

Exam IV Solutions (fall '07)

1.) Multiple Choice

(18 pts.)

For each statement below, circle the correct answer (TRUE or FALSE, no reasoning required).

- (a) If the intensity of a sound source decreases by a factor of 100, the corresponding intensity level decreases by 20 dB.

TRUE

~~FALSE~~

- (b) Longitudinal waves cannot form standing waves.

TRUE

FALSE

- (c) If two substances are in thermal equilibrium with each other, the temperatures of the two substances must be identical.

TRUE

FALSE

- (d) The kinetic theory of ideal gases states that, at a fixed temperature, the average kinetic energy of a gas molecule increases with the mass of that molecule.

TRUE

FALSE

- (e) Spontaneous heat flow increases the total entropy of the universe.

TRUE

FALSE

- (f) In a reversible process, the total entropy of the universe increases.

TRUE

FALSE

No.	Points
1	TS
2	PJ
3	KR
4	RR
5	MS
6	DX
Sum	

V₂: F
T
F
T
T
F

2.) Doppler Effect

(15 pts.)

An Aggie student is driving in his car on a highway at a speed of 70mph. In front of him, a police car (at a speed of 95mph) is drawing away, while behind him a fire truck (at a speed of 55mph) is trailing him. All vehicles move straight ahead in the same direction. Both the police car and fire truck have their sirens on, both of which emit a pure tone of frequency 750Hz. (speed of sound: $v = 340\text{m/s}$; $1\text{m/s} = 2.25\text{mph}$)

[600Hz]

(a) With what frequency does the student hear the police car?

(b) With what frequency does the student hear the fire truck?

(b) What is the beat frequency the student hears?

$$(a) \boxed{f_L^{pol}} = \frac{v + v_L}{v + v_s^{pol}} = \boxed{728 \text{ Hz}} \quad [583 \text{ Hz}]$$

$$(b) \boxed{f_L^{truck}} = \frac{v - v_L}{v - v_s^{truck}} = \boxed{734 \text{ Hz}} \quad [587 \text{ Hz}]$$

$$(c) \boxed{f_{beat}} = f^{truck} - f^{pol} = \boxed{6 \text{ Hz}} \quad [4 \text{ Hz}]$$

3.) Stefan Boltzmann Radiation Law

(12 pts.)

The Sun has a radius of $R_S = 7 \cdot 10^8 m$ and a surface temperature of $T_S = 6000^\circ K$. The distance from Sun to Earth is $R_{SE} = 1.5 \cdot 10^{11} m$. Assume the Sun to be an ideal blackbody radiator. (the surface area of a sphere is $S = 4\pi R^2$)

- How much total power does the Sun radiate from its surface?
- Assuming the Sun's power output to propagate spherically into space without losses, what is the intensity of its radiation on the Earth's surface (assume that no radiation is absorbed in the atmosphere)?
- What is the equilibrium temperature on the Earth surface facing the Sun (neglect again the atmosphere and assume the Earth surface to be a blackbody)?

$$(a) \quad P = H = A \epsilon \sigma T^4 = 4.52 \cdot 10^{26} \text{ W}$$

$$(b) \quad I_E = \frac{P}{A} = \frac{P}{4\pi R_{SE}^2} = 1600 \frac{\text{W}}{\text{m}^2}$$

$$(c) \quad I = \frac{P}{A} = \epsilon \sigma T^4$$

$$\Rightarrow T = \sqrt[4]{\frac{I}{\epsilon \sigma}} = 410^\circ K$$

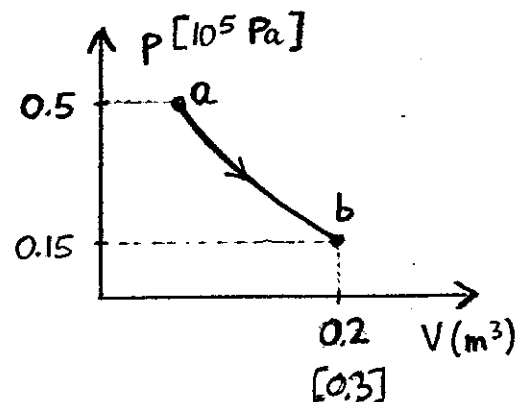
4.) Ideal Gas Law and 1. Law of Thermodynamics

(20 pts.)

The p - V diagram below illustrates an isothermal **expansion** of an ideal gas at temperature $T = 320^\circ\text{K}$.

[48]

- How many moles of the gas are involved?
- What is the volume of the gas at the initial point a ?
- How much work is done **by** the gas from a to b ?
- By how much did the internal energy of the gas change?



(a) at point b : $pV = nRT$

$$\Rightarrow \boxed{n = \frac{pV}{RT} = 1.128 \text{ mol}}$$

(b) $p_a V_a = p_b V_b \Rightarrow \boxed{V_a = V_b \frac{p_b}{p_a} = 0.06 \text{ m}^3}$ [0.09 m³]

(c) $\boxed{W = nRT \ln\left(\frac{V_b}{V_a}\right) = 3613 \text{ J}}$ [5420 J]

(d) $\boxed{\Delta U = \frac{3}{2} nR\Delta T = 0}$

5.) Heat Extraction and Refrigerator

[4.5]

(15 pts.)

A freezer has a coefficient of performance of 3.2. A person puts 2.5 kg of water at an initial temperature of 20°C into a freezer whose inside temperature is at a constant -8°C .

($L_f = 3.34 \times 10^5 \text{ J/kg}$, $c_w = 4.186 \times 10^3 \text{ J/kg}^\circ\text{C}$, $c_{ice} = 2.01 \times 10^3 \text{ J/kg}^\circ\text{C}$)

- How much heat must be removed from the water to convert it into ice at -8°C ?
- How much electrical energy does the freezer need for the freezing process in part (a)?
- How much excess heat does the freezer dump into its environment?

(a) $Q_c = m (\Delta T_w c_w + \Delta T_i c_i + L_f)$

$Q_c = 1.085 \times 10^6 \text{ J}$ [$1.952 \times 10^6 \text{ J}$]

(b) $K = \frac{Q_c}{W} \Rightarrow W = \frac{Q_c}{K} = 3.39 \times 10^5 \text{ J}$ [$6.10 \times 10^5 \text{ J}$]

(c) $Q_H = Q_c + W = 1.42 \times 10^6 \text{ J}$ [$2.56 \times 10^6 \text{ J}$]

6.) Heat Pump and Entropy

[5°F]

(20 pts.)

During winter time (outside air temperature $T_{out} = 25^\circ F$), a person would like to heat his living room from $55^\circ F$ to $75^\circ F$ using his Carnot heating system. The room, which has a volume of $120m^3$ is filled with air of density $\rho_{air} = 1.3kg/m^3$. Treat the inside air as an ideal monatomic gas with a molar mass of $32g$ at constant volume. Be sure to use SI units in your calculations.

- (a) How many moles of air are in the room? (recall: density=mass per volume)
- (b) How much heat needs to be added to the room to achieve the desired increase in temperature?
- (c) Calculate the Carnot efficiency of the heating system using the average temperature of the inside air during the heating process.
- (d) Using the Carnot efficiency from part (c), calculate the work required by the heating system to heat up the room.
- (e) Calculate the entropy change of: (i) the inside air; (ii) the outside reservoir; (iii) the universe.

$$(a) \quad n = \frac{M_{tot}}{M_{mol}} \quad M_{mol} = 0.032 \text{ kg} \quad M_{tot} = V \rho = 156 \text{ kg} \quad \Rightarrow \quad n = 4875 \text{ mol} \quad [4266 \text{ mol}]$$

$$(b) \quad Q_H = n C_v \Delta T = n \frac{3}{2} R \Delta T = 6.75 \times 10^5 \text{ J} \quad [5.91 \times 10^5 \text{ J}]$$

$$\Delta T [K^\circ] = \Delta T [F^\circ] \times \frac{5}{9}$$

$$(c) \quad e_{Carnot} = 1 - \frac{T_c}{T_H} = 1 - \frac{269.3}{291.5} = 0.07616 \quad [0.1144]$$

$$T_c = 269.3^\circ K, \quad T_H = 291.5^\circ K$$

(258.15)

$$(d) \quad W = e Q_H = 5.14 \times 10^4 \text{ J} \quad [6.76 \times 10^4 \text{ J}]$$

$$(e) \quad (i) \quad \Delta S_{in} = \frac{Q_H}{T_H} = \frac{6.75 \times 10^5}{291.5} = +2316 \frac{\text{J}}{\text{K}} \quad [2027.5 \frac{\text{J}}{\text{K}}]$$

$$(ii) \quad \Delta S_{out} = \frac{-Q_c}{T_c} = \frac{-(Q_H - W)}{269.3} = -2316 \frac{\text{J}}{\text{K}} \quad [-2027.5 \frac{\text{J}}{\text{K}}]$$

$$\left. \begin{array}{l} \Delta S_{tot} \\ = 0 \\ \text{(REVERSIBLE!)} \end{array} \right\}$$