PHYS 606 - Spring 2015 - Homework X - Solution

Problem [1]

$$|a_{i}|L_{i}, r_{i}| = \epsilon_{ike} \left[r_{k} P_{e}, r_{i} \right] = \epsilon_{ike} \left(r_{k} \left[P_{e}, r_{i} \right] + \left[r_{k}, r_{i} \right] P_{e} \right) = i\hbar \epsilon_{ijk} r_{k}$$

$$-i\hbar \sigma_{je}$$

$$[L_{i}, p_{i}] = \epsilon_{ike} \left[r_{k} \left[p_{e}, p_{i} \right] + \left[r_{k}, p_{i} \right] p_{e} \right) = i\hbar \epsilon_{ijk} \epsilon_{ijk}$$

$$[L_{i}, K_{i}] = \left[L_{i}, \epsilon_{ik} - p_{i} t \right] = i\hbar \epsilon_{ijk} \left(m r_{k} - p_{k} t \right) = i\hbar \epsilon_{ijk} k_{k}$$

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$$[L_{i}, K_{i}] =$$

Problem [2]

(f) Use
$$H_{n}(\xi) = (-1)^{n} e^{\frac{\xi^{2}}{d\xi^{n}}} e^{-\frac{\xi^{2}}{2}}$$
 (#WIII, [])

 $H_{n+1}(\xi) = (-1)^{n+1} e^{\frac{\xi^{2}}{d\xi^{n}}} \frac{d^{n}}{(-2\xi)} e^{-\frac{\xi^{2}}{2}} = (-1)^{n+1} e^{\frac{\eta^{2}}{2}} \left(-2n \frac{d^{n-1}}{d\xi^{n-1}} - 2\xi \frac{d^{n}}{d\xi^{n}}\right) e^{-\frac{\xi^{2}}{2}}$
 $= -2n H_{n-1}(\xi) + 2\xi H_{n}(\xi)$ voluth is the relation from (3).

Problem [3]

(a) From
$$X$$
. 4 in the lecture notes we already know that the radical equation for $R(r)$ in the case $V(P) = 0$ is

$$\begin{bmatrix}
-\frac{k^2}{2m} & \frac{1}{r^2} & \frac{d}{dr} \left(r^2 & \frac{d}{dr}\right) + \frac{R(2r)h^2}{2mr^2} & R(r) = ER(r)
\end{bmatrix}$$
Throduce $g = \frac{1}{4} \sqrt{dmE} = kr$ with $k = \frac{1}{4} \sqrt{kmE}$ (here exists of the fee particle)

$$\frac{1}{s^2} \frac{d}{ds} \left(s^2 \frac{d}{ds}\right) R_0 - \frac{2(2r)}{s^2} R_0 + R_0 = 0$$

$$\Rightarrow \frac{d^2}{ds^2} R + \frac{2}{s} \frac{dR}{ds} + \left(1 - \frac{2(2r)}{s^2}\right) R = 0$$
(b) Ansale $j_{e_1}(s) = \frac{1}{2^{e_1}} \int_{-1}^{1} e^{iss} \left(1 - s^2\right)^e ds$ (clookumou as Prisson's integral expresentation for sub (κ) : Integral expresentation for sph. Becare gits.)

$$\frac{1}{s^2} \int_{-1}^{1} \frac{ds}{ds} \left(1 - s^2\right)^e ds + 2lg^{e_1} \int_{-1}^{1} \left(is\right) e^{iss} \left(i - s^2\right)^e ds + l(l-1)g^{e_2} \int_{-1}^{1} e^{iss} \left(1 - s^2\right)^e ds$$

$$\frac{1}{s^2} \int_{-1}^{1} \frac{ds}{ds} \left(1 - s^2\right)^e ds + 2lg^{e_1} \int_{-1}^{1} \left(is\right) e^{iss} \left(1 - s^2\right)^e ds + g^{e_2} \int_{-1}^{1} e^{iss} \left(1 - s^2\right)^e ds$$

$$- l(2r1) s^{e_2} \int_{-1}^{1} e^{iss} \left(1 - s^2\right)^e ds + 2lg^{e_1} \int_{-1}^{1} e^{iss} \frac{ds}{ds} \left(1 - s^2\right)^e ds$$

$$\Rightarrow g^2 \int_{-1}^{1} e^{iss} \left(1 - s^2\right)^e ds + 2lg^{e_1} \int_{-1}^{1} e^{iss} \frac{ds}{ds} \left(1 - s^2\right)^e ds$$

$$\Rightarrow g^2 \int_{-1}^{1} e^{iss} \left(1 - s^2\right)^e ds + 2lg^{e_1} \int_{-1}^{1} e^{iss} \frac{ds}{ds} \left(1 - s^2\right)^e ds$$

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Suppose sock known (1)
$$e^{2} = e^{2} = e^{2}$$

