \cdot \vec{v}_{rel}}{|\vec{v}_{cm}| \cdot |\vec{v}_{rel}|}\right) \]

- Angular distribution peaked for most aligned configuration. Decreases in yield with decreasing alignment.

- Excess yield largest and most strongly aligned for most asymmetric splits.

- Less aligned decays represent longer decay times.

\[ Y_T = Y_d + Y_s \]

- Dynamical yield dominates at small angles and decreases as α increases.
ΔObservable = f_sΔS + f_dΔd

• As angle of rotation increases, ΔHF (ΔLF) start off very n-poor (n-rich), then evolve towards each other.

• Exponential fit: \( a + b e^{-c(\alpha)} \)
  - \( a \) = equilibrium value
  - \( c \) = rate constant for equilibration

• First-order kinetics.

• Dynamical composition generally follows the same trend as the overall composition (more extreme).

• Rate of change of the composition unaffected by correction

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Composition vs decay alignment: for different systems

- $\Delta/\alpha$ ($^{70}\text{Zn}$, $^{64}\text{Ni}$) correlations essentially the same.

- $\Delta/\alpha$ ($^{64}\text{Zn}$) correlation shifted to lower values (i.e. lower equilibrium composition). Same rate constants and change from initial to final value.

Comparing the symmetric and the asymmetric systems:

- $\Delta/\alpha$ correlations for the symmetric system are systematically lower $\rightarrow$ target effects.
Equilibrium composition

\[ \langle \Delta \rangle = a + b e^{-c(\alpha)} \]

- \( Z_L, Z_H \) values fairly clustered \( \rightarrow \) equilibrium value for LF (HF) depends on \( Z_L \) (\( Z_H \)) but not on \( Z_H \) (\( Z_L \)).

- Comparing \( ^{70}\text{Zn} \) (\( \square \)) and \( ^{64}\text{Ni} \) (\( \star \)) systems (similar n-rich system composition): ~ same equilibrium composition.

- \( ^{64}\text{Zn} \) (\( \bullet \)): consistently less n-rich equilibrium compositions

- The asymmetric \( ^{64}\text{Zn} + ^{64}\text{Ni} \) system (\( \bigtriangleup \)): slightly + n-rich daughters than the n-poor syst. slightly - n-rich daughters than the n-rich syst.

\[ \rightarrow \text{target effect} \]
Rate constant for equilibration:

\[ <\Delta> = a + b \ e^{-c(\alpha)} \]

- Exponential slope

- Average rate constant zs\(^{-1}\):
  - LF \(4 \pm 1\)
  - HF \(4 \pm 2\)

- Relevant parameter to calculate the equilibration times.

- Describes how fast the equilibration occurs within the PLF*.

- Agreement of rates \(\rightarrow\) force driving the equilibration is independent of the size of both partners only depends on the difference in asymmetry.
Angular ($\alpha$, $\varphi_{\text{in}}$ and $\Theta_{\text{out}}$) distributions: why $\alpha$?

- Consistent with a significant amount of dynamical decay.

- Statistical decay $\alpha$ and $\varphi_{\text{in}}$:
  Symmetric distribution about $90^\circ$ ~ sinusoidal for low spin
  Squashed out symmetrically toward edges as spin increases.

- Distributions strongly peaked toward $0^\circ$ and asymmetric
  $\rightarrow$ large yield of non-statistical decay.

- The distributions:
  $\varphi_{\text{in}}$ ($\Theta_{\text{out}}$ near $70^\circ$ or $110^\circ$) looks like the total $\varphi_{\text{in}}$
  $\varphi_{\text{in}}$ ($\Theta_{\text{out}}$ near $30^\circ$ or $150^\circ$) looks much flatter.
  $\downarrow$
  dynamical yield is preferentially closer to the plane.

  $\varphi_{\text{in}}$ angle should describe the deformation alignment in a similar manner as it does the $\alpha$ angle.
Composition vs decay alignment, for $\alpha$, $\phi_{in}$:

- Rotation of the PLF* as it decays into HF and LF is predominantly around an axis perpendicular to the RP.

- Composition as a function of these two angles expected to be similar.

- Rotation axis can be canted from perpendicular, we expect that $\alpha$ would provide a truer measure of the time.
Secondary decay (SD):

using GEMINI++
open markers: $\langle \Delta \rangle$ of the final state fragments

Varying the initial excitation energy:
• In both cases ( ), exponential dependence maintained.
• Shift to lower composition and muting of the amplitude (stronger for higher excitation energy)

Varying the starting $\langle \Delta \rangle$:
• System with initially larger asymmetry shifted down strongly by SD. (System farther from valley of stability feels a stronger force driving it back toward the valley)
• After SD, the more n-rich system remains more n-rich.

The trend is not destroyed or created, and the characteristic rate of the exponential is retained.
Average rate constant degree$^{-1}$:

**Symmetric systems:**
- LF 0.03 ± 0.01
- HF 0.02 ± 0.01

**Asymmetric system:**
- LF 0.02 ± 0.01
- HF 0.01 ± 0.02

- Relevant parameter to calculate the equilibration times.
- Describes how fast the equilibration occurs within the PLF$^*$.  

- Agreement of rates → force driving the equilibration is independent of the size of both partners only depends on the difference in asymmetry
Time-Scale

\[ t = \frac{\alpha}{\omega} \quad \text{where} \quad \omega = \frac{J\hbar}{I_{\text{eff}}} \]

\( \omega \) (angular frequency), 
\( J \) (angular momentum)

- The \( J \) is determined using the width of the out-of-plane \( \alpha \) particle distribution.

- GEMINI++ simulations: reproducing this width can be done with spin from \( 10\hbar \) (\( E^*/A=0.8\text{MeV} \)) to \( 50\hbar \) (\( E^*/A=1.2\text{MeV} \)). We can take \( J=22\hbar \) with a factor of 2.2 uncertainty.

- Moment of inertia is calculated using a 2 touching spheres model:
  \[ I_{\text{eff}} = m_{ZH}r_{CM,ZH}^2 + \frac{2}{5}m_{ZH}r_{ZH}^2 + m_{ZL}r_{CM,ZL}^2 + \frac{2}{5}m_{ZL}r_{ZL}^2 \]

- Using a complete rotational period:
  \[ t = (1-4) \text{ zs} \]