Links between the liquid-gas and
deconfinement-hadronization phase transitions

I.N. Mishustin

Frankfurt Institute for Advanced Studies, J.W. Goethe Universität,
Max-von-Laue Str. 1, D-60438 Frankfurt am Main, Germany
Kurchatov Institute, Russian Research Center, Kurchatov Sq. 1, 123182 Moscow, Russia

Abstract

According to present understanding, strongly interacting matter has several
phase transitions in different domains of the temperature-baryon density plane.
One of them, the liquid-gas phase transition, is well established theoretically and
studied experimentally in nuclear multifragmentation reactions at intermediate en-
ergies. The other one, the deconfinement phase transition, is at the focus of present
experimental studies with relativistic heavy-ion beams at SPS and RHIC. We dis-
cuss possible links between these two phase transitions from the viewpoint of their
experimental identification in violent nuclear collisions.

1 General remarks

A general goal of present and future experiments with heavy-ion beams is to study the
properties of strongly interacting matter away from the nuclear ground state. The main
interest is focused on searching for possible phase transitions in such matter. Several
phases are predicted in different domains of temperature $T$—baryon density $\rho_B$ plane.
As well known, strongly interacting matter has at least one multi-baryon bound state
at $\rho_B = \rho_0 \approx 0.16 \text{ fm}^{-3}$ and binding energy of about 10 MeV, corresponding to normal
nuclei. This means that the equation of state of symmetric nuclear matter has a zero-
pressure point at $\rho_B = \rho_0$. Since the pressure should also vanish at $\rho_B \to 0$, it must be
a non-monotonic function of $\rho_B$, i. e. $\partial P / \partial \rho_B < 0$ in a certain density interval. This
condition signals instability of matter with respect to growing density perturbations, a
characteristic feature of the liquid-gas phase transition. Therefore, it follows from the
very existence of the nuclear bound state that there should be a first order phase transition
of the liquid-gas type in normal nuclear matter at subsaturation densities, $\rho_B < \rho_0$, and
low temperatures, $T \leq 10 \text{ MeV}$.

The nuclear liquid-gas phase transition manifests itself most clearly in a remarkable
phenomenon known as nuclear multifragmentation, observed in intermediate-energy nu-
clear reactions. Here we mention only a few guiding ideas which helped to identify this
phase transition. The first one is the anomaly (plateau) in the caloric curve, which was
first predicted theoretically [1] and later on found experimentally [2]. More recently, an
interesting proposal was made [3, 4] to look for anomalous energy fluctuations in the
multifragmentation events, which might be a good signal of a first order phase transition
in finite systems. Another productive idea proposed in ref. [5] was to search for residual
signals of the spinodal decomposition expected in connection with a liquid-gas phase transition. Such a signal, although small, was indeed found experimentally as an enhanced emission of equal-size fragments [6]. Other evidences for the liquid-gas phase transition include large multiplicity fluctuations and bimodality [7, 8], critical behavior [8, 9, 10] near the critical point etc.

The situation at high $T$ and nonzero baryon chemical potential $\mu_B (\rho_B > 0)$ is not so clear, although everybody is sure that the deconfinement and chiral transitions should occur somewhere. It is expected that the Quark-Gluon Plasma (QGP) is formed at high enough $T$ and $\rho_B$. A rigorous theoretical background for these studies is provided by the QCD based numerical simulations on a lattice. However, at present reliable lattice calculations exist only for $\mu = 0$ i.e. $\rho_B = 0$ where they predict a smooth deconfinement transition (crossover) at $T \approx 170$ MeV [11]. As model calculations show, the phase diagram in the $(T, \mu_B)$ plane may contain a first order transition line (below called the critical line) which ends at a (tri)critical point [12, 13, 14]. Unfortunately, at finite $\mu$ the lattice calculations suffer from the so called "sign problem" and cannot be done easily. Different approximation schemes lead to differing predictions concerning the existence of a critical point (see e.g. refs. [15, 16, 17]). Possible signatures of this point in heavy-ion collisions were discussed in ref. [18]. However, it is unclear at present whether critical fluctuations associated with the second order phase transition can develop in a rapidly expanding system produced in a relativistic heavy-ion collision, because of the critical slowing down effect [19]. In our opinion, more promising strategy would be to search for a first order phase transition which should have much more spectacular manifestations, which we discuss below.

Relative to the liquid-gas transition, the exploration of the QCD phase diagram is considerably more challenging. On the theoretical side, we have no tractable models to relay on to predict how the phase diagram looks in the $T-\mu$ plane, nor where the dynamical trajectories will go. Since, by the nature of a phase transition, the effective degrees of freedom are different in the two phases, often two different models are applied below and above the critical line. On the other hand, the lattice QCD can only be applied to the systems in statistical equilibrium, i.e. it cannot be be used for dynamical simulations in real time. With regard to dynamical models, the best candidate is perhaps fluid dynamics which needs no specific information about the structure of the matter but merely needs macroscopic quantities such as the equation of state and kinetic coefficients. However, in its standard form this model is unsuitable for studies of unstable situations associated with a first order phase transition. Thus, it is very difficult to provide the experimentalists with a quantitative guidance ensuring that the parameters of the experiments are those where the phase transition signals are best seen.

On the experimental side, the exploration of the QCD phase structure is made extra complicated by the fact that only the hadronic phase survives (apart from electromagnetic probes), in contrast to the nuclear liquid-gas transition where both phases occur in the final state: the liquid in the form of heavy and intermediate-mass fragments, and the gas in the form of nucleons and light clusters. Therefore, it is important to use experience accumulated in the liquid-gas phase transition studies for designing the analysis techniques
for the exploration of the deconfinement-hadronization phase transition. For this reasons alone, it would be desirable to pursue further the liquid-gas transition studies.

A similarity between the liquid-gas phase transition and the hadronization process is the presence of more than one conserved charge: At low energy we have electric charge \(Z\) in addition to mass number \(A\), while at high energy, in addition to baryon number \(B\) (which is identical to \(A\)) and electric charge \(Q\) (which corresponds to \(Z\)), we have also strangeness \(S\). Therefore, the lessons learned at low energy regarding multicomponent systems may be very helpful to the QGP studies too.

Finally, notwithstanding the large uncertainty with regard to the value of the critical baryon density (above which the deconfinement transition is of first order), it appears likely that the first-order transition can best be studied experimentally in the region of moderate bombarding energies where compressed matter is characterized by a considerable net baryon density. As we know now, a strongly interacting matter produced at RHIC, presumably a hot quark-gluon plasma, has practically vanishing net baryon density [20]. While more suitable conditions may well have been achieved already at SPS, those data have not been analyzed in a way which would unambiguously demonstrate the QGP formation. The most promising facility for the future is the planned FAIR at GSI, where compressed baryonic matter is one of the prime areas of intended research. From this perspective, there is a natural evolution from nuclear multifragmentation reactions, where a certain degree of initial compression is needed to ensure the subsequent dilution that will bring the bulk matter into the region of spinodal instability: If a (considerably) larger degree of compression is achieved, then the system may be brought into the region of coexistence between baryon-rich hadronic matter and baryon-rich deconfined plasma.

A striking feature of central heavy-ion collisions at high energies, confirmed in many experiments (see e.g. [21, 22]), is a very strong collective expansion of matter at later stages of the reaction. This process looks like an explosion with the matter flow velocities comparable with the speed of light. The applicability of equilibrium concepts for describing phase transitions under such conditions becomes questionable and one should expect strong non-equilibrium effects. Below we demonstrate that non-equilibrium phase transitions in rapidly expanding matter can lead to interesting phenomena which, in a certain sense, are even easier to observe.

## 2 Dynamical fragmentation of a metastable phase

### 2.1 Nuclear liquid-gas transition

Instead of going into complicated transport calculations let us consider a simple model showing how the collective flow can modify the conventional picture of a first order phase transition [23]. Let us consider first the liquid-gas transition in nuclear matter. We assume that a system expands uniformly with the collective velocity field of a Hubble type, \(v_j(r) = H r\), where \(H\) is an appropriate Hubble constant. The expansion acts against the attractive forces which keep the nucleons together at normal density. Therefore, instead of uniformly expanding the whole system it is energetically more favorable to split it into
droplets which preserve a sufficiently high density inside, to keep attractive forces acting, and recede from each other according to the Hubble law. The space between the droplets is almost empty so that the energy cost for producing such an inhomogeneous state may be estimated as an extra interface area times a surface tension coefficient \( \sigma \). One should expect that in violent reactions where a thermal excitation is high, \( \sigma \) might be significantly reduced compared to the value of about 1 MeV/fm\(^2\) known for cold nuclei. The shape of the droplets, which is determined by the local density fluctuations, might be also quite complicated. But for our order-of-magnitude estimates we assume that the system splits into more or less spherical droplets of a similar size.

Now let us imagine that at the stage of the break-up the expanding system is represented by the collection of droplets (nuclear fragments) separated by fully developed surfaces. In leptonemous approximation the total energy of an individual spherical droplet of radius \( R = (3A/4\pi\rho_B)^{1/3} \) can be decomposed as

\[
E = E_{\text{bulk}} + E_{\text{kin}} + E_{\text{sur}}.
\]

Here the bulk term at \( \rho_B \neq \rho_0 \) can be written as

\[
E_{\text{bulk}} = \left[ a_V + \frac{K}{2} \left( 1 - \frac{\rho_B}{\rho_0} \right)^2 \right] \cdot A,
\]

where \( a_V \) is the bulk coefficient in the Weizsäcker formula and \( K \) is the incompressibility modulus. The kinetic energy of an individual droplet, associated with its collective expansion with respect to the center of mass, is easily calculated,

\[
E_{\text{kin}} = \int_0^R \frac{1}{2} m_N v_f^2(r) \rho(r) 4\pi r^2 dr = \frac{2\pi}{5} m_N H^2 \rho R^5,
\]

where \( m_N \) is the nucleon mass. The surface energy of a droplet is \( 4\pi R^2 \sigma \). It is worth noting that the collective kinetic energy acts here as an effective long-range potential similar to the Coulomb potential in nuclei.

To find the optimal droplet size one can apply the Grady’s argument [24] that the redistribution of matter is a local process minimizing the energy per droplet volume, \( \Delta E/V \). Then, since the bulk contribution does not depend on \( R \), the minimization condition constitutes the balance between the collective kinetic energy and interface energy. This gives

\[
\overline{A} = \frac{4\pi}{3} \rho R^3 = \frac{20\pi}{3} \frac{\sigma}{m_N H^2}.
\]

It is determined by only two parameters: surface tension \( \sigma \) and Hubble constant \( H \). The latter one can be estimated from flow observables. For instance, in central Au + Au collisions at 150, 250 and 400 MeV/nucleon the measured flow velocities \( v_f \) are 0.20c, 0.26c and 0.34c respectively [21]. Now one can estimate the Hubble constant as \( H^{-1} = R_{\text{ref}}/v_f \), which gives 35, 26 and 20 fm/c, respectively. To get the mean fragment mass \( \overline{A} \approx 3 \), as seen in experiment, one should take in eq. (4) \( \sigma \approx 0.2 \text{ MeV/fm}^2 \).
that is by about factor 5 smaller than in cold nuclei! May be this is not surprising because at a “temperature” 17 MeV, obtained for this reaction, $\sigma$ would already vanish in a thermodynamically equilibrium system. One should bear in mind, however, that the observed cold fragments are produced from hot primary fragments after their de-excitation. Therefore, primary fragments produced at the break-up stage should be bigger.

Knowing $\overline{A}$, one can use the minimum information principle [25, 26] to determine the inclusive fragment mass distribution $P(A)$. Let us impose a normalization condition, $\sum_A P(A) = 1$, and assume that the mean fragment mass, $\overline{A} = \sum_A A P(A)$, is fixed. Now one can define the information function as $\sum_A P(A) \ln P(A)$ and find $P(A)$ by minimizing it under the above constraints. The result is

$$P(A) = \frac{1}{\overline{A}} \exp \left( -\frac{A}{\overline{A}} \right). \quad (5)$$

This kind of mass distributions has been obtained in numerical simulations [27] as well as in the free-jet fragmentation experiments [26] It is remarkable that exactly this type of mass (charge) distributions is also observed in nuclear experiments! For instance, exponential fragment charge distributions have been found in central Au + Au collisions at 150, 250 and 400 MeV/nucleon [21] discussed above. By applying naively the statistical approach to these reactions one gets much too steep charge distributions (smaller $\overline{A}$), i.e. a smaller number of IMF’s.

2.2 Deconfinement-hadronization transition

A similar scenario may also be plausible for the deconfinement-hadronization phase transition in relativistic nuclear collisions [28, 29]. The difference will be mainly in the parameters characterizing this phase transition. Let us assume that the dynamical fragmentation of the deconfined (Q) phase results in a collection of QGP droplets embedded in a dilute hadronic (H) phase, as illustrated in fig. 1. The optimal droplet size can be determined by applying the same energy balance prescription discussed above. The only difference is that the droplet mass with respect to the hadronic background is now calculated as $M = \Delta \mathcal{E} V$, where $\Delta \mathcal{E} = \mathcal{E}_Q - \mathcal{E}_H$ is the energy density difference of Q and H bulk phases, and $V$ is the volume of the droplet. Applying the Grady’s minimization rule we get the optimum droplet radius

$$R^* = \left( \frac{5\sigma}{\Delta \mathcal{E} H^2} \right)^{1/3}. \quad (6)$$

As Eq. (6) indicates, the droplet size depends strongly on $H$. When expansion is slow (small $H$) the droplets are big. Ultimately, the process may look like a fission of a cloud of plasma. But fast expansion should lead to very small droplets. This state of matter is very far from thermodynamical equilibrium, particularly because the H phase is very dilute. One can say that the metastable Q matter is torn apart by a mechanical strain associated with the collective expansion. This has a direct analogy with the dynamical multifragmentation described in the previous section or with the fragmentation of pressurized fluids leaving nozzles [26].
Figure 1: Schematic view of multi-droplet state produced after the dynamical fragmentation of a metastable high energy-density phase (in this example, the Q phase). The droplets are embedded in the low energy-density phase (in this example, the H phase). Each droplet expands individually as well as participates in the overall Hubble-like expansion.

At ultrarelativistic collision energies associated with RHIC and LHC experiments, the expansion of partonic matter will be very anisotropic with its strongest component along the beam direction [30]. Clear indications of such an anisotropy are seen already at SPS energies (see [22]). It is natural to think that in this case the inhomogeneities associated with the phase transition will rearrange into pancake-like slabs of Q matter embedded in a dilute H phase. The characteristic width of the slab, 2L, can be estimated in a similar way and the resulting expression for Lʰ differs from Eq. (6) only by a geometrical factor (3 instead of 5 in parentheses). Generally, the faster the expansion, the smaller are the fractures. Of course, at a later time the Q droplets will further fragment in the transverse direction due to the transverse expansion.

The driving force for expansion is the pressure gradient, \( \nabla P = \frac{\rho^2}{a^2} \nabla \varepsilon \), which depends crucially on the sound velocity in the matter, \( c_s \). Here we are interested in the expansion rate of the partonic phase which is not directly observable. In the vicinity of the phase transition, one may expect a “soft point” [31, 32] where the sound velocity is smallest and the ability of matter to generate the collective expansion is minimal. If the initial state of the Q phase is close to this point, its subsequent expansion will be slow. Accordingly, the droplets produced in this case will be big. When moving away from the soft point, one would see smaller and smaller droplets. For numerical estimates we choose two values of the Hubble constant: \( H^{-1}=20 \text{ fm}/c \) to represent the slow expansion from the soft point and \( H^{-1}=6 \text{ fm}/c \) for the fast expansion.

One should also specify two other parameters, \( \sigma \) and \( \Delta \varepsilon \). The surface tension \( \sigma \) is
a subject of debate at present. Lattice simulations indicate that at the critical point it could be as low as a few MeV/fm². However, for our non-equilibrium scenario, more appropriate values are closer to 10-20 MeV/fm² which follow from effective chiral models. As a compromise, the value $\sigma = 10$ MeV/fm² is used below for rough estimates. Bearing in mind that nucleons and heavy mesons are the smallest droplets of the Q phase, one can take $\Delta \varepsilon = 0.5$ GeV/fm³, i.e. the energy density inside the nucleon. Then one gets $R^* = 3.4$ fm for $H^{-1} = 20$ fm/c and $R^* = 1.5$ fm for $H^{-1} = 6$ fm/c. As follows from eq. (6), for a spherical droplet $V \propto 1/\Delta \varepsilon$, and in the first approximation its mass,

$$M^* \approx \Delta \varepsilon V = \frac{20\pi}{3} \frac{\sigma}{H^2},$$  

(7)

is independent of $\Delta \varepsilon$ (compare with eq. (4). For two values of $R^*$ given above the mass is $\sim 100$ GeV and $\sim 10$ GeV, respectively. The pancake-like droplets could be heavier due to their larger transverse size. As mentioned in the previous section, the distribution of droplet masses should follow an exponential law, exp $\ (-\frac{M}{M^*})$. Thus, about $2/3$ of droplets have masses smaller than $M^*$, but with 1% probability one can find droplets as heavy as $5M^*$.

3 Observable manifestations of quark droplets

After separation, the QGP droplets will recede from each other according to the global collective expansion, predominantly in the beam direction. Therefore, their c.m. rapidities $y_i$ will be in one-to-one correspondence with their spatial positions. One may expect that they will be distributed more or less uniformly between the target and the projectile rapidities. Since rescatterings in the dilute H phase are rare, most hadrons produced from individual droplets will go directly into detectors. This may explain why freeze-out parameters extracted from the hadronic yields are close to the phase transition boundary [20]. Indeed, due to the rapid expansion it is unlikely that the thermodynamical equilibrium will be established between the Q and H phases or within the H phase alone. If this were to happen, the final H phase would be more or less uniform, and thus there would be no traces of the droplet phase in the final state.

The final fate of individual droplets depends on their sizes and on details of the equation of state. Due to the additional Laplace pressure, $2\pi/R$, the residual expansion of individual droplets will slow down. The smaller droplets may even reverse their expansion and cooling to shrinking and reheating. Then, the conversion of Q matter into H phase may proceed through the formation of the imploding deflagration front [32, 33]. Bigger droplets may expand further until they enter the region of spinodal instability. At this stage the difference between 1-st and 2-nd order phase transitions or a crossover is insignificant. Since the characteristic “rolling down” time is rather short, $\sim 1$ fm/c [34], the Q droplets will be rapidly converted into the non-equilibrium H phase. In refs. [35, 36, 37] the evolution of individual droplets was studied numerically within a hydrodynamical approach including dynamical chiral fields. It has been demonstrated that the
energy released at the spinodal decomposition can be transferred directly into the collective oscillations of the \((\sigma, \pi)\) fields which give rise to the soft pion radiation. One can also expect the formation of Disoriented Chiral Condensates (DCC) in the voids between the Q droplets.

An interesting possibility arises if the metastable Q phase has a point of zero pressure. In particular, this is the case for the MIT bag model equation of state at temperatures only slightly below \(T_c\) [38]. In this case the droplets might be in mechanical equilibrium with the surrounding vacuum \((P_H \approx 0)\), like atomic nuclei or water droplets. The equilibrium condition is

\[
P_Q = \frac{\nu_Q}{2\pi^2} \left[ \frac{7\pi^4}{180} T^4 + \frac{\pi^2}{6} T^2 \mu^2 + \frac{1}{12} \mu_4 \right] = \frac{2\sigma}{R},
\]

where \(\nu_Q = 12\) is the degeneracy factor for massless u and d quarks (the gluon contribution is omitted here), and \(B\) is a bag constant. The evolution is then governed by the evaporation of hadrons from the surface (see also the discussion in Ref. [39]). One can speculate about all kinds of exotic objects, like e.g. strangelets, glueballs, formed in this way. The possibility of forming ”vacuum bubbles”, i.e. regions with depleted quark and gluon condensates, was discussed in ref. [35]. All these interesting possibilities deserve further study and numerical simulations.

![Image](image.png)

Figure 2: Schematic view of the momentum space distribution of secondary hadrons produced from an ensemble of droplets. Each droplet emits hadrons (mostly pions) within a rapidity interval \(\delta y \sim 1\) and azimuthal angle spreading of \(\delta \phi \sim 1\).

In the droplet phase the mean number of produced hadrons in a given rapidity interval is

\[
\langle N \rangle = \sum_i \frac{N_D}{m_i} = \langle n \rangle \langle N_D \rangle,
\]
where $\overline{n}$ is the mean multiplicity of hadrons emitted from a droplet $i$, $\langle n \rangle$ is the average multiplicity per droplet and $\langle N_D \rangle$ is the mean number of droplets produced in this interval. If droplets do not overlap in the rapidity space, each droplet will give a bump in the hadron rapidity distribution around its center-of-mass rapidity $y_i$ [28, 34]. In case of a Boltzmann spectrum the width of the bump will be $\delta y \sim \sqrt{T/m}$, where $T$ is the droplet temperature and $m$ is the particle mass. At $T \sim 100$ MeV this gives $\delta y \approx 0.8$ for pions and $\delta y \approx 0.3$ for nucleons. These spectra might be slightly modified by the residual expansion of droplets. Due to the radial expansion of the fireball the droplets should also be well separated in the azimuthal angle. The characteristic angular spreading of pions produced by an individual droplet is determined by the ratio of the thermal momentum of emitted pions to their mean transverse momentum, $\delta \phi \approx 3T/\langle p_\perp \rangle \sim 1$. The resulting phase-space distribution of hadrons in a single event will be a superposition of contributions from different Q droplets superimposed on a more or less uniform background from the H phase. Such a distribution is shown schematically in Fig. 2. It is obvious that such inhomogeneities (clusterization) in the momentum space will be reflected in strong non-statistical fluctuations of hadron multiplicities measured in a given rapidity and angular window. The fluctuations will be more pronounced if primordial droplets are big, as expected in the vicinity of the soft point. If droplets as heavy as 100 GeV are formed, each of them will emit up to $\sim 200$ pions within a narrow rapidity and angular intervals, $\delta y \sim 1$, $\delta \phi \sim 1$. If only a few droplets are produced in average per unit rapidity, $N_D \gtrsim 1$, they will be easily resolved and analyzed. On the other hand, the fluctuations will be suppressed by factor $\sqrt{N_D}$ if many small droplets shine in the same rapidity interval.

It is convenient to characterize the multiplicity fluctuations in a given rapidity window by the scaled variance

$$\omega_N \equiv \frac{\langle N^2 \rangle - \langle N \rangle^2}{\langle N \rangle}.$$  \hfill (10)

Its important property is that $\omega_N = 1$ for the Poisson distribution, and therefore any deviation from unity will signal a non-statistical emission mechanism. As shown in ref. [40], for an ensemble of emitting sources (droplets) $\omega_N$ can be expressed in a simple form, $\omega_N = \omega_n + \langle n \rangle \omega_D$, where $\omega_n$ is an average multiplicity fluctuation in a single droplet, $\omega_D$ is the fluctuation in the droplet size distribution and $\langle n \rangle$ is the mean multiplicity from a single droplet. Since $\omega_n$ and $\omega_D$ are typically of order of unity, the fluctuations from the multi-droplet emission are enhanced by the factor $\langle n \rangle$. According to the picture of a first order phase transition advocated above, this enhancement factor could be as large as $10^2$. Until now no strong anomalies in hadron multiplicities distributions have been observed in relativistic heavy-ion collisions (see e. g. ref. [41]).

4 Conclusions

- It is most likely that strongly interacting matter has at least two first order phase transitions, i.e. the nuclear liquid-gas transition and the deconfinement-hadronization transition. Their unambiguous experimental identification is the main goal of high-
energy heavy-ion collision experiments at present and future facilities. Studying phase transitions in such a dynamical environment should take into account strong non-equilibrium effects.

- A first order phase transition in rapidly expanding matter should proceed through the nonequilibrium stage when a metastable phase splits into droplets whose size is inversely proportional to the expansion rate. The primordial droplets should be biggest in the vicinity of a soft point when the expansion is slowest.

- Hadron emission from droplets of the quark-gluon plasma should lead to large non-statistical fluctuations in their rapidity and azimuthal spectra, as well as in multiplicity distributions in a given rapidity window. The hadron abundances may reflect directly the chemical composition in the plasma phase.

- To identify the phase transition threshold the measurements should be done at different collision energies. The predicted dependence on the expansion rate and the reaction geometry can be checked in collisions with different ion masses and impact parameters.

- If the first order deconfinement/chiral phase transition is only possible at finite baryon densities, one should try to identify it by searching for the anomalous fluctuations in the regions of phase space characterized by a large baryon chemical potential. These could be the nuclear fragmentation regions in collisions with very high energies (high-energy SPS, RHIC, LHC) or the central rapidity region in less energetic collisions (AGS, low-energy SPS, future GSI facility FAIR).

- A rich experience is accumulated in theoretical and experimental studies of nuclear multifragmentation as a signal of the liquid-gas phase transition in normal nuclear matter. One should use these lessons in future studies of the deconfinement-hadronization and chiral phase transitions in relativistic heavy-ion collisions.

I thank J. Randrup for fruitful discussions and useful advises. This work was supported in part by the grants RFFR 05-02-04013 and NS-8756.2006.2 (Russia).

References


