Homework Assignment #2

(Due Date: Wednesday, September 13, 12:40 pm, in class)

- 2.1 Baseball Trajectory (cf. Exercise 2.13 in the textbook) (7 pts.) Construct a FORTRAN program to calculate the 2-D trajectory of a baseball (mass 0.3 kg, radius 5 cm) including a drag force (but without spinning) on sea level with (constant) drag coefficient C=0.5 and initial speed $v_0=125$ mph.
 - (a) Calculate and plot the trajectories and ranges (using a linear interpolation) in still air for various launch angles Θ_0 in steps of 1° and determine the launch angle that gives the maximum range.
 - (b) Repeat part (a) using $\Theta_0=40^\circ$ only for a head wind of 20 mph, and for a tail wind of 20 mph.
 - (c) Implement a speed-dependent drag coefficient,

$$C(v) = 0.1 + \frac{0.4}{1 + \exp[(v - v_d)/\Delta]}$$
(1)

with $v_d=160 \ mph$ and $\Delta=10 \ mph$, and calculate the trajectories for fixed launch angle, $\Theta_0=40^\circ$, for $v_0=160$ and 210mph, and compare to results for constant C=0.5.

2.2 Table Tennis Ball with Spin (cf. Exercise 2.24 in the textbook) (3 pts.) Modify your code of the previous problem (but save it under a new name!) to describe the trajectory of a horizontally launched (smooth) table tennis ball (radius 2.0 cm, mass 3 g, initial height=1.2 m) with initial speed $v_0=4$ m/s. Include both a drag force and a Magnus force, $\vec{F}_M = S_0 \vec{\omega} \times \vec{v}$, with the axis of rotation out of the vertical plane of motion, $S_0/m=0.04$ (SI units) and $\omega=\pm 2\pi \cdot 10$ rad/s. Calculate and plot the trajectories for all three cases (no spin, "topspin" and "slice").