

1. A coil of diameter 1 cm and length 3 cm contains 60 turns. Assume it is an ideal solenoid.

- 7 Points (a) What is its inductance?
- 6 Points (b) It is hooked in series with a  $3M\Omega$  resistor. What is the time constant of this circuit?
- 6 Points (c) A 30V battery is hooked to the circuit described in (b). After 10 minutes, what is the energy stored in the inductor?
- 6 Points (d) This inductor is now hooked in parallel with a capacitor. What value of  $C$  is required so that the resonant frequency  $f = 100$  MHz? Assume the inductor has zero resistance.

- 7 Points 2. (a) A model-train transformer plugs into 120 V ac, and draws 0.80 A while supplying 15 A to the train. What voltage is present across the tracks?

- 6 Points (b) A simple generator has a 500-loop square coil 15.0 cm on a side. How fast must it turn in a 0.350-T field to produce a 120-V peak output?

- 6 Points (c) The counter emf in a motor is 72 V when operating at 1250 rpm. What would be the counter emf at 2500 rpm if the magnetic field is unchanged?

- 6 Points (d) If the electric field in an EM wave has a peak value of  $0.62 \times 10^{-4}$  V/m, what is the peak value of the magnetic field strength?

3. Suppose a 60-kW radio station emits EM waves uniformly in all directions.

- 9 Points (a) How much energy per second crosses a  $1.0\text{-m}^2$  area 20 m from the transmitting antenna?

- 8 Points (b) What is the rms magnitude of the  $\mathbf{E}$  field at this point, assuming the station is operating at full power?

- 8 Points (c) What is the voltage induced in a 1.5-m-long vertical car antenna at this distance?

4. Suppose a conducting rod (mass  $m$ , resistance  $R$ ) rests on two frictionless and resistanceless parallel rails a distance  $l$  apart in a uniform magnetic field  $\mathbf{B}$  ( $\perp$  to the rails and the rod). At  $t = 0$ , the rod is at rest and a source of emf ( $\mathcal{E}_0$ ) is connected to the points a and b.

- 5 Points (a) Write the equation for the current in the rod when it has attained a velocity  $v$ .

- 5 Points (b) Write the equation for the force on the rod when it has attained a velocity  $v$ .

- 10 Points (c) Derive an expression for the velocity of the rod as a function of time.

- 5 Points (d) What is the velocity of the rod after a long time (assume it is still on the rails and in the magnetic field)?

